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# COLLOCATION FLUTTER ANALYSIS STUDY

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VOLUME IV.

CUFA - COMPUTER PROGRAM TO PERFORM FLUTTER  
ANALYSIS BY THE COLLOCATION METHOD

APRIL 1969



MISSILE SYSTEMS DIVISION

**HUGHES**

HUGHES AIRCRAFT COMPANY

COFA

COLLOCATION FLUTTER ANALYSIS STUDY

VOLUME IV

COFA - COMPUTER PROGRAM TO  
PERFORM FLUTTER ANALYSIS BY THE COLLOCATION METHOD

Prepared by Dynamics & Environments Section Personnel  
Hughes Aircraft Company, Missile Systems Division  
Contract No. 00019-68-L-0247

APRIL 1969

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## TABLE OF CONTENTS

<u>Section</u>		<u>Page</u>
	ABSTRACT . . . . .	ii
1	INTRODUCTION . . . . .	1
2	SIGN CONVENTION . . . . .	2
3	DERIVATION OF EQUATIONS . . . . .	3
4	REFERENCES . . . . .	13
5	DESCRIPTION OF PROGRAM INPUT . . . . .	14
6	DESCRIPTION OF PROGRAM OUTPUT . . . . .	40
7	EXAMPLE PROBLEMS . . . . .	42
8	PROGRAM LISTING . . . . .	62
9	FLOW DIAGRAM . . . . .	101
10	NOMENCLATURE . . . . .	188

## ABSTRACT

→ A collocation solution of the flutter and vibration problems for a multiple component system is presented. The formulation utilizes structural, aerodynamic, and inertial characteristics in the form of matrices of structural and aerodynamic influence coefficients and a mass matrix, respectively, for each component. The use of a rigid-body modal matrix permits a general analysis for a system free in space with up to six rigid-body degrees of freedom.

The computer program provides the flutter or vibration solution for a system composed of as many as 20 flexible components with a maximum total of 49 collocation control points. An option is provided to vary the density as well as the reduced velocity. Another option is provided to yield the modes from a vibration analysis in a punched-card format for use in flutter analysis by modal methods. ( )

## SECTION I

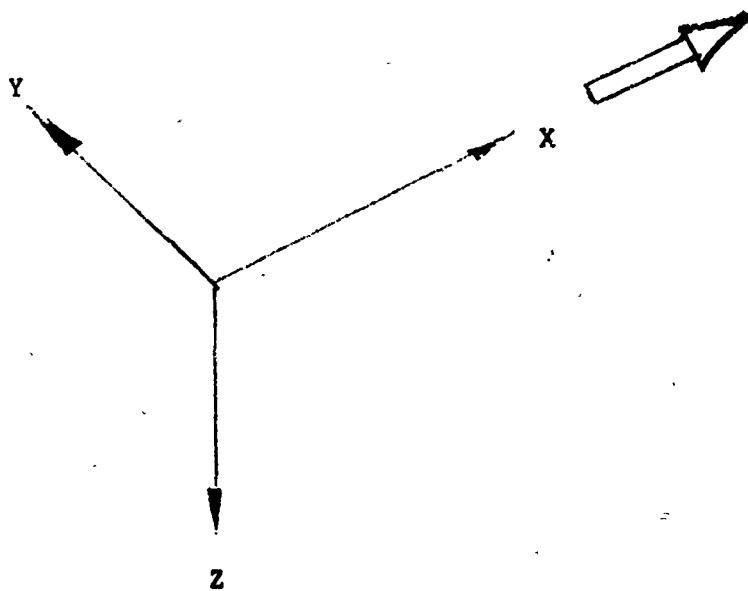
### INTRODUCTION

The mathematical formulation of the flutter problem results in a set of integral equations whose closed form solution is impossible to obtain for most practical problems. One of the most useful approximate methods of solving these equations is by direct collocation. A solution by collocation is one in which the equations are satisfied at a finite number of selected points on the structure. These points, known as collocation points, are satisfied simultaneously. The collocation solution results in a matrix formulation which when cast in the canonical form will yield eigenvalues that are directly related to the flutter stability parameters. This manual presents a digital computer program that will perform collocation flutter analyses. The computer program, which is written in Fortran IV, was developed by Rodden, Farkas, and Malcom in Reference 1.

The collocation formulation of the flutter problem has been presented in Reference 2. The equations are presented for analysis of single component systems restrained (cantilevered) in space and for sysmmetrical systems free in space undergoing either symmetric or antisymmetric flutter. A method of generalizing the matrix equation for free-free flutter to include up to six rigid-body degrees of freedom has been given in Reference 3. The present program extends the formulation of Reference 2 to include an arbitrary combination of rigid-body degrees of freedom (Ref. 3), and to consider more than one flexible component. In addition, an option has been provided to vary the altitude (i. e. density) as well as the reduced velocity. Finally, options have been added to carry out a vibration analysis (which requires no aerodynamic data) and to provide vibration modes in punched-card format for use in a modal flutter or vibration analysis.

## SECTION 2

The NASA body axis system with the x, y, and z axes directed forward, starboard, and downward, respectively, is recommended for consistency with the formulation of the static aeroelastic problems in Reference 4. However, the usual flutter convention with the x, y and z axes directed aft, starboard and downward, respectively, may be used instead. In either case, the vertical normal force and deflection are positive downward.



## SECTION 3

### DERIVATION OF EQUATIONS

The integral equations of aeroelasticity consist of two basic relationships: The first is the relation between the structural deformation, the structural influence function, and the inertial and aerodynamic loadings; the second is the relation between the aerodynamic disturbance (downwash), the aerodynamic influence (kernel) function, and the aerodynamic pressure. A collocation formulation of the deformation integral equation for a vehicle free in space may be written in matrix form by requiring that the integral equation be satisfied at a discrete set of control points. We choose a single type of coordinate, viz., the deflection  $h$ , as an adequate measure of both the deformation and the free-stream disturbance, not only for simplicity in the resulting equations but also because deflections have a more general meaning on a cambered vehicle and deflection influence coefficients are more readily obtained from a structural analysis than slope (or twist) influence coefficients. The resulting deformation matrix equation is

$$\{h_1\} - \{h_0\} = K[a] (\{F_i\} + \{F_a\}) \quad (1)$$

where  $\{h_1\}$  is the set of components of the absolute deflections of the control points,  $\{h_0\}$  is the set of components of the deflections of the control points due to the rigid-body motion of some reference points,  $[a]$  is the set of structural influence coefficients (SICs, or flexibility matrix) for the system cantilevered from (or otherwise restrained at) the reference point,  $\{F_i\}$  is the set of inertial force components integrated throughout the region adjacent to each control point,  $\{F_a\}$  is the set of aerodynamic force components integrated over the vehicle surface adjacent to each control point, and the scalar  $K$  has been introduced as a factor to the SICs for convenience in investigating variations in stiffness levels. The inertial forces may be written in terms of a mass matrix  $[M]$  and the control point accelerations.

$$\{F_i\} = -(1/386)[M]\{h_1\} \quad (2)$$

where the diagonal elements of the mass matrix are found from integrating the structural mass density throughout the region adjacent to the control points. (N. B., the mass matrix need not be diagonal, and, in general, will not be so if the elements must be derived from a set of weight data previously lumped at a system of control points different from those required in the aeroelastic analysis. The use of a coupled mass matrix permits simulation of given inertial characteristics at a set of control points frequently dictated by more difficult aerodynamic considerations.)

A collocation formulation of the aerodynamic integral equation is more difficult than in the case of the deformation integral equation because of the singularities in the aerodynamic kernel function. The determination of three relationships is necessary to derive a set of aerodynamic influence coefficients (AICs) that relate the control point forces to the deflections. The most basic and difficult is the pressure-downwash relation that is derived from numerical analysis of the aerodynamic integral equation. The simpler relations are the numerical integration of the pressure to obtain the force, and the numerical substantial differentiation of the deflection to obtain the downwash. The effort involved in each step depends on the planform, Mach number regime, and frequency range; a survey of the status of unsteady AICs is given in Ref. 4. For present purposes, it is sufficient to state the definition of the AICs in the oscillatory case. We write the aerodynamic control point forces in terms of the control point deflections as

$$\{F_a\} = (4\pi^2/12)\rho f^2 b_r^2 s [W] [C_h] \{h_1\} \quad (3)$$

where  $[C_h]$  is the theoretically derived dimensionless (complex) matrix of oscillatory AICs,  $f$  is the frequency of the assumed harmonic motion,  $\rho$  is the atmospheric density,  $b_r$  is the reference semichord,  $s$  is the reference span, and  $[W]$  is an empirically derived weighting matrix

for modification of the theoretical AICs. A method for obtaining the elements of the weighting matrix has been suggested in Ref. 4.

The sum of the force components may be written now from Eqs. (2) and (3) for the case of harmonic motion.

$$\{F_i\} + \{F_a\} = (4\pi f^2 / 386)([M] + 32.174 \rho b_r^2 s[W][C_h])\{u_1\} \quad (4a)$$

$$= (4\pi f^2 / 386)[\bar{M}]\{h_1\} \quad (4b)$$

We next discuss the manner of inclusion of the rigid-body degrees of freedom in Eq. (1). The matrix  $\{h_o\}$  has been defined as the set of components of the deflections of the control points due to the rigid-body motion of the reference point. Each component of the control point deflections  $h_o$  is linearly related to the rigid-body translations and rotations, provided the rotations are small. Therefore, we may define a rigid-body modal matrix  $[h_R]$  as the transformation

$$\{h_o\} = [h_R] \{a_R\} \quad (5)$$

where  $\{a_R\}$  is the set of amplitudes of rigid-body translations and rotations of the reference point. As an example, if we consider symmetrical vertical motion,  $[h_R]$  is composed of two columns: the first is a unit column corresponding to the plunging mode, the second consists of the x-coordinate of each control point corresponding to the pitching mode;  $[a_R]$  is composed of two elements: the first is the plunging displacement  $z_o$ , the second is the pitching angular displacement  $\theta$ .

Before proceeding in the derivation, we should review the format of the various matrices in the case of a multiple flexible component system. As an example, we consider a symmetrical flutter analysis of an aircraft whose wing, aft fuselage, and tail are flexible, and whose forward fuselage may be assumed to be rigid. We assume that the reference point (cantilever point) can be located in the vehicle such that

its various components are independent. If we choose a point at the intersection of the wing and fuselage, then the wing is independent of the aft fuselage-tail combination, but the tail and aft fuselage must be considered together. The motion of the rigid forward fuselage is determined by the motion of the reference point, and the forward fuselage will not enter into any flexible considerations but only into the free-free boundary conditions. From the foregoing, it is seen that the various matrices will appear in partitioned form. If we denote the wing and aft fuselage-tail system by the subscripts 1 and 2, respectively, then the flexibility matrix appears as

$$[a] = \begin{bmatrix} a_1 & 0 \\ 0 & a_2 \end{bmatrix} \quad (6)$$

the mass matrix as

$$[M] = \begin{bmatrix} M_1 & 0 \\ 0 & M_2 \end{bmatrix} \quad (7)$$

the weighting matrix as

$$[W] = \begin{bmatrix} W_1 & 0 \\ 0 & W_2 \end{bmatrix} \quad (8)$$

the AICs as

$$[C_h] = \begin{bmatrix} C_{h1} & 0 \\ 0 & C_{h2} \end{bmatrix} \quad (9)$$

and the rigid-body modal matrix as

$$[h_R] = \begin{bmatrix} h_{R1} \\ h_{R2} \end{bmatrix} \quad (10)$$

Two requirements should be emphasized with regard to the AICs. The first concerns the proper inclusion of the reference geometry associated with the nondimensional AICs. The dimensional form of Eq. (9) may be written.

$$b_r^2 s [C_h] = \begin{bmatrix} b_1^2 s_1 C_{h1} & 0 \\ 0 & b_2^2 s_2 C_{h2} \end{bmatrix} \quad (11)$$

where  $b_r$  and  $s$  are the reference semichord and span of the composite system,  $b_1$  and  $s_1$  are the reference geometry for the first component, and  $b_2$  and  $s_2$  are the reference geometry for the second component. The second requirement is that the AICs for each component must be determined for the same "dimensional" reduced velocity  $V/\omega$ . If the reference reduced velocity is

$$1/k_r = V/b_r \omega \quad (12)$$

then the reduced velocity for the first component must be

$$1/k_1 = (1/k_r)(b_r/b_1) \quad (13)$$

and, for the second component,

$$1/k_2 = (1/k_r)(b_r/b_2) \quad (14)$$

Both of these requirements can be met in formulating the composite AICs by choosing the same reference geometry in determining the AICs for each component.

The rigid-body modal matrix provides the basis for a general statement of the boundary conditions for the free-free flutter of the composite system. The boundary conditions for harmonic motion may be written as

$$[h_R]^T [\bar{M}] \{h_1\} + [\Delta \bar{m}] \{a_R\} = \{0\} \quad (15)$$

where  $[\Delta \bar{m}]$  is an incremental generalized mass matrix, including aerodynamic effects, of any rigid component of the system attached to the reference point (e.g., the forward fuselage that was assumed to be rigid in the foregoing example),\* and is not considered in the formulation of the flexible component mass and aerodynamic matrices. The form of the matrix  $[\Delta \bar{m}]$  may be illustrated by the previous example with a rigid forward fuselage again in symmetrical motion. We may write

$$[\Delta \bar{m}] = [\Delta m] + [\Delta Q] \quad (16)$$

---

\* N.B.: It is assumed that no dynamic coupling exists between the rigid and flexible components. A suitable distinction can always be made between the rigid and flexible components such that this requirement can be met.

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where the generalized rigid component mass matrix of the forward fuselage is

$$[\Delta m] = \begin{bmatrix} M_o & S_o \\ S_o & I_{yo} \end{bmatrix} \quad (17)$$

in which  $M_o$ ,  $S_o$ , and  $I_{yo}$  are the mass, static unbalance about the reference point, and pitching moment of inertia about the reference point, respectively, of the forward fuselage, and the generalized aerodynamic forces on the forward fuselage (if not negligible) are found from

$$[\Delta Q] = 32.174 \rho b_o^2 s_o [h_{Ro}]^T [C_{ho}] [h_{Ro}] \quad (18)$$

where  $[h_{Ro}]$  is the rigid-body modal matrix,  $[C_{ho}]$  is the set of AICs, and  $b_o$  and  $s_o$  are the reference geometry for the forward fuselage. Again the AICs must be found for the reduced velocity of the composite system.

We are now in a position to eliminate the rigid-body degrees of freedom and to formulate the eigenvalue problem for the flutter of the flexible free-free system. Substituting Eqs. (4b) and (5) into Eq. (1), and adding the structural damping factor  $1/(1 + ig)$  to the flexibility matrix to provide the artificial structural damping necessary to sustain the assumed harmonic motion of the flutter system, we obtain

$$\{h_1\} - [h_R] \{a_R\} = (4\pi^2 K_f^2 / 386(1 + ig)) [a] [\bar{M}] \{h_1\} \quad (19)$$

or  $\lambda(\{h_1\} - [h_R] \{a_R\}) = [a] [\bar{M}] \{h_1\} \quad (20a)$

$$= [U] \{h_1\} \quad (20b)$$

where  $\lambda$  denotes the eigenvalue

$$\lambda = \lambda_R + i\lambda_I \quad (21a)$$

$$= 386(1 + ig)/4\pi^2 K_f^2 \quad (21b)$$

Premultiplying Eq. (20b) by  $[h_R]^T [\bar{M}]$ , and multiplying Eq. (15) by  $\lambda$  and subtracting, permits solution for the amplitudes of the rigid-body motion

$$\lambda \{a_R\} = -[\bar{m}]^{-1} [h_R]^T [\bar{M}] [U] \{h_1\} \quad (22)$$

where

$$[\bar{m}] = [h_R]^T [\bar{M}] [h_R] + [\Delta \bar{m}] \quad (23)$$

Finally, substituting Eq. (22) into Eq. (20b) yields the generalized matrix equation for free-free flutter

$$\lambda \{h_1\} = ([I] - [h_R][\bar{m}]^{-1}[h_R]^T [\bar{M}]) [U] \{h_1\} \quad (24)$$

The solution of Eq. (24) for the complex eigenvalues leads to the free-frequency and the required structural damping. From Eq. (21), we obtain the frequency

$$f = (1/2\pi) \sqrt{386/K\lambda_R} \quad (25)$$

and the required structural damping

$$g = \lambda_I/\lambda_R \quad (26)$$

Since the formulation of the AICs requires the assumption of a reduced velocity  $1/k_r$ , the velocity follows from that and the frequency obtained in Eq. (25)

$$U = 0.5921 (2\pi f b_r) (1/k_r) \quad (27)$$

Equation (24) is seen to be completely general, being applicable from the cantilever case (in which we let  $[h_R]$  vanish) to the case of six rigid body degrees of freedom, and for a vibration analysis for which the aerodynamic terms and required structural damping are deleted. We observe that Eq. (24) is a matrix formulation of the algebraic procedures for free-free vibration analysis described in Ref. 4 (Par. 11.2).

From a series of solutions of Eq. (24) for various reduced velocities, the conventional required damping versus velocity stability curve can be constructed for a specific altitude, and the flutter point is determined as the velocity for which the required damping and actual damping are equal. An alternative approach to the flutter analysis is based on a single representative reduced velocity and a series of solutions of Eq. (24), carried out for various densities. The density at which the required damping and actual damping are equal may be used to find a stiffness-altitude similarity parameter for flutter from which the flutter stability may be determined. However, at present, the validity of this latter approach requires further investigation, particularly the sensitivity of the results to the choice of representative reduced velocity.

The generalized mass corresponding to each free vibration mode is of interest in various modal analyses of flying qualities, stability and control characteristics, or transient response of flexible vehicles. If Eq. (24) is solved for the free vibration modes (by deleting the aerodynamic terms) then the  $n$ 'th generalized mass is given by

$$m^{(n)} = \{h_1^{(n)}\}^T [M] \{h_1^{(n)}\} + \{a_R^{(n)}\}^T [\Delta m] \{a_R^{(n)}\} \quad (28)$$

where  $\{h_1^{(n)}\}$  is the n'th free vibration mode and the corresponding rigid component mode is found from Eq. (22)

$$\{a_R^{(n)}\} = - \frac{4\pi^2 K}{386} f_n^2 [M]^{-1} [h_1^{(n)}]^T [M] [U] \{h_1^{(n)}\} \quad (29)$$

## SECTION 4

### REFERENCES

1. W. P. Rodden, E. F. Farkas and H. A. Malcom. "Flutter and Vibration Analysis by a Collocation Method: Analytical Development and Computation Procedure". Aerospace Corporation Report No. TDR-169(3230-11)TN-14, 31 July 1963.
2. W. P. Rodden, "Matrix Approach to Flutter Analysis" Institute of the Aerospace Sciences Fairchild Fund Paper No. FF-23, May 1958; based on North American Aviation, Inc., Report NA-56-1070, 1 May 1956.
3. W. P. Rodden, "On Vibration and Flutter Analysis with Free-Free Boundary Conditions". Journal of the Aerospace Sciences, 28 (1961) 65.
4. W. P. Rodden and J. D. Revell. "The Status of Unsteady Aerodynamic Influence Coefficients". Institute of Aerospace Sciences Fairchild Fund Paper No. FF-33, 23 January 1962; preprinted in Aerospace Corporation Report TDR-930(2230-09) TN-2, 22 November 1961.
5. R. L. Bisplinghoff, H. Ashley, and R. L. Halfman. Aeroelasticity. Reading: Addison-Wesley Publishing Company, Inc., 1955.
6. R. H. Scanlan and Robert Rosenbaum. Introduction to the Study of Aircraft Vibration and Flutter. New York: The MacMillan Company, 1951.

## SECTION 5

### DESCRIPTION OF PROGRAM INPUT

#### UNITS

The dimensional data required for each component consist of the mass matrix in pounds, the flexibility matrix in inches per pound, and the reference semichord and semispan in feet. The aerodynamic influence coefficients are dimensionless. In the case of free-free analysis, the rigid-body mass matrix, e.g., in a symmetrical analysis if  $S_0$  and  $I_{yo}$  are given in the foot-pound system, the x-coordinates which correspond to the rigid body pitching mode must be measured in feet, whereas if  $S_0$  and  $I_{yo}$  are given in the inch-pound system, the x-coordinate must be measured in inches. The density is required in slugs per cubic foot.

#### CLASSES OF DATA AND PROBLEMS

Five classes of data must be provided: mass, aerodynamic influence coefficients (AICs) and their weighting matrices, structural influence coefficients, the rigid-body motion modal matrix, and the rigid component generalized mass characteristics. The cantilever case does not require either the rigid body modal matrix or the generalized masses. (For a vibration analysis, the aerodynamic input is not required.)

Several classifications of problems may be analyzed using the collocation flutter analysis program. They are cantilever flutter analysis - the structure is restrained from plunging motion. Free-free flutter analysis the structure is free to pitch, plunge, and roll. The  $\alpha$ -free cases may have rigid components and flexible components. However, when flexible components are coupled together, the structural attachment between component must be statically determinate. When rigid body components are used, any number up to six rigid body modes may be used. Also vibration analyses may be performed when zero aerodynamic forces are used.

## PROGRAM RESTRICTIONS AND OPTIONS

1. The maximum number of control points that can be used for all flexible components of any system is 49. A maximum of 49 control points may also be used for the rigid component for the purpose of deriving the generalized aerodynamic force.
2. The maximum number of flexible components is 20.
3. The maximum number of values used in the reference reduced velocity ( $1/K_R$ ) series is 20.
4. The maximum number of values used in a density series is 20.
5. The program provides for varying the densities with each  $(1/K_R)$  or for using the same densities with all  $(1/K_R)$ 's.
6. The maximum number of output modes is 25.
7. The maximum number of rigid-body motion modes is 6.
8. It is possible to reserve a partition in the upper left-hand corner of the flexible components AIC matrices for control points whose aerodynamic forces may be neglected or found from an alternate theory to that used for the primary control points. This partition is termed the external stores region since external stores are an example of a source of additional control points requiring such special consideration. The maximum number of control points that can be reserved on each flexible component for external stores is 48.
9. A weighting matrix is an optional input for each flexible component. The order of this matrix must be identical with the order of the AIC matrices for the particular component.
10. Any number of complete sets (decks) of input data may be stacked and run in one machine pass.

## DATA DECK SETUP

### Loading Order

The data decks are assembled using cards punched from keypunch forms and/or card that are punched-card output from appropriate computer programs. The data items in each deck have the following order,

with the exception that some of the items may be omitted if indicators used in the control cards specify their absence.

1. Title card
2. Data deck general control card
3. K card (flexibility matrix scale factor)
4. Data card for change in matrix iteration tests
5. Control card(s) for external stores and weighting matrices
6. Reference semichord ( $b_r$ ) and reference reduced velocities ( $1/k_r$ )'s
7. Reference semichord ( $b_{ri}$ ) and reference semispan ( $S_i$ ) for rigid and flexible components (surfaces)
8. Density series (if same densities are used for all  $(1/k_r)$ 's)
9. Generalized mass matrix ( $[\Delta m]$ ) for rigid components
10. Mass matrix ( $[M]_i$ ) for each flexible surface
11. Rigid-body motion modal matrix ( $[h_{R_o}]$ ) for rigid component
12. Rigid-body motion modal matrix ( $[h_{R_i}]$ ) for each flexible surface
13. Flexibility matrix ( $[\alpha]_i$ )
14. Weighting matrices ( $[W]_i$ )
15. Aerodynamic input repeated for each  $(1/k_r)$ 
  - a. Density series cards (if densities vary with each  $(1/k_r)$ )
  - b. AIC matrix ( $[C_{h_o}]$ ) for rigid component (if present)
  - c. AIC matrix ( $[C_h]_i$ ) for each flexible surface

Input Data Description

1. The title card may contain any alphanumeric characters desired in Columns 2 through 72.

2. Data deck general control card (FORMAT 18I4):

Col	1-4	5-8	9-12	13-16	17-20	21-24	25-28	29-32	33-36
Name	NSUR	NAERO	NRIGID	NFUS	NDENS	MODES	NDELM	NPUNCH	NCOM
Field	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)

- NSUR: Number of flexible components (surfaces),  $\leq 20$ .  
 NAERO: Number of reference reduced velocities,  $\leq 20$ ; NAERO = 0 is used for vibration analyses.  
 NRIGID: Number of rigid-body motion modes to be input (= number of columns in  $[h_R]$ ); NRIGID = 0 for the cantilever case.  
 NFUS: NFUS must = 1 if AICs  $([C_{ho}])_j$ ,  $j = 1$ , NAERO are input for the rigid components; NFUS = 0 if  $[C_{ho}]$  is not input.  
 NDENS: If NDENS = 0 the densities are to vary with each  $1/k_r$  and are input as part of Item 15; if NDENS > 0 this number of densities must be input as Item 8, and each density value will be used for all  $(1/k_r)$ 's.  
 MODES: Number of output modes,  $\leq 25$ .  
 NDELM: NDELM = 0 if no rigid component generalized mass matrix  $([\Delta m])$  is input; NDELM = 1 if  $[\Delta m]$  is input.  
 NPUNCH: This indicator is used to obtain a printout of the dynamic matrix  $([U])$  and to obtain the frequencies and modes in punched-card format; NPUNCH = 0 if no printout of  $[U]$  or punched output is desired; NPUNCH = 1 if only punched-card output is desired and NPUNCH = -1 will provide the printout of  $[U]$  and the punched output. (The minus sign must be in Column 29 and the 1 (one) in Column 32.)  
 NCON: This indicator provides for changing five program test numbers used in the matrix iteration subroutine; NCON = 0 if no changes are desired and NCON  $\neq 0$  if any of the tests is to be changed.

### 3. K card (FORMAT 6E12.8)

Col	1-2	
Name	K	
Field	(1)	

Field 1 contains K, the flexibility matrix normalizing constant; if the [a] matrix has not been normalized, enter K = 1.0. The flexibility matrix calculated by the program FLUENC has not been normalized.

4. Data card for changes in matrix iteration tests (FORMAT 3E12.8 and 2I4). Omit this card when NCON = 0. There are three test numbers and two control numbers that define the convergence criteria for the flutter eigenvalue solution. A suggested set of numbers are built into the program; these, however, may be changed by the program user. To alter any number, all five numbers must be reentered.

Col	1-12	13-24	25-36	37-40	41-44	
Name	EPSP	EPDP	AITKEN	NITRSP	NITRDP	
Field	(1)	(2)	(3)	(4)	(5)	

EPSP =  $0.5 \times 10^{-6}$  or input number; test for eigenvector convergence when the iteration procedure is approaching a single root.  
 EPDP =  $0.5 \times 10^{-7}$  or input number; test for convergence when the iteration procedure is approaching a pair of close roots.

AITKEN = 0.9 or input number; if this test is met, the program uses a procedure (known as Aitken's  $\delta^2$  method) to accelerate convergence.

NITRSP = 40; a maximum of 40 single precision arithmetic iterations will be performed for each eigenvalue if its eigenvectors have not converged in a lesser number.

ITRDP = 100; if the eigenvectors for any one eigenvalue have not converged in NITRSP single precision iterations, the program will then use up to a maximum of 100 double arithmetic iterations.

5. Control card(s) for external stores and weighting matrices (FORMAT 18I4); omit this data when NAERO = 0.

Col	1-4	5-8	9-12	13-16	
Name	ISXT <sub>1</sub>	ISW <sub>1</sub>	ISXT <sub>2</sub>	ISW <sub>2</sub>	
Field	1	2	3	4	

Continue on successive cards to ISW<sub>i</sub> = ISW<sub>NSUR</sub>.

ISXT<sub>i</sub> = Number of control points reserved for the external stores on surface i.

ISW<sub>i</sub> = 0, no weighting matrix is to be input for surface i.  
= 1, weighting matrix is to be input for surface i.

Continue on next card, until i = NSUR.

6. Reference semichord, b<sub>r</sub> and reduced velocity (1/k<sub>r</sub>) series (FORMAT 6E12.8): These reference parameters are used in computing the flutter velocities.

Col	1-12	13-24	25-36	37-48	49-60	61-72
Name	b <sub>r</sub>	(1/k <sub>r</sub> ) <sub>1</sub>	(1/k <sub>r</sub> ) <sub>2</sub>	(1/k <sub>r</sub> ) <sub>3</sub>	(1/k <sub>r</sub> ) <sub>4</sub>	(1/k <sub>r</sub> ) <sub>5</sub>
Field	(1)	(2)	(3)	(4)	(5)	(6)

Continue (1/k<sub>r</sub>)<sub>i</sub>'s on next card(s); i≤20. The b<sub>r</sub>(feet) may be any value; but it is noted that the (1/k<sub>r</sub>)<sub>i</sub> predetermines the (1/k<sub>i</sub>) used when computing the AIC matrices for each surface. The 1/k<sub>i</sub> for surface i is found from the relationship (1/k<sub>i</sub>) = (1/k<sub>r</sub>)(b<sub>r</sub>/b<sub>ri</sub>) where b<sub>ri</sub> is the reference semichord for surface i.

7. A reference semichord (b<sub>ri</sub>) and semispan (s<sub>i</sub>) must be input for the rigid component if NFUS = 1, and for each flexible surface if NAERO>0.

When NFUS = 1 (FORMAT 6E12.8)

Column	1-12	13-24	25-36	37-48	49-60	61-72
Name	$b_{r_0}$	$s_{r_0}$	$b_{r_1}$	$s_{r_1}$	$b_{r_2}$	$s_{r_2}$
Field	(1)	(2)	(3)	(4)	(5)	(6)

Where  $b_{r_0}$  and  $s_{r_0}$  are the reference semichord and semispan for the rigid component. Continue on next card(s) until  $b_{r_i} = b_{r_{NSUR}}$  and  $s_{r_i} = s_{r_{NSUR}}$ .

When NFUS = 0 (FORMAT 6E12.8)

Column	1-12	13-24	25-36	37-48	49-60	61-72
Name	$b_{r_1}$	$s_{r_1}$	$b_{r_2}$	$s_{r_2}$	$b_{r_3}$	$s_{r_3}$
Field	(1)	(2)	(?)	(4)	(5)	(6)

Continue on next card(s) until  $b_{r_i} = b_{r_{NSUR}}$  and  $s_{r_i} = s_{r_{NSUR}}$ .

8. Density series (FORMAT 6E12.5): Omit this input if NDENS=0 in Item 2. If NDENS>0 begin in field 1 of this card and NDENS densities,  $\leq 20$ . Continue on successive card(s).

Column	1-12	13-24	25-36	37-48
Name	$\rho_1$	$\rho_2$	$\rho_3$	$\rho_4$
Field	1	2	3	4

9. Rigid component generalized mass matrix  $[\Delta m]$ . The  $[\Delta m]$  matrix for the rigid component(s) of the system must be compatible with the flexible surfaces product matrix given by  $[h_R]^T [M] [h_R]$ , i.e., each element in  $[\Delta m]$  is based upon the same rigid-body motion generalized coordinate as the respective element in the product matrix. Input by column beginning each column on a new card. Omit this data when NDELM = 0.

Col	1-12	13-24	25-36	
Name	$\Delta m_{1,1}$	$\Delta m_{2,1}$	$\Delta m_{3,1}$	
Field	(1)	(2)	(3)	

			$\Delta m_{(NRIGID-1),1}$	$\Delta m_{NRIGID,1}$
			(NRIGID-1)	(NRIGID)

Continue on successive card(s) until

10. Mass matrix [M]: The mass matrix is partitioned as shown on page A-10, only the nonzero partitions are input; i.e., a separate mass matrix ( $[M_i]$ ) is input for each surface. The sequence for considering the surfaces is the same as that used in Item 5 and 7 if NAERO>0. Repeat the following input for each surface from  $i = 1$  to NSUR.

#### Size Control Cards

Column	1-4	5-8	9-12	
Name	NSIZE <sub>i</sub>			
Field	(1)	(2)	(3)	

NSIZE<sub>i</sub> = the order of  $[M_i]$

Often many of the elements in a mass matrix are zero; the following form has been provided so that most of the zero elements will not need to be entered into the program as data.

#### Control Card(s) for Omitting Zeros (FORMAT 18I4)

Column	1-4	5-8	9-12	13-16	17-20	
Name	LOW <sub>1</sub>	LHIGH <sub>1</sub>	LOW <sub>2</sub>	LHIGH <sub>2</sub>	LOW <sub>3</sub>	LHIGH <sub>i</sub>
Field	(1)	(2)	(3)	(4)	(5)	(2 <sub>i</sub> )

$LOW_i$  = The row number in which the first nonzero element appears in Column i.

$LHIGH_i$  = The row number in which the last nonzero element appears in Column i.

If only one nonzero element appears in Column i (i.e., a diagonal mass matrix) the row number in which it appears must be used for both LOW and LHIGH.

#### Mass Matrix Elements (FORMAT 6E12.8)

Col	1-12	13-24	25-36			
Name	$\Delta m_1, LOW$	$\Delta m_1, LOW+1$	$\Delta m_1, LOW+2$		$\Delta m_1, LHIGH-1$	$\Delta m_1, LHIGH$
Field	(1)	(2)	(3)			

The elements are entered by column; each column begins on a new card. Any zero elements in rows between LOW and LHIGH must be entered or their respective fields left blank. If external stores are present ( $ISXT > 0$ ) all store control points must be entered before the surface control points; i.e., the elements representing the external stores mass must occupy the upper left-hand corner of the mass matrix.

11. Rigid component inodal matrix,  $[h_{R_o}]$  (see page 7). Omit this input when  $NFUS = 0$ . The number of rows in  $[h_{R_o}]$  must be the same as the number of control points considered when computing the  $[C_{h_c}]$  matrices; the number of columns must agree with NRIGID.

#### Size Control Card(s) (FORMAT 18I4)

Column	1-4	5-8	
Name	NRROWS		
Field	(1)	(2)	

NRROWS = The number of rows in  $[h_{R_o}]$

Matrix [ $h_{R_o}$ ] Elements (FORMAT 6E12.8)

Column	1-12	13-24	25-36	37-48	49-60	61-72
Name	$h_{R_{o1}, 1}$	$h_{R_{o2}, 1}$	$h_{R_{o3}, 1}$	....	....	$h_{R_o \text{NROWS}, 1}$
Field	(1)	(2)	(3)	(4)	(5)	(6)

The elements are entered by column, with each column beginning on a new card.

12. Rigid-body modal matrix, [ $h_R$ ] (see page 7). Omit this input if NRIGID = 0. [ $h_R$ ] is to be input by partitions  $[h_R]_i$ , each partition is of order (NSIZE x NRIGID) for each surface. The following data is to be repeated for  $i = 1, \text{NSUR}$ .

Size Control Card (FORMAT 18I4)

Column	1-4	5-8	
Name	NSIZE		
Field	(1)	(2)	

NSIZE = Number of control points on each surface

Matrix [ $h_{R_i}$ ] Elements (FORMAT 6E12.8)

Column	1-12	13-24	25-36	37-48	49-60	61-72
Name	$h_{R_1, 1}$	$h_{R_2, 1}$	$h_{R_3, 1}$	....	....	$h_{R_{\text{NSIZE}}, 1}$
Field	(1)	(2)	(3)	(4)	(5)	(6)

The elements are entered by column, with each column beginning on a new card.

13. Flexibility matrices, [a] (see page 6). The flexibility matrix is partitioned, only the nonzero partitions  $[a]_i$ , corresponding to the

flexible surfaces are entered. The matrix may be formed by any of the well-known procedures using elementary beam theory, force or displacement methods. The program FLUENC will generate this matrix using the displacement method. The punched output from FLUENC may be used as direct input into this program. The following data is repeated for  $i = 1, NSUR$ .

Control Card (FORMAT 18I4):

Column	1-4	5-8	9-12	13-16	
Name	$m_i$	(BLANK)	IFORM	IROW	
Field	(1)	(2)	(3)	(4)	

$m_i$  = The number of rows in  $[a]_i$

IFORM = 0 if the elements are to be input using column binary format.

= 1 if the elements are to be input using FORTRAN (FORMAT 6E12.8) or FLUENC output is to be used directly.

IROW = 0 if the matrix elements are to be entered by column.

= 1 if the matrix elements are to be entered by row.

Matrix  $[a]_i$  elements (use format specified above):

For IFORM = 1 and IROW = 1 (FORMAT 6E12.8)

Column	1-12	13-24	25-36	37-48	
Name	$a_{1,1}$	$a_{1,2}$	$a_{1,3}$	$a_{1,4}$	
Field	(1)	(2)	(3)	(4)	

Each row starts on a new card.

For IFORM = 1 and IROW = 0 (FORMAT 6E12.8)

Column	1-12	13-24	25-36	37-48	
Name	$a_{1,1}$	$a_{2,1}$	$a_{3,1}$	$a_{4,1}$	
Field	(1)	(2)	(3)	(4)	

Each column starts on a new card.

If IFORM = 0, then IROW must = 0: The matrix elements are input using column binary format; Column 1 starts in Origin 1. Column 2 starts in location  $(1 + m_1)$ ; Column 3 starts in location  $(1 + 2m_1)$ ; etc. A TRA\* card must end each  $[a_i]$  deck. (The column binary format should be used only if the data are available as punched-card output from appropriate computer programs.) The only advantage of the C-B format is the minimum card storage space required.

14. Weighting matrix,  $[W]$  (see page 6). The weighting matrix is partitioned, only the nonzero partitions  $[W_i]$  corresponding to the flexible surface are entered. No provisions have been made for entering a  $[W_i]$  matrix for the rigid component; any adjustment to  $[C_{ho}]$  must be made before it is input as data. If  $(ISW)_i = 0$  omit this data. Repeat the following data for  $i = 1, NSUR$ .

For  $(ISW)_i = 0$  and  $(ISXT)_i > 0$

Control card for external stores elements (FORMAT 1814)

Column	1-4	5-8	9-12	13-16	
Name	$NXST_i$	(BLANK)	NFORM	NROW	
Field	(1)	(2)	(3)	(4)	

\*The TRA card has a 7 and 9 punch in Column 1, Column 2 through 72 are blank and Column 73 through 80 will contain the characters used for identification and sequencing in the punched card output deck.

$NXST_i = 0$  if no  $[W]_i$  matrix is input for the external stores area (the program will use a unit matrix, I)  
 $= n$  the number of control points reserved for stores.  
 $NFORM = 1$  if the  $[W]_i$  matrix elements will be input using FORTRAN (FORMAT 6E12.8)  
 $- 0$  if the elements are to be input using column binary format  
 $NROW = 0$  if the  $[W]_i$  matrix elements are to be input by column  
 $= 1$  if the matrix elements are to be input by row

External stores elements  $[W]_i$ . Format given on control card above.

For NFORM = 1 NROW = 1

Column	1-12	13-24	25-36	37-48	
Name	$W_{1,1}$	$W_{1,2}$	$W_{1,3}$	$W_{1,4}$	
Field	(1)	(2)	(3)	(4)	

Each row starts on a new card.

For NFORM = 1 NROW = 0

Column	1-12	13-24	25-36	37-48	
Name	$W_{1,1}$	$W_{2,1}$	$W_{3,1}$	$W_{4,1}$	
Field	(1)	(2)	(3)	(4)	

Each column starts on a new card.

If  $NFORM = 0$ , then must  $NROW = 0$ : The matrix elements are input using column binary format; Column 1 starts in Origin 1. Column 2 starts in location  $(1 + IXST_1)$ ; Column 3 starts in location  $(1 + 2IXST_1)$ ; etc. A TRA card must end each  $[a_i]$  deck. The column binary format should be used only if the data are available as punched-card output from appropriate computer programs. The only advantage of C-B format is the minimum card storage space required.

Control card for flexible surface weighting matrix  $[W_i]$

(FORMAT 18I4) The  $[W_i]$  matrix is often sparse, sometimes diagonal and may be of large order,  $\leq 49$ ; for this reason we provide for partitioning of the matrix and entering only the nonzero partitions.

Column	1-4	5-8	9-12	13-16
Name	NSIZE <sub>i</sub>	NPART	NFORM	NROW
Field	(1)	(2)	(3)	(4)

NSIZE = The number of control points used on surface i.

Do not include control points for external stores.

NPART = The number of partitions in the  $[W_i]$  surface matrix

NFORM = 1 if the  $[W_i]$  will be input using FORTRAN (FORMAT 6E12.8)

= 0 if the elements are to be input using column binary format

NROW = 0 if the  $[W_i]$  matrix elements are to be input by column

= 1 if the matrix elements are to be input by row

Repeat the following two data item for each partition  $j = 1, \text{NPART}$ .

Control card for partition  $[W_{ij}]$ , FORMAT (18I4)

Column	1-4	5-8	9-12	13-16	17-21	
Name	$N_j$					
Field	(1)	(2)	(3)	(4)	(5)	

$N_j$  = The order of partition  $j$  of  $[W_i]$

Elements in partition  $[W_{ij}]$ . Format given on the control card for flexible surface weighting matrix.

NFORM = 1      NROW = 1

Column	1-12	13-24	25-36	37-48	
Name	$W_{1,1}$	$W_{1,2}$	$W_{1,3}$	$W_{1,4}$	
Field	(1)	(2)	(3)	(4)	

Each row starts on a new card.

NFORM = 1      NROW = 0

Column	1-12	13-24	25-36	37-48	
Name	$W_{1,2}$	$W_{2,1}$	$W_{3,1}$	$W_{4,1}$	
Field	(1)	(2)	(3)	(4)	

Each column starts on a new card.

If NFORM = 0, then must NROW = 0: The matrix elements are input using column binary format; Column 1 starts in Origin 1. Column 2 starts in location  $(1 + IXST_1)$ ; Column 3 starts in location  $(1 + 2IXST_1)$  etc. A TRA card must end each  $[a_i]$  deck. The column binary format should be used only if the data are available as punched-card output from appropriate computer programs. The only advantage of C-B format is the minimum card storage space required.

For  $(ISW)_i = 0$  and  $(ISXT)_i = 0$

Control card for flexible surface weighting matrix  $[W_i]$  (FORMAT 18I4). The  $[W_i]$  matrix is often sparse, sometimes diagonal and may be of large order,  $\approx 49$ ; for this reason we provide for partitioning of the matrix and entering only the nonzero partitions. Repeat the following data for  $i = 1, NSUR$ .

Column	1-4	5-8	9-12	13-16	17-20	
Name	NSIZE	NPART	NFORM	NROW		
Field	(1)	(2)	(3)	(4)	(5)	

NSIZE = The number of control points used on surface  $i$

NPART = The number of partitions in the  $[W_i]$ , surface matrix

NFORM = 1 if the  $[W_i]$  will be input using FORTRAN (FORMAT 6E12.8)

= 0 if the elements are to be input using column binary format

NROW = 0 if the elements are to be input by column

= 1 if the elements are to be input by row

Repeat the following two data items for each partition  $j = 1, NPART$ .

Control card for partition  $[W_i]_j$  FORMAT (18I4)

Column	1-4	5-8	9-12	13-16	
Name	$N_j$				
Field	(1)	(2)	(3)	(4)	
	↓	↓	↓	↓	↓

$N_j$  = The order of partition  $j$  of  $[W_i]$

Elements in partition  $[W_i]_j$  format given on the control card for flexible surface weighting matrix.

NFORM = 1      NROW = 1

Column	1-12	13-24	25-36	37-48	
Name	$W_{1,1}$	$W_{1,2}$	$W_{1,3}$	$W_{1,4}$	
Field	(1)	(2)	(3)	(4)	
	↓	↓	↓	↓	↓

Each row starts on a new card.

NFORM = 1      NROW = 0

Column	1-12	13-24	25-36	37-48	
Name	$W_{1,1}$	$W_{2,1}$	$W_{3,1}$	$W_{4,1}$	
Field	(1)	(2)	(3)	(4)	
	↓	↓	↓	↓	↓

Each column starts on a new card.

If NFORM = 0, then must NROW = 0: The matrix elements are input using column binary format; Column 1 starts in Origin 1. Column 2 starts in location  $(1 + m_i)$ ; Column 3 starts in location  $(1 + 2m_i)$ ; etc. A TRA card must end each  $[a_i]$  deck. The column binary format should

used only if the data are available as punched-card output from appropriate computer programs. The only advantage of C-B format is the minimum card storage space required.

15. Aerodynamic data: The aerodynamic input consists of NAERO sets of AIC's. Each set of AIC's consists of the AIC's for each surface which have the same reference  $1/k_r$  (see Item 6). If NDENS = 0 a density series will precede each set of AIC's. Input the density series (if Item 8 was omitted) and the AIC matrices for each surface with the following input order. Repeat the order for each  $(1/k_r)_j$ ,  $j = 1, NAERO$ .

Control card for density series (FORMAT 18I4). Omit this input if NDENS>0.

Column	1-4	5-8	9-12	13-16	
Name	NRHO				
Field	(1)	(2)	(3)	(4)	
	↓	↓	↓	↓	↓

NRHO = The number of densities to be entered for  
 $(1/k_r)_j \leq 20$

#### Density Series (FORMAT 6E12.8)

Column	1-12	13-24	25-36	37-48	
Name	$\rho_1$	$\rho_2$	$\rho_3$	$\rho_4$	
Field	(1)	(2)	(3)	(4)	
	↓	↓	↓	↓	↓

Rigid component AIC matrix  $[C_{ho}]_j$ . Omit this input if NFUS = 0. The  $[C_{ho}]_j$  matrix may be sparse; thus, provision has been made to partition the matrix and enter only the nonzero partitions.

Reference 1/k for  $[C_{ho}]_j$  (FORMAT 6E12.8)

Column	1-12	13-24	25-36	37-48	
Name	1/k				
Field	(1)	(2)	(3)	(4)	

1/k = The reduced velocity used in computing the rigid component  $[C_{ho}]_j$ . The AIC's in  $[C_{ho}]$  must be computed for a 1/k which properly relates them to the  $j^{\text{th}}$  1/k.

Control card for  $[C_{ho}]_j$  matrix (FORMAT 18I4)

Column	1-4	5-8	9-12	13-16	
Name	NSIZE	NPART	NFORM	NROW	
Field	(1)	(2)	(3)	(4)	

NSIZE = Number of control points on the rigid component

NPART = Number of nonzero partitions in  $[C_{ho}]_j$   
= 1 for an unpartitioned matrix

NFORM = 1 if the  $[C_{ho}]_j$  matrix is to be input using FORTRAN  
(FORMAT 6E12.8)

= 0 if the  $[C_{ho}]_j$  matrix is to be input using column  
binary format

NROW = 1 if the  $[C_{ho}]_j$  matrix is to be input by row

= 0 if the  $[C_{ho}]_j$  matrix is to be input by column

Repeat the following data for each partition, K = 1, NPART.

**Partition Size Card (FORMAT 18I4)**

Column	1-4	5-8	9-12	13-16	
Name	N				
Field	(1)	(2)	(3)	(4)	

N = The order of partition k

Elements in partition K of  $[C_{h_0}]_j$ . Format is given on the control card for  $[C_{h_0}]_j$  matrix. All the elements in the AIC matrices are complex numbers, but the complexity is considered in the program. Thus, each partition may be input as though it is a real matrix of size N x 2N. The real elements form the odd number columns; and the imaginary elements in the even numbered columns.

For NFORM = 1      NROW = 1

Column	1-12	13-24	25-36	37-48	
Name	$a(\text{Re})_{1,1}$	$a(\text{I})_{1,1}$	$a(\text{Re})_{1,2}$	$a(\text{I})_{1,2}$	
Field	(1)	(2)	(3)	(4)	
	↓	↓	↓	↓	

Each row starts on a new card.

For NFORM = 1 and NROW = 0

Column	1-12	13-24	25-36	37-48	49-60	
Name	$a(\text{Re})_{1,1}$	$a(\text{I})_{1,1}$	$a(\text{Re})_{2,1}$	$a(\text{I})_{2,1}$		
Field	(1)	(2)	(3)	(4)	(5)	
	↓	↓	↓	↓	↓	

Each column starts on a new card.

For NFORM = 0, NROW must = 0. Use column binary format. Column 1 starts in card Origin 1, Column 2 in location (1 + 2N), Column 3 in location (1 + 4N), etc. A TRA card must end each deck. The column binary format should be used only if the data are available as punched-card output from appropriate computer programs. The only advantage of C-B format is the minimum card storage space required.

Flexible component AIC matrix  $[C_h]_{ij}$ . The AIC matrices are often sparse; thus, a provision is made partitioning the matrix and entering only the nonzero partitions. The following data is repeated for  $i = 1, NSUR$ .

For  $ISXT_i > 0$ .

Control card for external stores partition of the surface i  
AIC matrix  $[C_h]_{ij}$  (FORMAT 18I4)

Column	1-4	5-8	9-12	13-16	
Name	NXST	(BLANK)	NFORM	NROW	
Field	(1)	(2)	(3)	(4)	

$NXST_i$  = Number of control points reserved for external stores

NFORM = 1 if the matrix elements are to be input using

FORTRAN (FORMAT 6E12.8)

= 0 if the matrix elements are to be entered using  
column binary format

NROW = 1 if the matrix elements are to be entered by row

= 0 if the matrix elements are to be entered by column

Elements for external stores partition of AIC matrix  $[C_h]_{ij}$

For NFORM = 1 and NROW = 1

Column	1-12	13-24	25-36	37-48	
Name	$a(Re)_{1,1}$	$a(I)_{1,1}$	$a(Re)_{1,2}$	$a(I)_{1,2}$	
Field	(1)	(2)	(3)	(4)	

Each row begins on a new card.

For NFORM = 1 and NROW = 0

Column	1-12	13-24	25-36	37-48	
Name	a(Re)i, 1	a(I)1, 1	a(Re)2, 1	a(Re)2, 1	
Field	(1)	(2)	(3)	(4)	

If NFORM = 0 then NROW must = 0 use column binary format.

Column 1 starts in card origin 1, Column 2 in Location (1+2NXT<sub>i</sub>), Column 3 in Location (1+4NXST<sub>i</sub>), etc. A TRA Card must end each deck. The column binary format should be used only if the data are available as punched-card output from appropriate computer programs. The only advantage of C-B format is the minimum card storage space requirements.

Reference 1/k<sub>i</sub> card for control point AIC matrix  $[C_h]_{ij}$

#### FORMAT (6E12.8)

Column	1-12	13-24	25-36	
Name	1/k			
Field	(1)	(2)	(3)	

1/k<sub>i</sub> = The reduced velocity used in computing the flexible component  $[C_h]_{ij}$ . The AIC's must be computed for a 1/k<sub>i</sub> which properly relates them to the jth 1/k<sub>r</sub>.

Control card for control point AIC matrix  $[C_h]_{ij}$  (FORMAT (18I4)

Column	1-4	5-8	9-12	13-16	
Name	NSIZE	NPART	NFORM	NROW	
Field	(1)	(2)	(3)	(4)	

NSIZE = Order of control point AIC matrix  $[C_h]_{ij}$

NPART = Number of partitions in  $[C_h]_{ij}$

NFORM = 1 matrix elements are to be input using FORTRAN  
(FORMAT 6E12.3)

= 0 matrix elements are to be input using column binary  
format

NROW = 1 elements input by row.

= 0 elements input by column.

Repeat the following data for j = 2, NPART. j = 1 corresponds to the  
external stores partition

Control card for partition size of partition j FORMAT (18J4)

Column	1-4	5-8	9-12	
Name	N			
Field	(1)	(2)	(3)	

N = Order of partition j

Elements of control point AIC matrix  $[C_H]_{i,j}$  partition j

For NFORM = 1 and NROW = 1 (FORMAT 6E12.8)

Column	1-12	13-24	25-36	37-48	
Name	a(RE)1, 1	a(I)1, 1	a(Re)1, 2	a(I)1, 2	
Field	(1)	(2)	(3)	(4)	

Each row starts on a new card

For NFORM = 1 and NROW = 0 (FORMAT 6E12.8)

Column	1-12	13-24	25-36	37-48	
Name	a(Re)1, 1	a(I)1, 1	a(Re)2, 1	a(I)2, 1	
Field	(1)	(2)	(3)	(4)	

Each column starts on a new card

For NFORM = 0 then NROW must = 0 use column binary format.

Column 1 starts in card origin 1, Column 2 in Location (1 + 2N),  
 Column 3 in Location (1 + 4N), etc. A TRA card must end each deck.  
 The column binary format should be used only if the data are available  
 as punched card output from appropriate computer programs. The only  
 advantage of C-B format is the minimum card storage space  
 requirements

For ISXT<sub>i</sub> = 0

Reference 1/k<sub>i</sub> card for control point AIC matrix  $[C_h]_{ij}$

FORMAT (6E12.8)

Column	1-12	13-24	25-36	
Name	1/k <sub>i</sub>			
Field	(1)	(2)	(3)	

1/k<sub>i</sub> = The reduced velocity used in computing the flexible component  $[C_h]_{ij}$ . The AIC's must be computed for a 1/k<sub>i</sub> which properly relates them to the jth 1/k<sub>r</sub>.

Control card for control point AIC matrix  $[C_h]_{ij}$  FORMAT (18I4)

Column	1-4	5-8	9-12	13-16	
Name	NSIZE	NPART	NFORM	NROW	
Field	(1)	(2)	(3)	(4)	

NSIZE = Order of control point AIC matrix  $[C_h]_{ij}$

NPART = Number of partitions in  $[C_h]_{ij}$

NFORM = 1 matrix elements are to be input using FORTRAN (FORMAT 6E12.8)

= 0 matrix elements are to be input using column binary format.

NROW = 1 elements input by row

= 0 elements input by column

Repeat the following data for  $j = 1, \text{NPART}$ .

Control card for partition size of partition  $j$  FORMAT (18I4)

Column	1-4	5-8	9-12	
Name	N			
Field	(1)	(2)	(3)	

N = Order of partition

Elements of control point AIC matrix  $[C_h]_{i,j}$  partition  $j$

For NFORM = 1 and NROW = 1 (FORMAT 6E12.8)

Column	1-12	13-24	25-36	37-48	
Name	a(Re)1,1	a(I)1,1	a(Re)1,2	a(I)1,2	
Field	(1)	(2)	(3)	(4)	

Each row starts on a new card

For NFORM = 1 and NROW = 0 (FORMAT 6E12.8)

Column	1-12	13-24	25-36	37-48	
Name	a(Re)1,1	a(I)1,1	a(Re)2,1	a(I)2,1	
Field	(1)	(2)	(3)	(4)	

For NFORM = 0 then NROW must = 0 use column binary format.

Column 1 start in card origin 1, Column 2 in Location  $(1 + 2N)$ ,  
 Column 3 in Location  $(1 + 4N)$ , etc. A TRA card must end each deck.  
 The column binary format should be used only if the data are available  
 as punched card output from appropriate computer programs. The only  
 advantage of C-B format is the minimum card storage requirements.

## SECTION 6

### DESCRIPTION OF PROGRAM OUTPUT

#### A. Printed Output

1. All input data.
2. The dynamic matrix or flutter determinant if NPUNCH = -1 is used in the general control card.
3. For the vibration analysis or for each  $1/k_r$  in a flutter analysis
  - a. The eigenvalue for each output mode followed by the number of single- and double-precision iterations and the number of Aitken accelerations.
  - b. The normalized eigenvectors (modes) followed by the check eigenvalues and eigenvectors.
  - c. The frequencies (omegas) in cycles per second followed (in a flutter analysis) by the structural damping coefficient and the velocity (knots) associated with each frequency.
  - d. If NPUNCH = ±1, the sequencing numbers used for identifying the punched-card output (frequencies and modes); this will conclude the printout for each  $1/k_r$  used in a flutter analysis.
4. In a vibration analysis, the generalized mass corresponding to each output (free vibration) mode will follow the above printed output [ see Eq. (28), Section I ].
5. A number of different statements may be printed which indicate machine or program detected errors in input data (wrong format or incompatibility in the number of rows input for a matrix and the number designated).
6. If the program or the machine fails in the iteration portion of the program, a note will be printed stating the type or cause of failure.

7. If convergence is not obtained in the allowable number of iterations, a note will be printed and the program will continue. (In this case the eigenvalues and eigenvectors should be compared with the check eigenvalues and eigenvectors to determine if the convergence is sufficiently accurate.)
8. The printed output for the example problem is shown on the following pages.

## SECTION 7

### EXAMPLE PROBLEMS

As example problems, we choose a cantilever flutter analysis and a free-free symmetric flutter analysis of the jet transport wing (and rigid fuselage) treated throughout Ref. 5 and shown in Figure A-1. The wing mass, flexibility and aerodynamic matrices and the fuselage aerodynamic matrix (symmetric case) can be seen in the example problem printed output (pages 41-62) and will not be repeated with the list of input data to follow. The flexibility matrix normalizing factor is  $K = 10^{-7}$ . The wing weighting matrix is taken as unity ([I]) and, in this case, requires no input. The symmetrical rigid component (one-half of the fuselage) generalized mass matrix is given below in the pound-inch system

$$[\Delta m] = \begin{bmatrix} M_o & S_o \\ S_o & I_{yo} \end{bmatrix} = \begin{bmatrix} 17,400 & 1,370,250 \\ 1,370,250 & 4,457,907,200 \end{bmatrix}$$

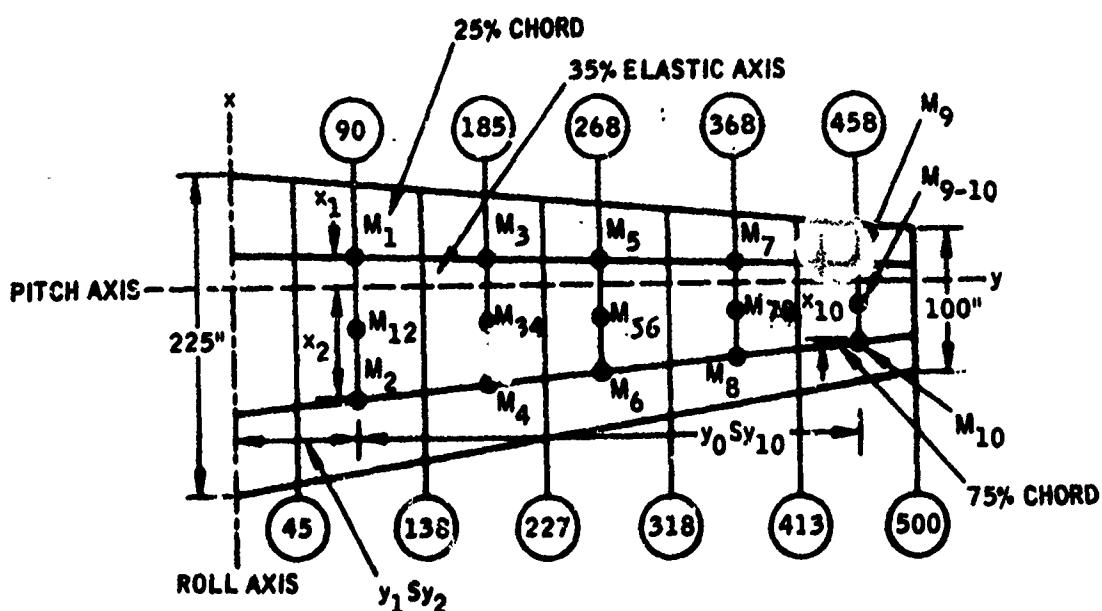


Figure A-1. Jet transport wing geometry.

In the antisymmetric case, the rigid component generalized mass matrix would be  $[\Delta m] = [I_{x_0}]$ , and in the composite longitudinal-lateral case, the generalized mass matrix would be

$$[\Delta m] = \begin{bmatrix} M_o & S_o & 0 \\ S_o & I_{yo} & 0 \\ 0 & 0 & I_{x_0} \end{bmatrix}$$

The symmetrical case requires the two rigid-body degrees of freedom of plunging and pitching. The rigid-body modal matrix, therefore, consists of two columns: a unit column, and a column of the x-coordinate of each control point. The rigid-body modal matrix for the wing is

$$[h_R] = [1 \ x] = \begin{bmatrix} 1 & 20.25 \\ 1 & -81.00 \\ 1 & 17.85 \\ 1 & -71.40 \\ 1 & 15.80 \\ 1 & -63.20 \\ 1 & 13.30 \\ 1 & -53.20 \\ 1 & 11.05 \\ 1 & -44.20 \end{bmatrix}$$

The rigid-body modal matrix for the fuselage is

$$[h_{Ro}] = [1 \ x] = \begin{bmatrix} 1 & -373.30 \\ 1 & -248.30 \\ 1 & -123.30 \\ 1 & +1.70 \\ 1 & +126.70 \end{bmatrix}$$

Note that the above matrix is used in computing the incremental generalized mass which results from the aerodynamic loads on one-half of the fuselage and, therefore, the x-coordinates must be given in the

proper order for the control points used in computing the fuselage AICs.  
[In this problem the fuselage AICs are hypothetical, but the x-coordinates are given in the order necessary for the slender-body theory AICs.]

The reference geometry for the wing is  $b_{rw} = 5.468$  ft and  $s_w = 37.917$  ft. The reference geometry for the fuselage is  $b_{ro} = 5.468$  ft and  $s_o = 18.9585$  ft. [We assume that the wing reference geometry was used to nondimensionalize the fuselage AIC matrix, and, because we require only one-half of the fuselage aerodynamic force, it can be obtained by setting  $s_o = (1/2)s_w$ .] Both example problems are carried out for the single reduced velocity  $1/k_r = 16.67$  with the reference semichord for the system  $b_r = 5.468$  ft and with sea-level density  $\rho = 0.002378$  slugs/ $ft^3$ .

The output modes, the flutter frequencies and velocities, and the required structural damping can be seen in the example problem printed output (pages A-55 through A-65).

The input keypunch sheets are given, followed by the computer output.

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PAGE \_\_\_\_\_ OF \_\_\_\_\_

NAME	PHONE	DATE	LOG NO.	PROB. NO.	PROG. NO.	IDENTIFICATION
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 30 .. 12 43 .. 15 16 17 18 19 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 .. 13 14 15 16 17 18 19 50						
1 JET TRANSPORT EXAMPLE PROBLEM - CANTILEVER CASE						HM1000000
2 General Control Card						
3						
4 1 1 0 0 1 4 0						HM1000001
5 Flexibility Matrix Normalizing Constant, K FORMAT 6(2,0)						
6 1.0 -07						HM1000002
7 0 0 0 0 0 0 0 0						
8 Reference and Reference 1 or 0 (FORMAT (DI,0))						HM1000003
9 0 0 0 0 0 0 0 0						
10 5.468 16.67						HM1000004
11 5.468 16.67						HM1000005
12 5.468 37.917						HM1000006
13 Density Series (FORMAT (DI,0))						
14 0.002378						
15						
16 10						
17 New Location of First and Last (LOW, HIGH) Number Element in Last Column of [M]						
18 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 .. 15 36 37 38 39 40 .. 33 44 45 46 .. 48 49 50 51 52 53 .. 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79						
19						
20						
21						
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NAME	PHONE	DATE	LOG NO.	PROB. NO.	PG. NO.	IDENTIFICATION
	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80					
1						
2	1 6 6 7			Refrence	1 / 100	C4
3				Matrix	FORMAT	6E12.8
4	1 0	5	1	Control Card for [C4] Matrix Input	FORMAT	10.4
5						
6	2					
7	3 0 0 3 9 7	4 0 3 - 6 0 0 9 2 6 7 3 + 0 2 - 3 0 5 7 9 6 1 5 + 0 3 - 3 2 2 7 8 2 0 9 + 0 2				
8	1 9 1 1 1 8 1 6 + 0 0	1 6 5 1 4 1 1 9 + 0 2	5 7 7 3 3 5 4 4 8 + 0 0 - 1 6 5 1 4 1 1 9 + 0 2			
9	2					
10	1 2 9 3 4 9 9 0 + 0 3 - 5 1 5 2 7 5 + 0 2 - 2 9 7 2 8 2 4 1 + 0 3 + 3 1 2 4 6 9 4 2 + 0 2					
11	1 4 2 1 1 3 5 3 + 0 0 + 1 3 9 3 0 7 8 8 1 - 0 2 + 4 2 6 3 4 0 5 8 + 0 0 - 1 3 9 3 0 7 8 8 + 0 2					
12	2					
13	1 3 0 4 8 3 9 9 6 + 0 3 - 5 3 0 6 6 0 6 1 + 0 2 - 3 0 8 2 7 5 9 4 + 0 3 + 3 1 8 7 1 3 5 4 + 0 2					
14	1 1 1 3 8 4 7 7 5 4 0 6 + 1 2 6 0 7 9 3 1 + 0 2 + 3 4 1 5 4 8 2 9 + 0 0 - 1 2 6 0 7 9 3 1 + 0 2					
15	2					
16	1 3 2 4 8 3 2 5 1 + 0 3 - 6 2 2 7 8 3 2 9 + 0 2 - 3 2 7 6 7 4 6 0 + 0 3 + 3 2 5 4 1 1 6 6 + 0 2					
17	1 8 4 2 1 6 2 3 2 - 0 1 + 1 0 7 9 5 6 2 + 0 2 + 2 5 2 6 4 3 7 0 + 0 0 - 1 1 0 7 9 5 6 2 + 0 2					
18	2					
19						
20						
21						
22						
23						
24						
25	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80					

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PAGE

NAME

PHONE

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1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 50 51 52 53 54 55 56 57 58 59 60

1.3	0.32	1.47	4.4	+0.3	-4.3	8.2	+0.2	-3.0	5.2	+0.3	+2.6	5.1	7.1	1.3	+0.2	1.0	0.5	6
2.5	3.23	6.89	7.0	-0.1	+8.4	3.0	0.2	6.2	+0.1	+1.59	7.1	0.6	8.0	-8.4	3.0	0.2	6.2	+0.1
3.	Other formats that can be used to input the $[C_n]$ matrices are explained																	
4.	In Section II, Part B, Item 15.																	
5.	JET TRANSPORT EXAMFILE PROBLEM - SYMMETRIC CASE																	
6.	1.1	2.	1	1	4	1	0											
7.	K																	
8.	1.1	5.67	1.58															
9.	10.	11.	12.	13.	14.	15.	16.	17.	18.	19.	20.	21.	22.	23.	24.	25.	26.	27.
10.	11.	12.	13.	14.	15.	16.	17.	18.	19.	20.	21.	22.	23.	24.	25.	26.	27.	28.
11.	12.	13.	14.	15.	16.	17.	18.	19.	20.	21.	22.	23.	24.	25.	26.	27.	28.	29.
12.	13.	14.	15.	16.	17.	18.	19.	20.	21.	22.	23.	24.	25.	26.	27.	28.	29.	30.
13.	14.	15.	16.	17.	18.	19.	20.	21.	22.	23.	24.	25.	26.	27.	28.	29.	30.	31.
14.	15.	16.	17.	18.	19.	20.	21.	22.	23.	24.	25.	26.	27.	28.	29.	30.	31.	32.
15.	16.	17.	18.	19.	20.	21.	22.	23.	24.	25.	26.	27.	28.	29.	30.	31.	32.	33.
16.	17.	18.	19.	20.	21.	22.	23.	24.	25.	26.	27.	28.	29.	30.	31.	32.	33.	34.
17.	18.	19.	20.	21.	22.	23.	24.	25.	26.	27.	28.	29.	30.	31.	32.	33.	34.	35.
18.	19.	20.	21.	22.	23.	24.	25.	26.	27.	28.	29.	30.	31.	32.	33.	34.	35.	36.
19.	20.	21.	22.	23.	24.	25.	26.	27.	28.	29.	30.	31.	32.	33.	34.	35.	36.	37.
20.	21.	22.	23.	24.	25.	26.	27.	28.	29.	30.	31.	32.	33.	34.	35.	36.	37.	38.
21.	22.	23.	24.	25.	26.	27.	28.	29.	30.	31.	32.	33.	34.	35.	36.	37.	38.	39.
22.	23.	24.	25.	26.	27.	28.	29.	30.	31.	32.	33.	34.	35.	36.	37.	38.	39.	40.
23.	24.	25.	26.	27.	28.	29.	30.	31.	32.	33.	34.	35.	36.	37.	38.	39.	40.	41.
24.	25.	26.	27.	28.	29.	30.	31.	32.	33.	34.	35.	36.	37.	38.	39.	40.	41.	42.
25.	26.	27.	28.	29.	30.	31.	32.	33.	34.	35.	36.	37.	38.	39.	40.	41.	42.	43.

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1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100

Central Card for [Ch.] Matrix Input (FORMAT 1314)

[Ch.] Matrix Elements (Column Binary Format)

5 The above control card indicates a 5 x 5 (unpartitioned) matrix to be input using column binary format. The matrix can be seen in the Friend output and will not be tabulated.

7 (Color) Input format may be explained in Section II, Part B, Item 15.)

8 1/4 for Surface [Ch.] Matrix

9 16.67 Central Card for Surface (Ch.) Matrix Input

10 10 5 1 1 HM 2000.64

11 10 5 1 1 HM 2000.65

12 13 [Ch.] Matrix by Partitions

13 The partitions are intended to those used in the compiler code.

14

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JFT TRANSPORT EXAMPLE PROBLEM - CANTILEVER CASE  
FLUTTER ANALYSIS BY A COLLOCATION METHOD USING AERODYNAMIC INFLUENCE COEFFICIENTS

NSUR = 1 NAERO = 1 NRIGID = 0 NFUS = 0 NDENS = 1 MODES OUT = 4 MDELM = 0 NPUNCH = 0  
 $A_{(REF)} = 1.548000E 01 \quad K = 0.1000000E-06$

SURFACE	6	S	EXTERNAL STORES SIZE
1	$0.5458000E 01$	$0.37017000E 02$	9

MASS MATRIX

	COLUMN 1	COLUMN 2	SURFACE 1, COLUMN 3	CONTROL POINTS COLUMN 4	COLUMN 5	COLUMN 6
1	$0.5383500E 04$	$-0.146000E 03$	0.	0.	0.	0.
2	$-0.1345000E 03$	$0.9252000E 03$	0.	0.	0.	0.
3	0.	0.	$0.20712000E 05$	$-0.11005000E 05$	0.	0.
4	0.	0.	$-0.10005000E 05$	$0.11476000E 05$	0.	0.
5	0.	0.	0.	0.	$0.31139000E 04$	$0.13976000E 03$
6	0.	0.	0.	0.	$0.15978000E 05$	$0.89669000E 03$
7	0.	0.	0.	0.	0.	0.
8	0.	0.	0.	0.	0.	0.
9	0.	0.	0.	0.	0.	0.
10	0.	0.	0.	0.	0.	0.
11	0.	0.	0.	0.	0.	0.
12	0.	0.	0.	0.	0.	0.
13	0.	0.	0.	0.	0.	0.
14	0.	0.	0.	0.	0.	0.
15	0.	0.	0.	0.	0.	0.
16	0.	0.	0.	0.	0.	0.
17	0.	0.	0.	0.	0.	0.
18	0.	0.	0.	0.	0.	0.
19	0.	0.	0.	0.	0.	0.
20	0.	0.	0.	0.	0.	0.
21	0.	0.	0.	0.	0.	0.
22	0.	0.	0.	0.	0.	0.
23	0.	0.	0.	0.	0.	0.
24	0.	0.	0.	0.	0.	0.
25	0.	0.	0.	0.	0.	0.
26	0.	0.	0.	0.	0.	0.
27	$0.26368000E 04$	$-0.21000000E 02$	0.	0.	0.	0.
28	$-0.21000000E 02$	$0.80330000E 03$	0.	0.	0.	0.
29	0.	0.	$0.46720000E 04$	$0.73900000E 01$	$0.17700000E 03$	0.
30	0.	0.	$0.73900000E 01$	$0.17700000E 03$	0.	0.

## SURFACE FLEXIBILITY MATRIX IN CONTROL POINTS COLUMN 3 COLUMN 1

SURFACE - WEIGHTING MATRIX

AERODYNAMIC MATRIX, 1<sup>st</sup> CONTROL POINTS

0.160/000E-02

COLUMN 1	COLUMN 2	COLUMN 3	COLUMN 4	COLUMN 5	COLUMN 6
1	0.16097700E 03	-0.6000026736 E 02	-0.505790615E 03	0.32278769E 02	0.
2	0.1911816E 02	-0.165250139E 02	0.573355498E 00	-0.16214119E 02	0.
3	0.	0.	0.	0.	0.
4	0.	0.	0.	0.	0.
5	0.	0.	0.	0.	0.
6	0.	0.	0.	0.	0.
7	0.	0.	0.	0.	0.
8	0.	0.	0.	0.	0.
9	0.	0.	0.	0.	0.
10	0.	0.	0.	0.	0.

COLUMN 7	COLUMN 8	COLUMN 9	COLUMN 10	COLUMN 11	COLUMN 12
1	0.	0.	0.	0.	0.
2	0.	0.	0.	0.	0.
3	-0.29723243E 03	0.312400442E 02	0.	0.	0.
4	0.4/6.34956E 00	-0.1391768E 02	0.18481998E 03	-0.538688661E 02	-0.38827594E 03
5	0.	0.	0.	0.	0.
6	0.	0.	0.	0.	0.
7	0.	0.	0.	0.	0.
8	0.	0.	0.	0.	0.
9	0.	0.	0.	0.	0.
10	0.	0.	0.	0.	0.

COLUMN 13	COLUMN 14	COLUMN 15	COLUMN 16	COLUMN 17	COLUMN 18
1	0.	0.	0.	0.	0.
2	0.	0.	0.	0.	0.
3	0.	0.	0.	0.	0.
4	0.	0.	0.	0.	0.
5	0.	0.	0.	0.	0.
6	0.1463147E 03	-0.52727129E 02	-0.12767 .E 03	0.	0.
7	0.6091471E 00	0.11074562E 02	0.2920470E 00	-0.1197502E 02	0.
8	0.	0.	0.	0.	0.
9	0.	0.	0.	0.	0.
10	0.	0.	0.	0.	0.

COLUMN 19	COLUMN 20	COLUMN 21	COLUMN 22	COLUMN 23	COLUMN 24
1	0.	0.	0.	0.	0.
2	0.	0.	0.	0.	0.
3	0.	0.	0.	0.	0.
4	0.	0.	0.	0.	0.
5	0.	0.	0.	0.	0.
6	0.	0.	0.	0.	0.
7	0.	0.	0.	0.	0.
8	0.	0.	0.	0.	0.
9	0.	0.	0.	0.	0.
10	0.	0.	0.	0.	0.

## OUTPUT DATA

## FLUTTER ANALYSIS BY A COLLOCATION METHOD, USING AERODYNAMIC INFLUENCE COEFFICIENTS

DENSITY = 1.2576919E+02

REFINED VELOCITY = 1.16674888E+02

## RIGID BODY DEGREES OF FREEDOM

MODE	FIGEN VALUE	ITERATIONS	S.P.	B.P.	ATKENS S.P.	D.P.
1	-1.28514224E-01	-2.02107439E-01	-	18	0	2
2	-1.171515A21E-01	-0.205/1745E-01	-	18	0	4
3	0.63205150E-01	0.116046E-01	-	16	3	4
4	0.2443861E-01	-6.126226481 E-01	28	0	4	3

## EIGENVECTORS

54

COLUMN 1	COLUMN 2	COLUMN 3	COLUMN 4	COLUMN 5	COLUMN 6
1	0.41765564E-01	0.10911714E-02	0.67422154E-01	0.27973628E-01	0.11268764E-01
2	0.33611182E-01	0.67521205E-02	0.68320588E-01	0.27121336E-01	0.92614527E-01
3	0.14670167E-01	0.81290164E-02	0.59252595E-01	0.26014691E-01	0.66273386E-01
4	0.12642116E-01	0.13248658E-01	0.17748778E-01	0.14824848E-02	0.24426274E-01
5	0.36193184E-01	0.17490041E-01	0.42532389E-01	0.856469743E-01	0.5877918E-01
6	0.34535127E-01	0.25592044E-01	0.44930061E-01	0.33866263E-01	0.59176231E-01
7	0.67711687E-01	0.14773918E-01	0.74531981E-01	0.6820339E-01	0.82465572E-01
8	0.65998268E-01	0.260276921E-01	0.74531981E-01	0.29932516E-01	0.86621867E-01
9	0.18000001E-01	0.57693566E-01	0.665644549E-01	0.27935114E-01	0.93070000E-01
10	0.28173523E-01	0.147391217E-01	0.10000000E-01	0.71209527E-10	0.19000000E-01

COLUMN 7

COLUMN 8

COLUMN 9

COLUMN 10

COLUMN 11

COLUMN 12

COLUMN 13

COLUMN 14

COLUMN 15

COLUMN 16

COLUMN 17

COLUMN 18

COLUMN 19

COLUMN 20

COLUMN 21

COLUMN 22

COLUMN 23

COLUMN 24

COLUMN 25

COLUMN 26

COLUMN 27

COLUMN 28

COLUMN 29

COLUMN 30

COLUMN 31

COLUMN 32

COLUMN 33

COLUMN 34

## CHECK EIGENVALUES AND EIGENVECTORS

	COLUMN 1	COLUMN 2	COLUMN 3	COLUMN 4	COLUMN 5	COLUMN 6
	COLUMN 7	COLUMN 8	COLUMN 9	COLUMN 10	COLUMN 11	COLUMN 12
1	0.4765545E-08	-0.2518494E-01	0.12123636E-01	0.2858472E-06	0.63295459E-01	0.11864946E-07
2	0.20439134E-07	-0.1262485E-07				
3	0.107070466E-04	0.81288441E-02	0.17796768E-01	0.13996269E-02	0.24426423E-01	0.9546721E-01
4	0.12642694E-09	0.13286569E-01	0.42532286E-01	0.80469934E-01	0.58779208E-01	0.14039379E-01
5	0.36103978E-00	0.17496535E-01	0.44036884E-01	0.33061094E-01	0.59176783E-01	0.17164619E-09
6	0.34535149E-00	0.25592861E-01	0.71723857E-01	0.68293201E-01	0.82485651E-01	0.8196559E-01
7	0.67711681E-00	0.14759617E-01	0.299431851E-01	0.29943183E-01	0.66821284E-01	0.13224914E-08
8	0.65068186E-00	0.24870910E-01	0.65114331E-01	0.7934334E-01	0.93069882E-01	0.6575559E-01
9	0.19100000E-01	0.10314414E-01	0.14730285E-01	0.16100000E-01	0.19184554E-01	0.4802418E-09
10	0.96177516E-00	0.14730285E-01	0.16100000E-01	0.19184554E-01	0.19000000E-01	0.4802418E-09
11	0.86493178E-01	-0.11842119E-01				
12	-0.10421509E-01	-0.97384776E-01				
13	-0.15971453E-00	-0.112608E-00				
14	-0.18188964E-01	-0.1110679E-01				
15	-0.46007209E-01	-0.11389738E-01				
16	-0.45833511E-01	-0.1157629E-01				
17	-0.18102335E-01	-0.66989843E-01				
18	0.978744610E-01	-0.11321135E-01				
19	0.11880000E-01	0.8115384E-01				
20	0.978823531E-00	-0.11462694E-01				

MODE	FREQ (CPS)	DAMPING	VELOCITY (KNOTS)
1	0.18617534E-11	-0.86317019E-01	0.62794529E-03
2	0.28163590E-01	-0.24510470E-01	0.96163469E-03
3	0.39303258E-01	0.18747073E-01	0.13328069E-04
4	0.69164967E-01	-0.61758942E-01	0.23454407E-04

JFT TRANSPORT EX-EXAMPLE - RÔLE EN - SYMÉTRIC CASE  
FLUTTER ANALYSIS BY A COLLOCATION METHOD USING AERODYNAMIC INFLUENCE COEFFICIENTS

NSTIR = 1 MODES = 2 NUS = 1 MODES OUT = 1 RIGID COMPONENT = 4 MODEW = 1 NPUNCH = 0  
RIGID COMPONENT = 0.546800E 01 S RIGID COMPONENT = 0.16958500E 02

H (REF) = 1.54680000E 01 K = 0.10000300E 06

SURFACE 1 0.54680000E 01 S 0.37917000E 02

SURFACE 2 0.54680000E 01 S 0.37917000E 02

RIGID COMPONENT MASS MATRIX  
COLUMN 1 COLUMN 2 COLUMN 3 COLUMN 4

1	0.174000E 02	0.170000E 07	0.457900E 16
2	0.15202000E 07	0.15202000E 07	0.15202000E 07

MASS MATRIX

SURFACE 1 0 CONTROL POINTS  
COLUMN 1 COLUMN 2 COLUMN 3 COLUMN 4 COLUMN 5 COLUMN 6

1	0.53836000E 04	-0.110000E 03	1.	0.	0.	0.
2	-0.13494300E 03	0.92520000E 03	0.	0.	0.	0.
3	0.	0.	0.26732000E 05	-0.110000E 05	0.	0.
4	0.	0.	-0.110000E 05	0.11478000E 05	0.	0.
5	0.	0.	0.	0.	0.31139000E 04	0.
6	0.	0.	0.	0.	0.13900000E 03	0.60.
7	0.	0.	0.	0.	0.	0.
8	0.	0.	0.	0.	0.	0.
9	0.	0.	0.	0.	0.	0.
10	0.	0.	0.	0.	0.	0.
11	0.	0.	0.	0.	0.	0.
12	0.	0.	0.	0.	0.	0.
13	0.	0.	0.	0.	0.	0.
14	0.	0.	0.	0.	0.	0.
15	0.	0.	0.	0.	0.	0.
16	0.	0.	0.	0.	0.	0.

RIGID COMPONENT MODES,  
COLUMN 1 COLUMN 2 COLUMN 3

1	0.300000E 01	-0.273577E 02	0.5
2	0.100000E 03	-0.483490E 01	0.1
3	0.100000E 03	0.483490E 01	0.1
4	0.100000E 03	-0.483490E 01	0.1
5	0.100000E 03	0.483490E 01	0.1

RIGID COMPONENT MODES,  
> CONTROL POINTS.

RIGID BODY MODAL MATRIX  
SURFACE 1, 10 CONTROL POINTS

COLUMN	1	2, 3, 4, 5, 6, 7, 8, 9, 10
1	0.196000E 01	0.202500E 02
2	0.100000E 01	-0.500000E 02
3	0.100000E 01	0.100000E 02
4	0.100000E 01	-0.714200E 02
5	0.100000E 01	0.100000E 02
6	0.100000E 01	-0.100000E 02
7	0.100000E 01	0.632000E 02
8	0.100000E 01	-0.532000E 02
9	0.100000E 01	0.105000E 02
10	0.100000E 01	-0.442000E 02

FLEXIBILITY MATRIX

COLUMN	1	2	3	4	5	6
1	0.0172600E 02	0.133600E 02	0.127400E 03	0.627400E 03	0.627400E 02	0.1625100E 03
2	0.133600E 02	0.308600E 03	0.627400E 02	0.32297400E 03	0.10492400E 03	0.352900E 03
3	0.12779800E 03	0.627400E 02	0.2773200E 03	0.1572600E 03	0.4825500E 03	0.3762800E 03
4	0.62722000E 02	0.32297400E 03	0.572600E 03	0.63749000E 03	0.362800E 03	0.80136000E 03
5	0.1051100E 03	0.1492700E 03	0.4625500E 03	0.3762800E 03	0.1275800E 04	0.11344500E 04
6	0.11692200E 03	0.53529000E 03	0.3762800E 03	0.80136000E 03	0.11344500E 04	0.16999020E 04
7	0.2047800E 03	0.1563400E 03	0.7326400E 03	0.6433800E 03	0.1935000E 04	0.1816000E 04
8	0.15936000E 03	0.3592100E 03	0.6433800E 03	0.10012100E 04	0.1816000E 04	0.2292600E 04
9	0.2427500E 03	1.202700E 03	0.8837800E 03	0.2528300E 04	0.2429400E 04	0.2429400E 04
10	0.20403000E 03	0.4578500E 03	0.5837800E 03	0.11810600E 04	0.2429400E 04	0.2824900E 04
COLUMN	7	8	9	10	COLUMN	10
1	0.2047800E 03	0.1563400E 03	0.2428500E 03	0.2040300E 03		
2	0.1563400E 03	0.3592100E 03	0.2040300E 03	0.2428500E 03		
3	0.7326400E 03	0.6433800E 03	0.9581000E 03	0.2040300E 03		
4	0.5413400E 03	0.10012100E 04	0.6837800E 03	0.11810600E 04		
5	0.10511000E 04	0.1816000E 04	0.25283000E 04	0.24294000E 04		
6	0.19160000E 04	0.29249000E 04	0.24294000E 04	0.28249000E 04		
7	0.3602400E 04	0.3505200E 04	0.5267500E 04	0.2117100E 04		
8	0.3505200E 04	0.4292100E 04	0.5117100E 04	0.5718700E 04		
9	0.5267500E 04	0.5117100E 04	0.6484000E 04	0.6234000E 04		
10	0.51171000E 04	0.57187000E 04	0.82340000E 04	0.92340000E 04		

SURFACE 1, NO WEIGHTING MATRIX

COLUMN	1	2	3	4	5	6
COLUMN	1	2	3	4	5	6
1	-0.198515E-01	-0.192241E-01	-0.1782672E-01	0.99733821E-01	0.17801996E-01	-0.24681994E-01
2	0.26447044E-01	-0.16270088E-01	-0.189710978E-01	0.67599525E-01	0.25688689E-01	0.32829672E-01
3	0.	0.	0.25808189E-01	0.32329072E-01	-0.89711928E-01	-0.67269222E-01
4	0.	0.	0.	0.	-0.18604608E-01	-0.23997266E-01
5	0.	0.	0.	0.	0.19429638E-01	0.735666824E-01
COLUMN	7	8	9	10	COLUMN	11
COLUMN	7	8	9	10	COLUMN	11
1	0.	0.	0.	0.	0.	0.
2	0.	0.	0.	0.	0.	0.
3	0.20347044E-01	0.30575088ME-01	0.	0.	0.	0.
4	-0.59060403E-01	-0.446609E-01	0.17070520E-01	0.17538263E-01	0.	0.
5	0.45456274E-01	-0.5160124E-01	-0.1932837E-01	0.81208698E-01	0.	0.

AERODYNAMIC MATRIX 1-K R = 0.1667000E 02

COLUMN 1	COLUMN 2	SURFACE 1	COLUMN 3	CONTROL POINTS	COLUMN 4	COLUMN 5	COLUMN 6
1	2	3	4	5	6	7	8
1 0.369761F 03	-0.639267E 02	-6.105/6615E 03	0.32762769E 02	0.	0.	0.	0.
2 0.19214119E 00	0.16214119E 02	0.5/3.65446E 00	-0.16214119E 02	0.	0.	0.	0.
3 0.	0.	0.	0.	0.	0.	0.	0.
4 0.	0.	0.	0.	0.	0.	0.	0.
5 0.	0.	0.	0.	0.	0.	0.	0.
6 0.	0.	0.	0.	0.	0.	0.	0.
7 0.	0.	0.	0.	0.	0.	0.	0.
8 0.	0.	0.	0.	0.	0.	0.	0.
9 0.	0.	0.	0.	0.	0.	0.	0.
10 0.	0.	0.	0.	0.	0.	0.	0.
COLUMN 7	COLUMN 8	COLUMN 9	COLUMN 10	COLUMN 11	COLUMN 12	COLUMN 13	COLUMN 14
1 0.	0.	0.	0.	0.	0.	0.	0.
2 0.	0.	0.	0.	0.	0.	0.	0.
3 -0.2728241E 03	0.3124692E 02	0.	0.	0.	0.	0.	0.
4 0.42434156E 00	-0.1393759E 02	0.	0.	0.	0.	0.	0.
5 0.	0.	0.	0.	0.	0.	0.	0.
6 0.	0.	0.	0.	0.	0.	0.	0.
7 0.	0.	0.	0.	0.	0.	0.	0.
8 0.	0.	0.	0.	0.	0.	0.	0.
9 0.	0.	0.	0.	0.	0.	0.	0.
10 0.	0.	0.	0.	0.	0.	0.	0.
COLUMN 15	COLUMN 16	COLUMN 17	COLUMN 18	COLUMN 19	COLUMN 20	COLUMN 21	COLUMN 22
1 0.	0.	0.	0.	0.	0.	0.	0.
2 0.	0.	0.	0.	0.	0.	0.	0.
3 0.	0.	0.	0.	0.	0.	0.	0.
4 0.	0.	0.	0.	0.	0.	0.	0.
5 0.	0.	0.	0.	0.	0.	0.	0.
6 0.	0.	0.	0.	0.	0.	0.	0.
7 0.32483251E 03	-0.227819E 02	-0.37460E 03	0.32541166E 02	0.	0.	0.	0.
8 0.84216232E 01	0.11979562E 02	0.25201d7E 00	-0.11872562E 02	0.	0.	0.	0.
9 0.	0.	0.	0.	0.	0.	0.	0.
10 0.	0.	0.	0.	0.	0.	0.	0.

## OUTPUT DATA

## FLUTTER ANALYSIS BY A COLLOCATION METHOD, USING AERODYNAMIC INFLUENCE COEFFICIENTS

DENSITY = 0.23780000E-02 REDUCED VELOCITY = 0.16670000E-02

## RIGID BODY DEGREES OF FREEDOM

MODE	EIGENVALUE	ITERATIONS S.P.	U.P.	AITKENS S.P.	U.P.
COLUMN 1	COLUMN 2	COLUMN 3	COLUMN 4	COLUMN 5	COLUMN 6
1 -0.22672209E 00	0.92881241E-01	-0.10988617E 00	-9.189249931E 00	-8.11566342E 00	0.10828242E-02
2 -0.24322614E 00	0.96231452E-01	-0.11262997E 00	-6.13723300E 00	-6.14282341E 00	0.42084169E-03
3 -0.18896246E 00	0.9612126536E-01	0.36834289E-02	-9.72438926E-01	0.39344759E-01	-9.37217668E-01
4 -0.13740121E 00	0.94912446E-01	0.38691294E-02	-9.12866633E 00	0.62688741E-02	-9.4150643E-01
5 -0.16190737E 00	0.24659401E-01	0.27872387E-01	-6.15872387E-01	0.38627622E 00	-0.14034653E 00
6 0.13893190E 00	0.93865569E 01	0.27711237E 00	-7.05199444E-01	0.38137447E 00	-0.15814607E 00
7 0.57352650E 00	0.514K/600E-01	0.63461424E 00	9.2094W7631E-01	0.72148682E 00	-0.93107597E-01
8 0.54571530E 00	0.66242930E-01	0.64748610E 00	-9.26468339E-01	0.75147159E 00	-0.13747385E 00
9 0.10100330E 01	0.59255681E-00	0.98694971E 00	0.36698169E-01	0.94384934E 00	0.67121342E-01
10 0.97166492E 00	0.1926324E-03	0.10000000E 01	0.10268105E-03	0.10600000E 01	0.73126528E-00

## EIGENVECTORS

60

COLUMN 7	COLUMN 8
1 0.51517504E-01	-0.2863167E-01
2 0.3740376E-03	-0.5456816E-02
3 -0.61298371E-01	-0.81922612E-01
4 -0.727671RUE-01	-0.5344277E-01
5 0.54630956E 00	-0.13743654E 00
6 -0.51010173E 00	-0.1630349E 00
7 -0.12070490E 00	-0.60967883E-01
8 -0.827351729E-01	-0.1190777E 00
9 0.10000000E 01	0
10 -0.941057171E 00	-0.3070476E-03

## CHECK EIGENVALUES AND EIGENVECTORS

$\alpha = -229.67607E-08 - 0.1592595E-08 \quad \beta = 0.130141E-06 \quad \gamma = -0.15691698E-06 \quad \delta = 0.4890500E-0 / 0.13604395E-0 /$   
 $\epsilon = 0.19045539E-07 - 0.123168739E-07$

	COLUMN 1	COLUMN 2	COLUMN 3	COLUMN 4	COLUMN 5	COLUMN 6
1	-0.22972211E-06	0.47861248E-01	-0.10951607E-01	-0.10249928E-01	-0.11566528E-01	0.10824196E-02
2	-0.24322616E-06	0.9621465E-01	-0.125989E-01	-0.132529E-01	-0.14202324E-01	0.42061735E-03
3	-0.10895248E-09	0.910124561E-01	-0.10895270E-01	-0.11230898E-01	-0.39344898E-01	-0.57211735E-01
4	-0.13140214E-06	0.959471E-01	-0.14669318E-01	-0.12666631E-01	-0.62602456E-02	-0.41586375E-01
5	0.16190735E-09	0.95669469E-01	-0.2369996E-01	-0.21872351E-01	-0.3896277E-01	-0.14034820E-01
6	0.1389196E-09	0.938102252E-01	-0.27711225E-01	-0.2552998E-01	-0.3813746E-01	-0.15814662E-01
7	0.57152656E-09	0.52462666E-01	-0.63801430E-01	-0.2940764E-01	-0.72148695E-01	-0.931094646E-01
8	0.2451247E-09	0.6762452E-01	-0.64748619E-01	-0.26464305E-01	-0.7514767E-01	-0.1347361E-01
9	0.11000111E-01	0.19256939E-01	"	0.36009610E-01	0.94384457E-01	0.071212431E-01
10	0.97106389E-09	0.10265281E-01	-0.100999E-01	-0.100999E-01	-0.19268157E-10	-0.15925522E-09
	COLUMN 7	COLUMN 8	COLUMN 9	COLUMN 10	COLUMN 11	COLUMN 12
1	0.52517193E-02	-0.28639315E-01	-0.100999E-01	-0.100999E-01	-0.100999E-01	-0.100999E-01
2	0.37102715E-03	-0.54459635E-02	-0.100999E-01	-0.100999E-01	-0.100999E-01	-0.100999E-01
3	-0.61294424E-01	-0.519216/2E-01	-0.100999E-01	-0.100999E-01	-0.100999E-01	-0.100999E-01
4	-0.72261575E-01	-0.5164522E-01	-0.100999E-01	-0.100999E-01	-0.100999E-01	-0.100999E-01
5	-0.5637959E-09	0.0 -0.1143433E-09	-0.100999E-01	-0.100999E-01	-0.100999E-01	-0.100999E-01
6	-0.5104036E-09	0.0 -0.1630335E-09	-0.100999E-01	-0.100999E-01	-0.100999E-01	-0.100999E-01
7	-0.1774819E-09	0.0 -0.69967363E-01	-0.100999E-01	-0.100999E-01	-0.100999E-01	-0.100999E-01
8	-0.8756019E-01	-0.180159E-01	-0.100999E-01	-0.100999E-01	-0.100999E-01	-0.100999E-01
9	0.00000000E-01	0.12743709E-08	-0.100999E-01	-0.100999E-01	-0.100999E-01	-0.100999E-01
10	0.94199217E-09	-0.80785611E-02	-0.100999E-01	-0.100999E-01	-0.100999E-01	-0.100999E-01

## MODE FRQCY (CPS) DAMPING VELOCITY (KNOTS)

1	0.20447998E-01	-0.69443715E-03	0.70819116E-03
2	0.2449231E-01	-0.12056207E-01	0.92947631E-03
3	0.447133568E-01	0.27818862E-01	0.15162683E-04
4	0.69852134E-01	-0.61699671E-01	0.23732553E-04

**SECTION 8**

**PROGRAM LISTING**

```

$      OPTION FORTRAN
$      FORTRAN LSTOU.DFCK
C MAIN      FLUTTER OVERLAY
C          JAN 13.1967
C          COMM: IT(218)
C          CHANGE BCD TAPES TO BINARY TAPES
10 CALL LLINK (6HPARLT)
CALL PART1
CALL LLINK (6HPAR/TT)

CALL PART2
GO TO 10
END

$      FORTRAN LSTOU.DFCK
C MPRINT
      SUBROUTINE MPRINT (A,M,N,MD,NTAPE)
      DIMENSION A(1), IT(6), C(6)
      EQUIVALENCE (IT,C)
2 FORMAT (1H , 4X, 6( 6X, 7HCOLUMN 1I4 )   //    )
3 FORMAT (1H 1I4, X,   (6E 17.8)  )
N1=N
N2=6
N3=6
N4=1
4 IF (N3-N1) 6,6,5
5 N2=N1-N3+6
N3=N1
6 K=0
DO 7 I = N4,N4
K=K+1
7 IT(K)=I
      WRITE (NTAPE,2) (IT(I),I=1,N2)
DO 9 J=1,M
K=0
L=MD*(N4-1)+J
DO 8 J=N4,N3
K=K+1
C(K)=A(L)
8 L=L+MD
9 WRITE (NTAPE,3) L,(C(K),K=1,N2)
IF (N3-N1) 10,11,11
10 N3=N3+6
N4=N4+6
GO TO 4
11 RETURN
END

$      FORTRAN LSTOU.DFCK
C MPUNCH
      SUBROUTINE MPUNCH(A,M,N,IOUT,ITRA,ITRG,BCDZ,MAXM,NTAPE,NCARDS)
      DIMENSION A(1)
      RETURN
END

$      LINK PAR1 TT
$      FORTRAN LSTOU.DFCK
C PART1
      SUBROUTINE PART1
C NSUR=TOTAL NUMBER OF SURFACES ALLOWED.
C NDENS=TOTAL NUMBER OF DENSITIES ALLOWED.
C NRIGID=TOTAL NUMBER OF RIGID BODIES ALLOWED
C NSIZF=TOTAL NUMBER CONTROL POINTS ON ANY ONE SURFACE ALLOWED
C NMODES=TOTAL NUMBER MODES INPUT ON ANY ONE SURFACE.

```

001  
002  
003  
004  
005  
006

DIMENSION ISXST(20), ISW(20), HR(21), S(21), RHO(20), UM(6,6),  
 1 DU(6,12), DMBAR(6,12), BARMRR(6,12), LOW(50), LHIGH(50)  
 2 , IT(218), VELCT(20), NSIZES(20).  
 3 A(50,100), F(50,100), U(50,100), HR(50,6), HRT(6,100),  
 4 HT(6,100), G(6,100)

C THE FOLLOWING STATEMENT(S) HAVE BEEN MANUFACTURED BY THE TRANSLATOR TO  
 C COMPENSATE FOR THE FACT THAT EQUIVALENCE DOES NOT REORDER COMMON--  
 COMMON IT

EQUIVALENCE (IT(1),ISXST), (IT(21),ISW), (IT(41),RHO),  
 1 ,(IT(61),NTAPE1), (IT(62),NTAPE2), (IT(63),NTAPE3),  
 2 ,(IT(64),NTAPE4), (IT(65),NTAPE5), (IT(66),NTAPE6),  
 3 ,(IT(67),NTAPE7), (IT(68),NTAPE8), (IT(69),NTAPE9),  
 4 ,(IT(70),NSUR), (IT(71),NRIGID), (IT(72),BREF),  
 5 ,(IT(73),NAERO), (IT(74),NFUS), (IT(75),NDENS),  
 6 ,(IT(76),MODES), (IT(77),NPPOINT), (IT(78),NPUNCH),  
 7 ,(IT(79),MAXR), (IT(80),MAXQ), (IT(81),MAXS),  
 8 ,(IT(82),NC), (IT(83),NSURFS), (IT(84),NR?),  
 9 ,(IT(85),BR), (IT(106),S), (IT(127),VELCTY),

EQUIVALENCE (IT(147),NTAPEU), (IT(148),NRHO), (IT(149),NITRSP),  
 1 ,(IT(150),NITRDP), (IT(151),FPSP), (IT(152),FPDP),  
 2 ,(IT(153),PICON), (IT(154),NVEL), (IT(155),NCARDS),  
 3 ,(IT(156),AITKEN), (IT(157),NGO), (F,G), (F(601,1),HT)  
 4 ,(U,LOW), (U(51,1),LHIGH), (IT(158),FK), (IT(159),SDR)  
 5 (CON), (IT(160),NSIZES), (IT(180),UM), (UM,AR,BARMRR)  
 6 ,(IT(216),NDELM),(IT(217),AITKED),(IT(218),KPART)

1 FORMAT (18I4)  
 2 FORMAT (6E12.8)  
 3 FORMAT (1H-16X, 41H FLUTTER ANALYSIS BY A COLLOCATION METHOD  
 1 /42H USING AERODYNAMIC INFLUENCE COEFFICIENTS //10H NSUR =  
 2 112, 10H NAERO = 114, 11H NRIGID = 112, 9H NFUS =  
 3 112, 10H NDENS = 114, 14H MODES OUT = 112  
 4 , 9H NDELM = 112, 10H NPUNCH = 112 )

4 FORMAT (1H0,22X, 11H B (REF) = 1E20.8, 5X, 4HK = 1E20.8 //1H0 25X,  
 1 7HSURFACE 1RX, 1H0 19X, 1HS 10X, 20HEXTERNAL STORES SIZE //)

5 FORMAT (1H0 10X, 21H B RIGID COMPONENT = 1E18.8, 5Y, 8H S RIGID  
 1 .13H COMPONENT = 1E18.8 )

6 FORMAT (1H 1129, 2( 5X, 1E20.8), 1112 )

10 FORMAT (1H1 48X, 12H MASS MATRIX )

11 FORMAT (41H0 NUMBER OF CONTROL POINTS THIS MATRIX, ( 114,  
 1 48H) AND TOTAL NUMBER OF CONTROL POINTS EXPECTED, ( 114,  
 2 57H) DO NOT AGREE. PROGRAM CONTINUED...)

12 FORMAT (1H) 42X, 24H RIGID BODY MODAL MATRIX )

13 FORMAT (1H .88X, 8HSURFACE 112, 1H, 116, 15H CONTROL POINTS)

14 FORMAT (1H1 41X, 20H FLEXIBILITY MATRIX )

15 FORMAT (1H1 46X, 18H WEIGHTING MATRIX )

16 FORMAT (1H1 28X, 24H RIGID COMPONENT AERO MATRIX, 119, 8H CONTROL  
 1 .7H POINTS )

17 FORMAT (1R1 .33X, 20H AERODYNAMIC MATRIX 8X, 10H J./K/R =  
 1 1E20.8 )

18 FORMAT (1H0 10X, 23H RIGID COMPONENT MODES, 1110,  
 1 1/H CONTROL POINTS. )

19 FORMAT (1H0 30X, 24H RIGID COMPONENT MASS MATRIX )

20 FORMAT (47H) ERROR IN INVERSE ROUTINE. PROGRAM TERMINATED )

21 FORMAT (1H .88X, 8HSURFACE 112, 1H, 6X, 13H NO WEIGHTING  
 1 .7H MATRIX )

22 FORMAT ( 3E12.8, 214 )

23 FORMAT ( 8H0FPSP = 1E16.8, 1X, 8H EPUP = 1E16.8, 1X,  
 1 10H AITKEN = 1E16.8, 1X, 10H NITRSP = 114, 1X,  
 2 10H NITRDP = 114 )

24 FORMAT (1H0 48X, 20H GENERALIZED MASSES //// (1H .38X,  
 1 5H MASS 114, 4H = 1E16.8 ) )

25 FORMAT ( 1H0 30X, 23H RIGID COMPONENT MODES    )	079
26 FORMAT ( 214, 62X, 1A6, 1I4 )	080
27 FORMAT ( 1H0 34X, 23H PUNCHED CARDS NUMBERS 1A6, 1I4, -6H THRU 1                1A6, 1I4 )	081
28 FORMAT (1H0 20X, 3H K= 1E16.R )	082
DATA Q000CT/02020.30440005/	083
BCDZ =Q000CT	085

S                    OPTION FORTRAN  
S                    FORTRAN LSTOUT.DECK  
C MAIN            FLUTTER OVERLAY  
C                    JAN 13, 1967  
C                    COMMON IT(218)  
C                    CHANGE BCD TAPES TO BINARY TAPES  
10 CALL LLINK (6HPAR1TT)  
CALL PART1  
CALL LLINK (6HPAR2TT)

```

$      OPTION FORTRAN
$      FORTRAN LSTOU,DECK
C MAIN      FLUTTER OVERLAY
C          JAN 13, 1967
COMMON IT(218)
CHANGE BCD TAPES TO BINARY TAPES
10 CALL LLINK (6HPAR1TT)
CALL PART1
CALL LLINK (6HPAR2TT)

CALL PART2
GO TO 10
END

$      FORTRAN LSTOU,DECK
C MPRINT
SUBROUTINE MPRINT (A,M,N,MD,NTAPE)           HM14007
DIMENSION A(1), IT(6), C(6)                  HM140078
EQUIVALENCE (IT,C)                          HM140079
2 FORMAT (1H , 4X, 6( 6X, 7HCOLUMN   114 )    //   ) HM14008
3 FORMAT (1H 114, X,   (6E 17.8)   )          HM14008
N1=N                                         HM140084
N2=6                                         HM140085
N3=6                                         HM140086
N4=1                                         HM140087
4 IF (N3-N1) 6,6,5                         HM140088
5 N2=N1+N3+6                                HM140089
N3=N1                                         HM140090
6 K=0                                         HM140091
DO 7 I= N4,N3                               HM140092
K=K+1                                         HM140093
7 IT(K)=1                                     HM140094
      WRITE (NTAPEF,2) (IT(I),I=1,N2)          HM140095
DO 8 I=1,M                                    HM140096
K=0                                         HM140097
L=MD*(N4-1)+1                            HM140098
DO 9 A J=N4,N3                               HM140099
K=K+1                                         HM140100
C(K)=A(I)                                     HM140101
8 L=L+MD                                      HM140102
9 WRITE (NTAPEF,3) I,(C(K),K=1,N2)          HM140103
IF (N3-N1) 10,11,11                          HM140104
10 N3=N3+6                                    HM140105
N4=N4+6                                     HM140106
GOTO 4                                       HM140107
11 RETURN                                     HM140108
END

$      FORTRAN LSTOU,DECK
C MPUNCH
SUBROUTINE MPUNCH(A,M,N,IOUT,ITRA,ITRG,BCDZ,MAXM,NTAPE,NCARDS) 0010
DIMENSION A(1)                                0020
RETURN                                         0030
END                                         0040
LINK PARITT
FORTRAN LSTOU,DECK

C PART1
SUBROUTINE PART1                           0010
NSUR=TOTAL NUMBER OF SURFACES ALLOWED.    0020
NDENS=TOTAL NUMBER OF DENSITIES ALLOWED.   0030
NRIGID=TOTAL NUMBER OF RIGID BODIES ALLOWED 0040
NSTZF=TOTAL NUMBER CONTROL POINTS ON ANY ONE SURFACE ALLOWED 0050
NMODES=TOTAL NUMBER MODES INPUT ON ANY ONE SURFACE.        0060

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DIMENSION ISXST(20), ISW(20), HR(21), S(21), RHO(20), DM(6,6),  
 1 DD(6,12), DMBAR(6,12), BARMRR(6,12), LOW(50), LHIGH(50) 0120  
 2 , IT(21R), VELCTY(20), NSIZES(20) 0130  
 3 A(50,150), F(50,100), U(50,100), HR(50,6), IRT(6,100) 0140  
 4 HT(6,100), G(6,100) 0150  
 0160  
 C THE FOLLOWING STATEMENT(S) HAVE BEEN MANUFACTURED BY THE TRANSLATOR TO  
 COMPENSATE FOR THE FACT THAT EQUIVALENCE DOES NOT REORDER COMMON-- 0170  
 COMMON IF  
 EQUIVALENCE (IT(1),ISXST), (IT(21),ISW), (IT(41),RHO) 0180  
 1 . (IT(51),NTAPE1), (IT(62),NTAPE2), (IT(63),NTAPE3), 0190  
 2 (IT(64),NTAPE4), (IT(65),NTAPE5), (IT(66),NTAPE6), 0200  
 3 (IT(67),NTAPE7), (IT(68),NTAPE8), (IT(69),NTAPE9), 0210  
 4 (IT(70),NSUR), (IT(71),NRIGID), (IT(72),HREF), 0220  
 5 (IT(73),NAERO), (IT(74),NFUS), (IT(75),NDENS), 0230  
 6 (IT(76),MODES), (IT(77),NPOINT), (IT(78),NPUNCH), 0240  
 7 (IT(79),MAXR), (IT(80),MAXU), (IT(81),MAXS), 0250  
 8 (IT(82),NC), (IT(83),NSURFS), (IT(84),NP2), 0260  
 9 (IT(85),HR), (IT(106),S), (IT(127),VELCTY) 0270  
 EQUIVALENCE (IT(147),NTAPEU), (IT(148),NRHO), (IT(149),NITRSP), 0280  
 1 (IT(150),NITRDP), (IT(151),EPSP), (IT(152),EPDP), 0290  
 2 (IT(153),PICON), (IT(154),NVEL), (IT(155),NCARDS), 0300  
 3 (IT(156),AITKEN), (IT(157),NGO), (F,G), (F(601,1),HT) 0310  
 4 (U,LOW), (U(51,1),LHIGH), (IT(158),FK), (IT(159),SQR) 0320  
 5 CON) , (IT(160),NSIZES), (IT(180),DM), (DM=AR,BARMRR) 0330  
 6 , (IT(216),NDELM),(IT(217),AITKED),(IT(218),KPART) 0340  
 0350  
 1 FORMAT (181A)  
 2 FORMAT (6E12.8)  
 3 FORMAT (1H 16X, 41H FLUTTER ANALYSIS BY A COLLOCATION METHOD 0450  
 1 42H USING AERODYNAMIC INFLUENCE COEFFICIENTS //10H NSUR = 0460  
 2 112, 10H NAERO = 114, 11H NRIGID = 112, 9H NFUS = 0470  
 3 112, 10H NDENS = 114, 14H MODES OUT = 112 0480  
 4 , 9H NDELM = 112, 10H NPUNCH = 112 ) 0490  
 4 FORMAT (1H0 22X, 11H B (REF) = 1E20.8, 5X, 4HK = 1E20.8 /1H0 25X,  
 1 7HSURFACE 18X, 1HB 19X, 1HS 10X, 20HEXTERNAL STORES SIZE //) 0500  
 5 FORMAT (1H0 10X, 2)H R RIGID COMPONENT = 1E18.8, 5Y, 8H S RIGID 0510  
 1 13H COMPONENT = 1E18.8 ) 0520  
 6 FORMAT (1H 1E20, 2( 5X, 1E20.8), 1112 ) 0530  
 10 FORMAT (1H1 48X, 12H MASS MATRIX ) 0540  
 11 FORMAT (41H0 NUMBER OF CONTROL POINTS THIS MATRIX, / 114, 0550  
 1 48H) AND TOTAL NUMBER OF CONTROL POINTS EXPECTED, ( 114, 0560  
 2 37H) DO NOT AGREE. PROGRAM CONTINUED... 0570  
 12 FORMAT (1H1 42X, /4H RIGID BODY MODAL MATRIX ) 0580  
 13 FORMAT (1H 38X, RHSURFACE 112, 1H, 116, 15H CONTROL POINTS) 0590  
 14 FORMAT (1H1 43X, 20H FLEXIBILITY MATRIX ) 0600  
 15 FORMAT (1H1 46X, 18H WEIGHTING MATRIX ) 0610  
 16 FORMAT (1H1 28X, 29H RIGID COMPONENT AERO MATRIX, 119, RH CONTROL 0620  
 1 /H POINTS ) 0630  
 17 FORMAT (1H1 33X, 20H AERODYNAMIC MATRIX 8X, 10H 1./K R = 0640  
 1 1E20.8 ) 0650  
 18 FORMAT (1H0 50X, 23H RIGID COMPONENT MODES, 1110, 0660  
 1 1/H CONTROL POINTS. ) 0670  
 19 FORMAT (1H0 10X, 24H RIGID COMPONENT MASS MATRIX ) 0680  
 20 FORMAT (47H1 ERROR IN INVERSE ROUTINE. PROGRAM TERMINATED ) 0690  
 21 FORMAT ( 1H 38X, RHSURFACE 112, 1H, 6X, 13H NO WEIGHTING 0700  
 1 7H MATRIX ) 0710  
 22 FORMAT ( 3E12.8, 214 ) 0720  
 23 FORMAT ( RHEPSP = 1E16.8, 1X, RH EPDP = 1E16.8, 1X, 0730  
 1 10H AITKEN = 1E16.8, 1X, 10H NITRSP = 114, 1X, 0740  
 2 10H NITRDP = 114 ) 0750  
 24 FORMAT (1H4 40X, 20H GENERALIZED MASSES //// (1H 30X, 0760  
 1 5H MASS 114, 3H = 1E16.8 ) ) 0770  
 0780

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25 FORMAT ( 1H0 3X, 23H RIGID COMPONENT MODES // )      0/90
26 FORMAT ( 214, 62X, 1A6, 1I4 )                      0800
27 FORMAT ( 1H0 3X, 23H PUNCHED CARDS NUMBERS 1A6, 1I4, 6H THRU
1          1A6, 1I4 )                                0910
28 FORMAT (1H0 20X, 3H K= 1E16.8 )                  0820
DATA QDUCT/0202030440005/
RC02 = QDUCT
NTAPE0 = PUNCH OUTPUT TAPE
NTAPE2 = INPUT TAPE
NTAPE3 = OUTPUT PRINT TAPE
NTAPE4 = /
NTAPE5 = / ARE UTILITY TAPES
NTAPE6 = /
NTAPE7 = /
NTAPE8 = /
NTAPE9=/
IF ( NGO=98765 )      90,97,99
97 IF ( NAFRO )        98,320,98
)8 NAFRO = NAERO-1
IF ( NAFRO )          99,99,1/0
99 NTAPE0 = 8
NTAPE2=5
NTAPE3=6
NTAPE4 = 9
NTAPE5 = 3
NTAPE6 = 4
NTAPE7=11
NTAPE8=1
NTAPE9 =10
MAXR = 50
MAXQ = 6
NCON=0
MAXS=50
1110
1120
1130
1140
1150
1160
1170
1180
1190
1200
1210
1220
1230
1240
1250
1260
1270
1280
1290
1300
1310
1320
1330
1340
1350
1360
1370
1380
1390
991 REWIND NTAPE4
REWIND NTAPE5
REWIND NTAPE6
REWIND NTAPE9
SORCON = SQRT( 386.0 ) / ( 2.0*3.14159 )
EPSP = .5E-06
FPDP = .5E-07
AITKFN = .9
AITKFD = .9
PICON = .592142.0*3.14159
NCARDS = 0
NVFI = 0
NC=1
NITRSP=40
NITRDP=100
RHO(1) = 0.0
100 CALL RDIN (NTAPE2,NTAPE3,1)
READ (NTAPE2,1) NSUR, NAERO, NRIGID, NFUS, NDENS, MODES
101 INDFIM, NPUNCH, NCON
READ (NTAPE2,2) FK
WRITE (NTAPE3,3) NSUR, NAERO, NRIGID, NFUS, NDENS, MODES
102 , INDFIM, NPUNCH
NR2=NRIGID*NC
NSURFS=NSUR+NFUS
IF ( NCON )      102,104,102
103 READ (NTAPE2,22) EPSP,FPDP,AITKEN, NITRSP,NITRDP

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      READ (NTAPE2,22)AITKEN
      WRITE (NTAPE3,23)EPSP, EPDP, AITKEN, NITRSP, NITROP 1400
104 IF ( NAERO )           105,103,105 1410
103 WRITE (NTAPE3,24)FK 1420
      GOTO 111 1430
105 READ (NTAPE2,1)(ISXST(I),ISH(I),I=1,NSUR) 1440
      READ (NTAPE2,2)BREF, (VELCTY(I),I=1,NAERO) 1450
      NC=2 1460
      NR2= NRIGID +NC 1470
      READ (NTAPE2,2)(BR(I),S(I),I=1,NSURFS) 1480
      IF ( NDENS )           106,107,108 1490
106 READ (NTAPE2,2)(RHO(I),I=1,NDFNS) 1500
107 IF ( NFUS )           108,109,109 1510
108 WRITE (NTAPE3,5)BR(), S() 1520
109 WRITE (NTAPE3,4)BREF ,FK 1530
      DO 110 I=1,NSUR 1540
          J=I+NFUS 1550
110 WRITE (NTAPE3,6) I, BR(J), S(J) .ISXST(I) 1560
***** READ IN FUSE GE MASS CHARACTERISTICS 1580
C READ IN FUSE GE MASS CHARACTERISTICS 1590
111 IF ( NRIGID )           112,117,112 1600
112 IF ( NDELM )           115,113,115 1610
113 DO 114 I=1,NRIGID 1620
      DO 114 J=1,NRIGID 1630
114 DM(I,J)=0.0 1640
      GOTO 117 1650
115 DO 116 I=1,NRIGID 1660
116 READ (NTAPE2,2)(DM(J,I),J=1,NRIGID) 1670
      WRITE (NTAPE3,19)
      CALL MPRINT (DM,NRIGID,NRIGID,MAXQ,NTAPE3) 1680
***** READ MASS MATRIX FOR EACH SURFACE, STORE SYSTEM MASS MATRIX ON NTAPE4 1690
117 K1=0 1700
      WRITE (NTAPE3,10)
      DO 120 I=1,NSUR 1710
          READ (NTAPE2,1)NSIZEF 1720
          READ (NTAPE2,1)(LOW(J),LHIGH(J),J=1,NSIZE) 1730
          DO 119 J=1,NSIZEF 1740
              DO 118 K=1,NSIZE 1750
                  A(K,J)=0.0 1760
118     N1=LOW(J) 1770
      N2=LHIGH(J) 1780
119     READ (NTAPE2,2)(A(N,J),N=N1,N2) 1790
      WRITE (NTAPE4)NSIZE, NSIZE, ((A(N,J),N=1,NSIZE),J=1,NSIZE) 1800
      WRITE (NTAPE3,11)I, NSIZE 1810
      CALL MPRINT (A,NSIZE,NSIZE,MAXR,NTAPE4) 1820
      NSIZFS(I)=NSIZEF 1830
120     K1=K1+NSIZEF 1840
***** NPOINT = TOTAL NUMBER OF CONTROL POINTS ON ALL SURFACES. 1850
      NPOINT=K1 1860
C READ IN RIGID BODY MODAL MATRIX FOR EACH SYSTEM. 1870
121 IF ( NFUS )           121,123,121 1880
121 READ (NTAPE2,1)NSIZEF 1890
      DO 122 J=1,NRIGID 1900
122 READ (NTAPE2,2)(HR(I,J),I=1,NSIZE) 1910
      WRITE (NTAPE3,18)NSIZEF 1920
      CALL MPRINT (HR,NSIZF,NRIGID,MAXS,NTAPE3) 1930
      WRITE (NTAPE4)NSIZEF, NRIGID, ((HR(I,J),I=1,NSIZE),J=1,NRIGID) 1940
123 IF ( NRIGID )           124,128,124 1950
124 K1=1 1960

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      WRITE (NTAPE3,12)
      DO 126 ISUR=1,NSUR
        READ (NTAPE2,1) NSIZEF
        K2=K1+NS1/F-1
        DO 125 J=1,NRIGID
125       READ (NTAPE2,2)(HR(I,J),I=K1,K2)
        WRITE (NTAPE3,1)ISUR,NSIZE
        CALL MPRINT (HR(K1,1),NSIZEF,NRIGID,MAXS,NTAPE3)
126       K1=K1+NS1/F
        WRITE (NTAPE5)NPOINT, NRIGID, ((HR(N,J),N=1,NPOINT), I=1,
1           NRIGID )
        IF ( K1-NPOINT-1) 127,128,127
127 WRITE (NTAPE3,11)K1, NPOINT
***** READ IN FLFXIBILITY MATRIX FOR EACH SURFACE,      STORE ON NTAPES
128 K1=0
        WRITE (NTAPE3,14)
        DO 153 I=1,NSUR
        READ (NTAPE2,1)NSIZE, J, IFORM, IROWS
        CALL MRFAD (A,NSIZE,NSIZE,IFORM,IROWS,0,1,F,MAXR,NTAPE2,NTAPE3)
        WRITE (NTAPE3,15)I,NSIZE
        CALL MPRINT (A,NSIZEF,NSIZE,MAXR,NTAPE3)
        WRITE (NTAPE5)NSIZE, NSIZE, ((A(J,K),J=1,NSIZE),K=1,NSIZE)
153 K1=K1+NSIZE
        IF ( K1-NPOINT ) 158,164,158
158 WRITE (NTAPE3,11)K1, NPOINT
164 IF ( NAERO ) 166,165,166
165 NRHO=1
        DO 500 I=1,NRIGID
        DO 500 J=1,NRIGID
500       AQ(I,J)=0.0
        WRITE (NTAPE5)((DM(I,J),I=1,NRIGID),J=1,NRIGID)
        NC=NC
        GOTO 215
***** READ IN WEIGHTING MATRIX FOR EACH SURFACE.....STORE ON NTAPE6,
166 WRITE (NTAPE3,16)
        DO 178 I=1,NSUR
          IF ( ISH(I) ) 167,177,167
167       N1=ISYST(I)
          IF ( N1 ) 168,172,168
168       DO 179 J=1,N1
          DO 179 L=1,MAXR
            A(J,L)=0.0
169       A(L,J)=0.0
170       A(J,J)=1.0
        READ (NTAPE2,1)NXST, J, IFORM, IROW
        IF ( NXST ) 171,172,171
171       CALL MRREAD (A,NXST,NXST,IFORM,IROW,0,1,F,MAXR,NTAPE2,NTAPE3)
172       K=N1+1
        READ (NTAPE2,1)NSIZE, NPART, IFORM, IROW
        IF ( IFORM ) 174,173,174
173       CALL MRREAD (A(K,K),NSIZEF,NSIZEF,0,0,0,1,F,MAXR,NTAPE2,NTAPE3)
        K=K+NSIZEF
        GOTO 176
174       DO 175 J=1,NPART
          READ (NTAPE2,1)NSIZEF
          N=N+F
1741      DO 1741 L=K,N
          DO 1741 M=1,K
1741      A(M,L)=0.0

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```

      CALL MPRINT (A(K,K),NSIZE,NSIZE,1,IROW,0,0,F,MAXR,NTAPE2,NTAPE3) 2670
  175      K=K+NSIZEF 2680
  176      K=K-1 2690
***** 2700
  177      WRITE (NTAPE3,15) I, K 2710
  178      CALL MPRINT (A,K,K,MAXR,NTAPE3) 2720
  179      WRITE (NTAPE3) K, K, ((A(J,L),J=1,K),L=1,K) 2730
  180      GOTO 178 2740
  181      WRITE (NTAPE3,21)I 2750
  182      CONTINUE 2760
  183      REWIND NTAPE3 2770
  184      REWIND NTAPE7 2780
  185      NCX=NC 2790
  186      NVFL = NVEL+1 2800
***** 2810
  187      IF SERIES OF DENSITIES FOR EACH V/R OMEGA, READ IN THAT SERIES. 2820
  188      IF ( NDFNS )      180,181,180 2830
  189      NRHO=NDENS 2840
  190      GOTO 182 2850
  191      READ (NTAPE2,1)NRHO 2860
  192      READ (NTAPE2,2)(RHO(I),I=1,NRHO) 2870
***** 2880
  193      READ IN COMPLEX AERODYNAMIC MATRIX FOR EACH SURFACE 2890
  194      DO 210  I=1,NSURFS 2900
  195      K=1 2910
  196      K2=1 2920
  197      IF ( NFUS )      183,184,183 2930
  198      IF ( I=1 )      184,188,184 2940
  199      L=I-NFUS 2950
  200      IF ( ISXST(L) )      185,188,185 2960
  201      K=ISXST(L)+1 2970
  202      K2 = K+ISXST(L) 2980
  203      DO 186  J=1,K 2990
  204      DO 186  L=1,K2 3000
  205      A(J,L)=0.0 3010
  206      READ (NTAPE2,1)NXST, J, IFORM, IROW 3020
  207      IF ( NXST )      187,188,187 3030
  208      N= NXST *NC 3040
  209      CALL MREAD (A,NXST,N,IFORM,IROW,0,1,U,MAXR,NTAPE2,NTAPE3) 3050
  210      READ (NTAPE2,2)VFLC 3060
  211      READ (NTAPE2,1)NSIZEF, NPART, IFORM, IROW 3070
  212      IF ( IFORM )      190,189,190 3080
  213      N= NSIZEF *NC 3090
  214      CALL MREAD (A(K,K),NSIZE,N ,IFORM,IROW,0,1,U,MAXR,NTAPE2,NTAPE3) 3100
  215      NS17F=NSIZEF+K-1 3110
  216      GOTO 193 3120
  217      DO 192  J=1,NPART 3130
  218      READ (NTAPE2,1)NSIZE 3140
  219      N=K2+NC 3150
  220      DO 191  M=K2,N 3160
  221      DO 191  I=1,K 3170
  222      A(I,M)=0.0 3180
  223      N= NS17F *NC 3190
  224      CALL MREAD (A(K,K),NSIZE,N,1,IROW,0,0,U,MAXR,NTAPE2,NTAPE3) 3200
  225      K=K+NSIZEF 3210
  226      K2=K2+N 3220
  227      NS17F=K-1 3230
  228      N=K2-1 3240
  229      193 IF ( I=1 )      199,194,190 3250
  230      194 IF ( NFUS )      195,197,195 3260
  231      WRITE (NTAPE3,15)NSIZE 3270

```

```

      CALL MPRINT (A,NSIZE,N,MAXR,NTAPE5)          3290
C*****                                         3290
C COMPUTE (DO) = (HR)T * (CH) * (HR)           3300
      K1=1                                         3310
      K2=1                                         3320
      M=NC+1                                       3330
      READ (NTAPE5)NSIZE, L, ((U(L,J),L=1,NSIZE),J=1,NRIGID) 3340
      CALL MMULTD (A,M,U,O,F,NSIZE,NSIZE,NRIGID,MAXR,MAXR,MAXR) 3350
      DO 196 L=1,NSIZE                           3360
         DO 198 J=1,NRIGID                      3370
196     A(J,L)=U(L,J)                         3380
      CALL MMULTD (A,O,F,M,DO,NRIGID,NSIZE,NRIGID,MAXR,MAXO,MAXU) 3390
      GOTO 210                                     3400
197     DO 198 L=1,NRIGID                      3410
         DO 198 J=1,NR2                          3420
198     DO(L,J)=0.0                            3430
199     I=1-NFUS                                3440
      IF ( ISW(L) )      202,200,202          3450
200     WRITE (NTAPE7)NSIZE, N, ((A(J,M),J=1,NSIZE),M=1,N) 3460
      GOTO 208                                     3480
202     READ (NTAPE6)I, L, ((F(J,M),J=1,L),M=1,L) 3490
      IF ( NSIZE=L )      204,206,204          3500
204     WRITE (NTAPE3,11)NSIZE,L                3510
206     CALL MMULTD (F,O,A,NC-1,U,L,L,L,MAXR,MAXR,MAXR) 3520
      WRITE (NTAPE7)NSIZE, N, ((U(J,M),J=1,NSIZE),M=1,N) 3530
208     WRITE (NTAPE3,17)VELC                  3550
      L=I-NFUS                                3560
      WRITE (NTAPE3,13)L, NSIZE                 3570
      CALL MPRINT (A,NSIZE,N,MAXR,NTAPE3)        3580
210     CONTINUE                                3590
C*****                                         3600
C CARRY ON FROM HERE TO END ONCE FOR EACH DENSITY. 3610
      215 DO 300 IRHO=1,NRHO
      K=NC+NPOINT                               3620
      DO 216 I=1,NPOINT
         DO 216 J=1,K
216     U(I,J)=0.0                            3630
      REWIND NTAPE4
      REWIND NTAPE5
      REWIND NTAPE7
      CON=RHO(IRHO)*RR(1)**2*S(1)  #32.174 3640
      IF ( NRIGID)  218,222,218
218     DO 220 I=1,NRIGID
         DO 220 J=1,NR2,NCX
            DMBAR(I,J+1)=CON*DQ(I,J+1)
            K=J/NC+NC-1
220     DMBAR(I,J)=DM(I,K)+CON*DQ(I,J)    3650
C*****                                         3660
C READ ENTIRE HR MATRIX.
      READ (NTAPE4)I,I, ((HR(I,J),I=1,NPOINT),J=1,NRIGID) 3670
      222 K1=0
      DO 246 ISUR=1,NSUR
         K=ISUR+NFUS
         CON=RHO(IRHO)*RR(K)**2*S(K)  #32.174 3680
C*****                                         3690
C             READ (M) I
      READ (NTAPE4)NSIZEF, NSIZEF, ((F(I,J),I=1,NSIZE), J=1,NSIZE) 3700
      IF ( NAFRD )      221,221,223          3710
      221 DO 226 I=1,NSIZE
         DO 226 J=1,NSIZE
226     A(I,J)=F(I,J)                        3720

```

```

I=NSIZE          3910
GOTO 231        3920
C*****          3930
C      READ (H)*(CH) I 3940
243      READ (NTAPE7)NSIZEF, L, ((A(I,J), I=1,NSIZE), J=1,L) 3950
C*****          3960
C      COMPUTE (M BAR) =((H)+RHO*RR**2*S*(H)*(CH)) I 3970
DO 228 I=1,NSIZE 3980
DO 228 J=1,L,NCX 3990
K=J/2+1          4000
A(I,J)=CON*A(I,J)+F(I,K) 4010
228 A(I,J+1)=CON*A(I,J+1) 4020
C*****          4030
C READ FIXIBILITY MATRIX FOR SURFACE 4040
231 READ (NTAPE5)NSIZEF, NSIZE, ((F(I,J), I=1,NSIZE), J=1,NSIZE) 4050
K=NC*K1+1        4060
CALL MMULTD (F,0,A,NC-1,U(K1+1:K),NSIZE,NSIZE,NSIZE,MAXR,MAXR) 4070
1               4080
IF ( NRIGID )    232,246,232 4090
C*****          4100
C FIND ( LITTLE M BAR ) = (DELTAM) + (H R)TRANSPOSED * (( BAR ) * (H R)) 4110
232 DO 240 I=1,NSIZE 4120
K=K1+1          4130
DO 240 J=1,NRIGID 4140
G(J,I)=HR(K,J) 4150
240 K=NC*K1+1    4160
CALL MMULTD (G,0,A,NC-1,HRT(1,K),NRIGID,NSIZE,NSIZE,MAXU,MAXR) 4170
1               4180
CALL MMULTD (HRT(1,K),NC-1,HR(K1+1,1),U,A,NRIGID,NSIZE,NRIGID, 4190
1               4200
MAXQ,MAXS,MAXR) 4210
DO 244 I=1,NRIGID 4220
DO 244 J=1,NR2 4230
244 BARMRR(I,J)=BARMRR(I,J)+A(I,J) 4240
246 K1=K1+NSIZE 4250
L=NC*NPOINT     4260
IF ( NRIGID )    247,268,247 4270
247 GOTO (252,248),NC 4280
248 DO 250 I=1,NRIGID 4290
DO 250 J=1,NR2,NCX 4300
K=J/2+1          4310
G(I,K)=BARMRR(I,J+1) 4320
250 BARMRR(I,K)=BARMRR(I,J) 4330
C*****          4340
C THEN (LITTLE M BAR) INVERSE AND FINAL U MATRIX STORED ON NTAPE9. 4350
252 CALL MNVRSX (BARMRR,G,A(1,1), A(1,MAXQ),NRIGID,IR,NC-1) 4360
1               4370
254 GOTO (260,256),NCX 4380
256 DO 258 I=1,NRIGID 4390
DO 258 J=1,NR2,NCX 4400
K=NR2-J          4410
M=K/2+1          4420
BARMRR(I,K)=BARMRR(I,M) 4430
258 BARMRR(I,K+1)=G(I,M) 4440
260 CALL MMULTD (BARMRR,NC-1,HRT,NC-1,F,NRIGID,NRIGID,POINT, 4450
1               4460
MAXQ,MAXQ,MAXR) 4470
CALL MMULTD (F,NC-1,U,NC-1,HRT,NRIGID,NPOINT,NPOINT,MAXR,MAXR) 4480
1               4490
CALL MMULTD (HR,1,F,NC-1,A,NPOINT,NRIGID,NPOINT,MAXS,MAXR,MAXR)
DO 264 I=1,NPOINT
DO 262 J=1,1
F(I,J)=U(I,J)
```

```

262      A(I,J)=-A(I,J)          4500-
      K=I+NC-NC+1
264      A(I,K)=1.0+A(I,K)      4510-
      CALL MMULTD (A,NC-1,F,NC-1,U,NPOINT,NPOINT,NPOINT,MAXR,MAXR,MAXR)
      IF ( NAERO )           268,266,268  4520-
      4530-
      4540-
      4550-
      4560-
      4570-
      4580-
      4590-
      4600-
      4610-
      4620-
      4630-
      4640-
      4650-
      4660-
      4670-
      4680-
      4690-
      4700-
      4710-
      4720-
      4730-
      4740-
      4750-
      4760-
      4770-
      4780-
      4790-
      4800-
      4810-
      4820-
      4830-
      4840-
      4850-
      4860-
      4870-
      4880-
      4890-
      4900-
      4910-
      4920-
      4930-
      4940-
      5000-
      5010-
      5020-
      5030-
      5040-
      5050-
      5060-
      5070-
      5080-
      5090-
      5100-
      5110-
      5120-
      5130-
      5140-
266 READ (NTAPE5)A(1,1)
      WRITE (NTAPE5)((HRT(I,J),I=1,NRIGID),J=1,NPOINT)
268 WRITE (NTAPE9)NPOINT, L, ((U(I,J),I=1,NPOINT),J=1,L)
300 CONTINUE
      REWIND NTAPE5
      REWIND NTAPE6
      REWIND NTAPE7
      REWIND NTAPE8
      REWIND NTAPE9
      KPART = 2
      RETURN
310 WRITE (NTAPE3,20)
      GOTO 991
320 REWIND NTAPE4
      REWIND NTAPE5
      IF ( NRIGID )           330,332,330  4700-
      4710-
      4720-
      4730-
      4740-
      4750-
      4760-
      4770-
      4780-
      4790-
      4800-
      4810-
      4820-
      4830-
      4840-
      4850-
      4860-
      4870-
      4880-
      4890-
      4900-
      4910-
      4920-
      4930-
      4940-
      5000-
      5010-
      5020-
      5030-
      5040-
      5050-
      5060-
      5070-
      5080-
      5090-
      5100-
      5110-
      5120-
      5130-
      5140-
330 READ (NTAPE5)I,I, A(I,J)
332 K1=1
      DO 334 I=1,NPOINT
      DO 334 J=1,NPOINT
334 F(I,J)=0.0
      DO 336 ISUR=1,NSUR
      K2=K1+NSIZFS(ISUR)-1
      READ (NTAPE5)I,I, A(I,J)
      READ (NTAPE4)NSIZE, NSIZE, ((F(I,J),I=K1,K2),J=K1,K2)
336 K1=K1+NSIZF
      READ (NTAPE4)NSIZE, MODE, ((A(I,J),I=1,NSIZE),J=1,MODE)
      M=MODE/NC
      CALL MMULTD (F,0,A,NC-1,U,NPOINT,NPOINT,M,MAXR,MAXR,MAXR)
      IF ( NDELM )           337,348,337
      337 IF ( NRIGID )           338,348,338
      338 READ (NTAPE5)((DM(I,J),I=1,NRIGID),J=1,NRIGID)
      READ (NTAPE5)((G(I,J),I=1,NRIGID),J=1,NPOINT)
      DO 339 I=1,NRIGID
      DO 339 J=1,NPOINT
339 G(I,J)=-G(I,J)
      CALL MMULTD (G,0,A,0,HRT,NRIGID,NPOINT,M,MAXQ,MAXR,MAXQ)
      READ (NTAPE4) (HR(I,1),I=1,M)
      DO 340 I=1,M
      DO 340 J=1,NRIGID
340 G(J,I)= HRT(J,I)/HR(I,1)
      WRITE (NTAPE3,25)
      CALL MPRINT (G,NRIGID,M,MAXQ,NTAPE3)
      IF ( NPUNCH )           343,345,343
      343 WRITE (NTAPE4,26)NRIGID, M, RCDZ, NCARDS
      NCARD = NCARDS+1
      CALL MPUNCH ( G,NRIGID,M,0,1,1,RCDZ,MAXQ,NTAPE4,NCARD)
      WRITE (NTAPE4,27)RCDZ, NCARDS, RCDZ, NCARD
      NCARDS=NCARD+1
      345 CONTINUE
      CALL MMULTD (DM,0,G,0,HRT,NRIGID,NRIGID,M,MAXQ,MAXQ,MAXQ)
      DO 346 I=1,NRIGID
      DO 346 J=1,MODE
346 HR(J,I)= G(I,J)
      DO 350 I=1,NPOINT
      DO 350 J=1,MODE

```

```

350   F(J,I)=A(I,J)          5150
      CALL MMULTD (F,0,U,0,A,M,NPOINT,M,MAXR,MAXR,MAXR)
      IF ( NDELM )            352,358,352 5160
      5170
352   IF ( NRIGID )         354,358,354 5180
354   CALL MMULTD (HR,0,HRT,0,F,M,NRIGID,M,MAXR,MAXQ,MAXR,
      DO 356 I=1,MDNF       5190
      5200
      DO 356 J=1,M           5210
      5220
356   A(J,I) = A(J,I) + F(J,I) 5230
358   WRITE (NTAPE3,24) ( I, A(I,I), I=1,M) 5240
      GOTO 991
      END
      FORTRAN LSTOU.DCK 5260

C MREAD
C MREAD
C MATRIX READ SUBROUTINE
      CALL MREAD (A,M,N,IFORM,IROW,ITRA,IORG,T,MD,NTAPE2,NTAPE3)
      M0010
      M0020
      M0030
      M0040
      M0050
      M0060
      M0070
      M0080
      M0090
      M0100
      M0110
      M0120
      M0130
      M0140
      M0150
      M0160
      M0170
      M0180
      M0190
      M0195
      M0200
      M0210
      M0220
      M0230
      M0240
      M0250
      M0260
      M0270
      M0280
      M0290
      M0300
      M0310
      M0320
      M0330
      M0340
      M0350
      M0360
      M0370
      M0380
      M0390
      M0400
      M0402
      M0404
      M0406
      M0410
      M0415
      M0420
      M0430
      M0440

      A = MATRIX TO READ IN      ITRA = 0, TRA CARD AFTER MATRIX
      M = NUMBER OF ROWS          =+1, .VA CARD AFTER EACH ROW
      N = NUMBER OF COLUMNS        (OR COLUMN)
      IFORM = -1, FORMAT(12A6)    IORG = ORIGIN OF FIRST C.R. CARD
      = 0, COLUMN BINARY          T = MDXN TEMPORARY CELLS
      = +1, FORMAT(6E12.8)        MD = DIMENSIONED NUMBER OF ROWS
      IRONW = .0, MATRIX BY COLUMNS   IN A
      = +1, MATRIX BY ROWS        NTAPE2 = INPUT TAPE
      SURROUNGE MREAD (A,M,N,IFORM,IROW,ITRA,IORG,T,MD,NTAPE2,NTAPE3)
      DIMENSTION A(1), T(1)
      1 FORMAT (6E12.8)           M0140
      2 FORMAT (12A6)             M0150
      3 FORMAT ( // 26H THATS ALL YOUR DATA. ) M0160
      4 FORMAT (4E16.8)           M0170
      MN=MD*N
      DO 5 I=1,MN
      T(I)=0.0
      5 A(I)=0.0
      IF ( IFORM ) 39,15,6
      6 IF ( IRONW ) 8,/,8
      7 K3=1
      K4=N
      K5=MD
      K6=M-1
      K7=1
      GOTO 9
      R K2=MN
      K3=MD
      K4=M
      K5=1
      K6=0
      9 DO 11 I=1,K4
      K1=I*K5-K6+1
      IF ( K6 ) 10,111,10
      10 K2=K1+K6
      111 IF ( IFORM = 1 ) 39,110,109
      109 READ (NTAPE2,1) (A(L),L = K1,K2,K3)
      GO TO 11
      110 READ (NTAPE2,1)(A(L),L=K1,K2,K3)
      11 CONTINUE
      GOTO 36
      15 K1=N
      K2=M

```

K3=1	M0450
IF ( IORG-1 ) 16,17,17	M0460
16 K3=2	M0470
17 IF ( IR0W ) 18,19,18	M0480
18 K2=N	M0490
K1=M	M0500
19 IF ( ITRA ) 22,21,22	M0510
21 K1=1	M0520
22 K=0	M0530
DO 23 I=1,K1	M0540
K4=K+K3	M0550
K5=1	M0560
CALL RINRD (T(K4), K5, L, NTAPE2, NTAPE3 )	M0570
GOTO (23,38,23,23),I	M0580
23 K=K+K2	M0590
IF ( IR0W ) 28,24,28	M0600
24 L=0	M0610
IF ( IORG-1 ) 26,26,26	M0620
25 L=IORG-1	M0630
26 DO 27 I=1,N	M0640
J=I*MD-MD	M0650
DO 27 K=1,M	M0660
J=J+1	M0670
L=L+1	M0680
A(J)=T(L)	M0690
GOTO 36	M0700
28 L=0	M0710
IF ( IORG-1 ) 30,30,29	M0720
29 L=IORG-1	M0730
30 DO 31 K=1,N	M0740
J= K*MD-MD	M0750
DO 31 I=K,MN,N	M0760
J=J+1	M0770
K1=L+1	M0780
A(J)=T(K1)	M0790
36 RFTHRN	M0800
38 WRTTF (NTAPE3,3)	M0810
STOP	M0820
39 READ (NTAPE2,2)(A(I),I=1,M)	M0840
GOTO 36	M0850
FND	M0860
FORTRAN 'S10H,DECK	
C RINRD	
SUBROUTINE RINRD (T,K,L,NTAPE1,NTAPE2)	0010
DIMENSION T(1)	0020
RETURN	0030
FND	0040
FORTRAN LS10H,DECK	
C RDIN	
SUBROUTINE RDIN (NTAPE2, NTAPE3, I )	0010
1 FORMAT(8HH	0020
1 )	0030
2 FORMAT(1H1)	0040
3 FORMAT ( 1H0 )	0050
READ (NTAPE2,1)	0060
GOTO (4,5),I	0070
4 WRITE (NTAPE3,2)	0080
GOTO 6	0090
5 WRITE (NTAPE3,3)	0100
6 WRITE (NTAPE3,1)	0110
RETURN	0120

```

END 0130
FORTRAN LSTOU.DECK
C MMULTD 0010
SUBROUTINE MMULTD (A,N1,B,N2,C,M,N,K,MA,MR,MC)
DIMENSION A(1), B(1), C(1) 0020
      IC=1 0040
      IA=MC*K 0050
      IB=MA*N 0060
      ID=M 0070
      IH=MC 0080
      IJ=MC 0090
      IF ( N1 ) 4,3,4 0100
3     IF ( N2 ) 1,4,7 0110
4     IB=2*IB 0120
      ID=2*ID 0130
      IF ( N2 ) 5,6,5 0140
5     IC=2 0150
      GOTO 7 0160
6     IH=2*IH 0170
      IC=3 0180
7     IA=2*IA 0190
      IJ=2*IJ 0200
8     DO 18 I=1,M 0210
      INC=0 0220
      DO 11 J=1,IA,IH 0230
        C(J)=0.0 0240
        IN=INC 0250
        DO 10 L=I,IB,ID 0260
          IN=IN+1 0270
          C(J)=C(J)+A(L)*B(IN) 0280
10    INC=INC+MH 0290
      INC=0 0300
      GOTO (18,12,15),IC 0310
12   DO 14 J=1,IA,IJ 0320
      IF=I+MA 0330
      IF=J+MC 0340
      IN=INC 0350
      DO 13 L=IF,IB,ID 0360
        IN=IN+1 0370
        IG=IN+MR 0380
        C(IF)=C(IF)+A(L)*B(IN) 0390
13    C(J)=C(J)-A(L)*B(IG) 0400
14    INC=INC+MR *2 0410
      GOTO 18 0420
15   IF=I+MC 0430
      IF=I+MA 0440
      DO 17 J=IF,IA,IJ 0450
        IN=INC 0460
        C(J)=0.0 0470
        DO 16 L=IF,IB,ID 0480
          IN=IN+1 0490
          C(J)=C(J)+A(L)*B(IN) 0500
16    INC=INC+MH 0510
18   CONTINUE 0520
      RETURN 0530
END 0540
FORTRAN LSTOU.DECK
C MNVRSX 0010
SUBROUTINE MNVRSX (AR,A1,R,C,KSZ,1GOOFD,NOP) 0020
DIMENSION AR(6,6), A1(6,6), R(6,6), C(6,6) 0040
1GOOFD=0

```

```

      IF ( NOP )      10-,101,102          0050
101  CALL INVERS (AR,KSZ,IGOJFD)        0060
      GO TO 20          0070
102  CONTINUE          0080
      DO 1 K=1,KSZ          0090
      DO 1 L=1,KSZ          0100
1     R(K,L)=AR(K,I)          0110
      NO=0          0120
      CALL INVERS(R,KSZ,NO)          0130
      IF (NO) 2,3,?          0140
C  REAL MATRIX NOT SINGULAR          0150
C  MULT R*AI  STO. C          0160
3     DO 4 K=1,KSZ          0170
      DO 4 L=1,KSZ          0180
      C(K,L)=0.0          0190
      DO 4 I=1,KSZ          0200
4     C(K,L)=C(K,L)+R(K,I)*AI(I,L)          0210
C  MULT. AI*C + AR  STO. R          0220
      DO 5 K=1,KSZ          0230
      DO 5 L=1,KSZ          0240
      R(K,L)=AR(K,I)          0250
      DO 5 I=1,KSZ          0260
5     R(K,L)=R(K,I)+AI(K,I)*C(I,L)          0270
      NO=0          0280
      CALL INVERS(R,KSZ,NO)          0290
      IF (NO) 2,7,?          0300
C  SECOND MATRIX NOT SINGULAR          0310
C  MULT. -C*R  STO. AI      ALSO SET AR=B          0320
7     DO 8 K=1,KSZ          0330
      DO 8 L=1,KSZ          0340
      AI(K,L)=0.0          0350
      AR(K,L)=B(K,L)          0360
      DO 8 I=1,KSZ          0370
8     AI(K,L)=AI(K,L)-C(K,I)*B(I,L)          0380
      GO TO 20          0390
C  REAL MATRIX OR SECOND MATRIX SINGULAR    TRY IMAG. ROUTE
2     DO 9 K=1,KSZ          0400
      DO 9 L=1,KSZ          0410
9     R(K,L)=AI(K,L)          0420
      NO=0          0430
      CALL INVERS(R,KSZ,NO)          0440
      IF (NO) 10,11,10          0450
C  IMAG. NOT SINGULAR          0460
C  MULT. R*AR  STO. C          0470
11    DO 12 K=1,KSZ          0480
      DO 12 L=1,KSZ          0490
      C(K,L)=0.0          0500
      DO 12 I=1,KSZ          0510
12    C(K,I)=C(K,I)+R(K,I)*AR(I,L)          0520
C  MULT. AR*C+AI  STO R          0530
      DO 13 K=1,KSZ          0540
      DO 13 L=1,KSZ          0550
      R(K,L)=AI(K,I)          0560
      DO 13 I=1,KSZ          0570
13    R(K,I)=R(K,I)+AR(K,I)*C(I,L)          0580
      NO=0          0590
      CALL INVERS(R,KSZ,NO)          0600
      IF (NO) 10,15,10          0610
C  THIRD MATRIX NOT SINGULAR          0620
C  MULT -C*B  STO AR      ALSO SET AI=-R          0630
15    DO 16 K=1,KSZ          0640

```

```

DO 16 L=1,KSZ
AR(K,L)=0
A1(K,L)=-R(K,L)
DO 16 I=1,KSZ
AR(K,L)=AR(K,L)+C(K,I)*R(I,L)
DO TO 20
I GOOF D=1
20 RETURN
END

```

FORTRAN LSTOU, DFCK

INVERS

```

SUBROUTINE INVERS (A,N,I GOOF D)
DIMENSTON A(4,4), L(6), M(6)
CALL OVRFL (K000FX)
GO TO(500,500),K000FX
500 CALL OVRFL (K000FX)
GO TO(501,501),K000FX
501 CALL UVCHK (K000FX)
GO TO(502,502),K000FX
502 IG00FD=0

```

SEARCH FOR LARGEST ELEMENT

```

DO 80 K=1,N
L(K)=K
M(K)=K
RIGA=A(K,K)
DO 20 I=K,N
DO 20 J=K,N
IF(ABS(RIGA)-ABS(A(I,J)))10,20,20
RIGA=A(I,J)

```

L(K)=I

M(K)=J

CONTINUE

INTERCHANGE ROWS

```

JROW=L(K)
IF(I(K)=K)35,55,20
DO 40 I=1,N
HOLD=-A(K,I)

```

A(K,I)=A(JROW,I)

A(JROW,I)=HOLD

INTERCHANGE COLUMNS

```

ICOL=M(K)
IF(M(K)=K)45,45,37
DO 40 J=1,N
HOLD=-A(I,K)

```

A(I,K)=A(J,ICOL)

A(J,ICOL)=HOLD

DIVIDE COLUMN BY MINUS PIVOT

DO 45 IC=1,N

IF(IC-K)50,55,50

A(IC,K)=A(IC,K)/(-A(K,K))

CONTINUE

REDUCE MATRIX

DO 65 I=1,N

DO 65 J=1,N

IF(I-K)57,65,57

57 IF(J-K)60,65,60

60 A(I,J)=A(I,K)\*A(K,J)+A(I,J)

CONTINUE

DIVIDE ROW BY PIVOT

DO 75 JR=1,N

IF(JR-K)70,75,70

0660  
0670  
0680  
0690  
0700  
0710  
0720  
0730  
0740  
0010  
0020  
0040  
0050  
0060  
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0080  
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0270  
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0290  
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0480  
0490  
0500  
0510

```

71 A(K,JR)=A(K,JR)/A(K,K)          0520
75 CONTINUE                         0530
C CONTINUED PRODUCT OF PIVOTS      0540
C REPLACE PIVOT BY RECIPROCAL     0550
C A(K,K)=1.0/A(K,K)               0560
C CONTINUE COMPLETE OPERATION    0570
80 CONTINUE                         0580
CALL DVCHK (K000FX)                0590
GO TO(510,503),K000FX             0600
503 CALL OVERFL(K000FX)              0610
GO TO(510,504),K000FX             0620
504 CALL OVERFL(K000FX)              0630
GO TO(510,505),K000FX             0640
C FINAL ROW AND COLUMN INTERCHANGE 0650
505 K=N                            0660
100 K=(K-1)                         0670
IF(K)150,150,103                 0680
101 I=I (K)                        0690
IF(I-K)120,120,105                 0700
105 DO 110 J=1,N                  0710
HOLD=A(J,K)                      0720
A(J,K)=-A(J,I)                   0730
110 A(J,I)=HOLD                   0740
120 J=M(K)                         0750
IF(J-K)100,100,125                 0760
125 DO 130 I=1,N                  0770
HOLD=A(K,I)                      0780
A(K,I)=-A(J,I)                   0790
130 A(J,I)=HOLD                   0800
GO TO 100                          0810
150 RETURN                         0820
510 1 GOOF D=1                     0830
GO TO 150                          0840
END                               0850
E LINK    PARPTT,PAR1TT           0010
E FORTRAN LSTOU,DFCK             0020
C PART?                           0030
SURROUNGE PART?                  0040
C PART.... VIBRATION AND FLUTTER ANALYSIS BY A COLLOCATION METHOD. 0050
DIMENSION IT(219),VFLCTY(20),NSIZES(20),DM(6,6),RHO(70)
COMMON//1/ U(49,196),QUFSS(49,2),H(49,50),EIG(50),
1 TEMP(2/34),NAKSR(25),NAKDR(25),NITER(75), 0060
2 OMEGA(25),DAMP(25),VELC(25)        0070
C THE FOLLOWING STATEMENT(S) HAVE BEEN MANUFACTURED BY THE TRANSLATOR TO 0080
C COMPENSATE FOR THE FACT THAT EQUIVALENCE DOES NOT REORDER COMMON-- 0090
COMMON IT                           0100
EQUIVALENCE (IT(1),ISXST), (IT(2),ISH), (IT(41),RH0),
1 (IT(61),NTAPE1), (IT(62),NTAPE2), (IT(63),NTAPE3),
2 (IT(64),NTAPE4), (IT(65),NTAPE5), (IT(66),NTAPE6), 0110
3 (IT(67),NTAPE7), (IT(68),NTAPE8), (IT(69),NTAPE9), 0120
4 (IT(70),NSUR), (IT(71),NRIGID), (IT(72),HREF), 0130
5 (IT(73),NAFRO), (IT(74),NFUS), (IT(75),NDENS), 0140
6 (IT(76),MODES), (IT(77),NPOINT), (IT(78),NPINCH), 0150
7 (IT(79),MAXR), (IT(80),MAXQ), (IT(81),MAXS), 0160
8 (IT(82),NC), (IT(83),NSURFS), (IT(84),NP2), 0170
9 (IT(85),HR), (IT(106),S)          0180
EQUIVALENCE (IT(12),VFLCTY), (IT(14),NTAPE0), (IT(148),NRHO), 0190
1 (IT(149),NITRSP), (IT(150),NITRDP), (IT(151),EPSP), 0200
2 (IT(152),FPDP), (IT(153),PICON), (IT(154),NVEL), 0210
3 (IT(155),NCARDS), (IT(156),AITKEN), (IT(157),NGO), 0220
4 (IT(158),FK), (IT(159),SORCON), (IT(160),NSIZES), 0230
                                         0240
                                         0250
                                         0260
                                         0270
                                         0280
                                         0290

```

```

6      (IT(180),DM),(IT(217),AITKED),(IT(218),KPART) 031
200 FORMAT (1H1 4BX, 12H OUTPUT DATA // 1H 11X, 5H FLUTTER 0320
1      52H ANALYSIS BY A COLLOCATION ME,HOD, USING AERODYNAMIC 0330
2      24H INFLUENCE COEFFICIENTS // 1H0 14X, 11H DENSITY = 0340
3      1E20.R, 5X, 20H REDUCED VELOCITY = 1E20.R, // 1H0 33X, 0350
4      116, 32H RIGID BODY DEGREES OF FREEDOM // / / / ) 0360

201 FORMAT (1H1 20X, 5H MODE 7X, 12H OMEGA (CPS) 10X, 6H DAMPING 0370
1      4X, 17H VELOCITY (KNOTS) // ( 1H 2-X, 114, 0380
2      3F20.8 ) 0390
202 FORMAT ( 214, 62X, 1A6, 114 ) 0400
203 FORMAT ( 1H0 34X, 23H PUNCHED CARDS NUMBERS 1A6, 114, 6H THRU 0410
1      1A6, 114 ) 0420
204 FORMAT (1H1 45X, 16H DYNAMIC MATRIX ) 0430
205 FORMAT (51H FLEXIBLE MODE SHAPES, SURFACE 114 ) 0440
206 FORMAT (5H MODE 116, 32H, GIVES AN IMAGINARY FREQUENCY. ) 0450
DATA QAHACT/02020.30440005/
RC02=00000CT
NVFL=NVEL
MAXP=49
K=NC+NPOINT
DO 290 I=1,NPOINT
  DO 290 J=1,K
290  U(I,J)=0.0
REWIND NTAPF9
DO 314 IRHO=1,NRHO
  MODE=MODES
  READ (NTAPF9)NSIZE, NSIZE?, ((U(I,J),I=1,NSIZE),
1      J=1,NSIZE?) 0570
  IF ( NPUNCH )      302,304,304
302  WRTTF (NTAPE1,204)
  CALL MPRINT (U,NPOINT,K,MAXP,NTAPE1)
304  WRTTF (NTAPE1,200)RH0(IRHO), VELCTY(NVEL), NRIGID
  DO 305 I=1,MODE
    NAKDR(I)=0
  305  NAKSR(I)=0
    CALL MITERS (U,GUESS,0 ,NPOINT,MODE ,MAXP ,NC ,EPSP ,
1      FPDP ,NAKSR ,NAKDR ,NITRSP,NITRDP,AITKE,AITKED,
2      IR ,TEMP ,H ,EIG ,NITER ,NTAPE0,NTAPE3) 0660
    IF ( NAFRO )      3055,3054,3055
3054  WRTTF (NTAPF4) NPOINT, MODE, ((H(I,J),I=1,NPOINT);J=1,MODE) 0700
  WRTTF (NTAPF4) (EIG(I),I=1,MODE),NPOINT,MODE,NPOINT,MODE,MODE 0710
3055  CONTINUE
  MODES2 = NC*MODE
  DO 310 I=1,MODES2,NC
    K=I/NC + NC -1
    IF ( EIG(I))      3051,3052,3052
3051  WRTTF (NTAPE1,206)K
  OMFGA(K)=0.0
  GOTO 3053
3052  OMFGA(K)= SORCON / ( SORT( FK*FIG(I)) )
3053  GOTO (306,308),NC
  306  DAMP(K)=0.0
    VELC(K)=0.0
    GOTO 310
308  DAMP(K)= FIG(I+1) / FIG(I)
    VELC(K)= PIICON*OMFGA(K)*RRFF* VELCTY(NVEL)
310  CONTINUE
  WRTTF (NTAPE1,201)(K, OMEGA(K), DAMP(K), VELC(K) ,
1      K=1,MODE )
  IF ( NPUNCH )      312,314,312

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312 K1=1          0910
  WRITE (NTAPE0,202) NSIZES(1), MODES2, RCDZ, NCARDS
  NCRDS = NCARDS+1
  CALL MPUNCH (OMEGA, MODES2, 1, 0, 1, 1, RCDZ, MAXP, NTAPE0, NCRDS)
  WRITE (NTAPE0,203) RCDZ, NCARDS, RCDZ, NCRDS
  NCARDS=NCRDS+1
  DO 313 ISUR =1,NSUR          0920
    IF ( ISUR-1 )           3121,3122,3121          0930
 3121 WRITE (NTAPE0,202) NSIZES(ISUR), MODES2, RCDZ, NCARDS
  NCRDS=NCARDS+1
  GO TO 3123          0940
 3122 NCARDS=NCARDS          0950
 3123 CALL MPUNCH (H(K1,1),NSIZES(ISUR), MODES2, 0, 1, 1, RCDZ, MAXP, NTAPE0,
    1           NCRDS )
  WRITE (NTAPE0,205) ISUR          0960
  WRITE (NTAPE0,203) RCDZ, NCARDS, RCDZ, NCRDS
  NCARDS=NCRDS+1          0970
 313 K1=K1+NSIZES(ISUR)          0980
 314 CONTINUE          0990
  REWIND NTAPE0          1000
  NGO = 98765          1010
  KPART = 1          1020
  RETURN          1030
  END          1040
  FCTRAN LSTOU,DFCK          1050
C NORM7          1060
  SUBROUTINE NORM (A,H,N,C,INDFX,MAXR,NC,np)          1070
  DIMENSION A(1), H(1), C(1), T(2)          1080,200,200
  IF ( INDEX )          108,200,200
  100 GO TO (110,140),NP          1090
  110 GO TO (500,120),NC          1100
  120 RIG = C(1)**2+C(2)**2          1110
  GO TO 600          1120
  140 CALL DNORM (A,R,N,C,MAXR,NC,T)
  GO TO 700          1130
  200 INDEX=1          1140
  NSTART=NP+1
  NSTOP=N+NP
  K=NP*MAXR
  IF ( NSTART-NSTOP )          1150
  205 GO TO ( ,0,500),NC          1160
  210 RIG=ABS A(1))
  DO 230 I=NSTART,NSTOP,np          1170
  IF ( RIG=ABS(A(1)) )          205,205,400
  220 INDEX=1          205,205,400
  RIG=ABS(A(1)))
  230 CONTINUE          205,205,400
  GO TO 400          205,205,400
  300 RIG = A(1)**2 + A(K+1)**2          205,205,400
  DO 310 I=NSTART,NSTOP,np          205,205,400
  J=K+1
  IF ( RIG-(A(1)**2+A(J)**2) )          205,205,400
  320 RIG = A(1)**2 + A(J)**2,
  INDEX = 1          205,205,400
  330 CONTINUE          205,205,400
  400 J=NP*NC          205,205,400
  I=INDFX+(NC-1)*K+(NP-1)
  C(J)=A(1)
  J=J+(NP-1)
  I=I-(NP-1)
  C(J)=A(1)
  MTR40002
  MTR40004
  MTR40006
  MTR40007
  MTR40008
  MTR40009
  MTR40010
  MTR40012
  MTR40013
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  MTR40045

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I=INDEX+(NP-1)          MTR40046
C(NP)=A(I)              MTR40047
C(1)=A(INDEX)           MTR40048
GO TO (410,140),NP      MTR40050
410 GO TO (500,600),NC   MTR40051
500 DO 510 I=1,N         MTR40053
510 R(I)=A(I)/C(1)       MTR40054
GO TO 700                MTR40055
600 BIG = C(1)**2+C(2)**2 MTR40057
DO 610 I=1,N             MTR40058
J=I+MAXR                 MTR40060
T= A(I)*C(1)+A(J)*C(2)  MTR40061
R(J) = ( A(J)*C(1)-A(I)*C(2) ) / BIG MTR40062
510 R(I)= T/BIG          MTR40063
700 INDEX = INDEX/NP +NP-1 MTR40064
RETURN                   MTR40065
END                      MTR40067

FORTRAN LSTOU,DECK

C DNORMZ
SUBROUTINE DNORM (A,B,N,C,MAXR,NC,T)
DOUBLE PRECISION A(1), B(1),C(1),T(1)          MTR40069
410 GO TO (500,600),NC   MTR40071
500 DO 510 I=1,N         MTR40072
510 R(I)=A(I)/C(1)       MTR40074
GO TO 700                MTR40075
600 BIG=C(1)*C(1) + C(2)*C(2) MTR40076
DO 610 I=1,N             MTR40078
J=I+MAXR                 MTR40079
T= A(I)*C(1)+A(J)*C(2)  MTR40080
R(J) = ( A(J)*C(1)-A(I)*C(2) ) / BIG MTR40081
610 R(I)= T/BIG          MTR40082
700 RETURN                MTR40083
END                      MTR40084
MTR40086

FORTRAN LSTOU,DECK

C POHS
SUBROUTINE POH (LMBDN,LMRD1,LMRD2,HN,HN1,H1,H2,N,NC) MTR40089
DIMENSION LMBDN(), LMRD1(), LMRD2(), HN(), HN1(), H1(), H2() MTR40091
1          H2(), A()
DOUBLE PRECISION LMBDN, LMBD1, LMRD2, HN, HN1, H1, H2, A MTR40092
GO TO (200,100),NC        MTR40093
210 DO 210 I=1,N          MTR40095
K=I+N                  MTR40097
A(1) = LMBDN(1)*HN(I)-LMRDN(2)*HN(K) MTR40101
A(2) = LMBDN(1)*HN(K)+LMRDN(2)*HN(I) MTR40102
H1(I) = LMRD2(1)*HN1(I)-LMRD2(2)*HN1(K)-A(1) MTR40104
H1(K) = LMRD2(1)*HN1(K)+LMRD2(2)*HN1(I)-A(2) MTR40105
H2(I) = A(1)-LMRD1(1)*HN1(I)+LMRD1(2)*HN1(K) MTR40107
H2(K) = A(2)-LMRD1(1)*HN1(K)-LMRD1(2)*HN1(I) MTR40108
210 RETURN                MTR40110
200 DO 210 I=1,N          MTR40112
A(1) = LMBDN(1)*HN(I) MTR40114
H1(I) = LMRD2(1)*HN1(I)-A(1) MTR40116
210 H2(I) = A(1)-LMRD1*HN1(I) MTR40117
RETURN                  MTR40119
END                      MTR40121

FORTRAN LSTOU,DECK

C AITKNS
SUBROUTINE AITKNS (HN,HN1,HN2,HNEW,R,N,MAXR,NC,np,IR) MTR40123
DIMENSION HN(), HN1(), HN2(), HNEW(), A(2), B(4), C(2), D(2) MTR40125
IR=0                     MTR40127
L=NP*N                  MTR40129

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```

C(1) = R**2
    DO 110 I=1,1,NP
        R(1) = 0
        R(2) = 0
        DO 100 J=1,NC
            K=(J-1)*MAXR+1
            D(1) = H(1) + (HN1(K)-HN2(K))**2
            D(2) = D(2) + (HN(K)-HN1(K))**2
            IF ( D(1) ) 105,110,105
105    CONTINUE
            IF ( D(2)/D(1) = C(1) ) 110,110,801
110    CONTINUE
        GO TO (300,200),NP
200    CALL ALTKND (HN,HN1,HN2,HNEW,N,MAXR,NC,A,B,C,D)
        GO TO 700
300    DO 600 I=1,N
        GO TO (400,500),NC
400    C(1) = HN(I)-2.*HN1(I)+HN2(I)
        IF ( C(1) ) 410,600,410
410    HNFH(I) = HN2(I) - ( (HN1(I)-HN2(I))**2 / C(1) )
        GO TO 600
500    A(1) = 0.
        C(1) = 2.
        D(1) = 0.
        DO 510 J=1,2
            K = I+(J-1)*MAXR
            R(J) = HN(K)-2.*HN1(K)+HN2(K)
            C = C*(HN1(K)-HN2(K))
            A = -(HN1(K)-HN2(K))**2 -A
            D = R(J)**2 +D
            IF ( D ) 520,600,520
520    HNFH(I) = HN2(I) - ( R(1)*A(1)+R(2)*C(1) ) / D(1)
            HNFH(K) = HN2(K) - ( R(1)*C(1)-R(2)*A(1) ) / D(1)
530    CONTINUE
710    IR = 1
900    RETURN
END
FORTRAN LSTOII.DCK
C ALTKND
    SUBROUTINE ALTKND (HN,HN1,HN2,HNFH,N,MAXR,NC,A,B,C,D)
    DIMENSION HN(1), HN1(1), HN2(1),HNEW(1), A(1), B(2), C(1), D(1)
    DOUBLE PRECISION HN, HN1, HN2, HNEW, A, B, C, D
300    DO 600 I=1,N
        GO TO (400,500),NC
400    C(1) = HN(I)-2.*HN1(I)+HN2(I)
        IF ( ABS(C(1)) = .0000000100 ) 600,600,410
410    HNFH(I) = HN2(I) - ( (HN1(I)-HN2(I))*(HN1(I)-HN2(I)) / C(1) )
        GO TO 600
500    A(1) = 0.
        C(1) = 2.
        D(1) = 0.
        DO 510 J=1,2
            K = I+(J-1)*MAXR
            R(J) = HN(K)-2.*HN1(K)+HN2(K)
            C = C*(HN1(K)-HN2(K))
            A = -( (HN1(K)-HN2(K))*(HN1(K)-HN2(K)) ) - A
            D = R(J)*R(J) + D
            IF ( D ) 520,600,520
520    HNFH(I) = HN2(I) - ( R(1)*A(1)+R(2)*C(1) ) / D(1)
            HNFH(K) = HN2(K) - ( R(1)*C(1)-R(2)*A(1) ) / D(1)
600    CONTINUE

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700 1R = 1          MTR40215
800 RETURN          MTR40217
FND          MTR40219
$   FORTRAN LST011.DECK
C LEGISS
  SUBROUTINE LEGISS (LAMRDA, POS, E1, E2, NC, IR)
  DIMENSION LAMRDA(1), POS(1)
  DOUBLE PRECISION LAMRDA, POS, R1, R2A, R2B
  IR=0
  GO TO (100,200),NC
100 R1 = ( DABS( LAMRDA(1)-LAMRDA(2) ) ) / E1      MTR40222
    R2A = DAHS( DABS(POS(2)/POS(1))-1. ) / E2      MTR40224
    R2B = DAHS( DAHS(POS(4)/POS(1))-1. ) / E2      MTR40225
    CALL MPRINT (R1,2,1,2,6)                          MTR40227
    CALL MPRINT (R2A,2,1,2,6)                         MTR40229
    CALL MPRINT (R2B,2,1,2,6)                         MTR40231
110 IF ( R1-R2A )           120,140,140          MTR40232
120 IF ( R1-R2B )           130,140,140          MTR40233
130 IR=NC                  MTR40234
140 RETURN                 MTR40235
200 R1 = DSORT( (LAMRDA(1)-LAMRDA(3))*(LAMRDA(1)-LAMRDA(2)) + (LAMRDA
1     (2)-LAMRDA(4))*(LAMRDA(2)-LAMRDA(4)) ) / F1      MTR40236
1     P2A = DABS( DSORT( ((POS(3)*POS(1)+POS(2)*POS(4))*(P+S(1)*POS(1) + MTR40241
1     POS(2)*POS(4)) + (POS(3)*POS(2)-POS(4)*POS(1))*(POS(3)*
2     POS(2)-POS(4)*POS(1)) ) / (POS(1)*POS(1)+POS(2)*POS(2)) )      MTR40243
3     -L. ) / F2      MTR40244
    R2R = DARS( DSORT( ( (POS(7)*POS(5)+POS(6)*POS(8)) / (POS(5)*POS      MTR40245
1     (5) + POS(6)*POS(6)) )*( (POS(7)*POS(5)+POS(6)*POS(8)) /      MTR40246
2     (POS(5)*POS(5) + POS(6)*POS(6)) ) + ( (POS(7)*POS(6) - POS(5)*POS(4)) / (POS(5)*POS(5) + POS(6)*POS(6)) ) * ( (POS(1)*      MTR40248
4     *POS(4) - POS(3)*POS(5)) / (POS(5)*POS(5) + POS(6)*POS(6)) )      MTR40250
5     ) ) -1. ) / F2      MTR40251
    GO TO 110          MTR40253
    END          MTR40254
$   FORTRAN LST011.DECK
C MADS
  SUBROUTINE MADS (A,B,C,NSIZE,NC)          MTR40264
  DOUBLE PRECISION A(1), B(1), C(1)          MTR40265
  K=NC*NSIZE          MTR40267
  DO 100 I=1,K          MTR40269
100  C(I)=A(I)-B(I)          MTR40271
  RETURN          MTR40272
  END          MTR40273
$   FORTRAN LST011.DECK
C MMULT
  SUBROUTINE MMULT (A,R,C,LIZ,NIZ,MIZ,MAXA,MAXR,MAXC,NC,np)          MTR40275
  DIMENSION A(1), R(1), C(1)          MTR40277
  KA=NC*MAXA          MTR40279
  KB=NC*MAXR          MTR40280
  KC=NC*MAXC          MTR40281
  GO TO 200 (200,100),NP          MTR40283
100 CALL DMULT (A,R,C,LIZ,NIZ,MIZ,KA,KB,KC,NC)          MTR40285
  GO TO 700          MTR40286
200 DO 600 I=1,LIZ          MTR40288
    DO 500 M=1,MIZ          MTR40290
      K= (M-1)*KB +1          MTR40292
      I= (M-1)*KC +1          MTR40293
      C(I)=0.          MTR40295
      GO TO (300,400),NC          MTR40297
600      DO 310 N=1,NIZ          MTR40299
        J=(N-1)*KA+1          MTR40301

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      JB = (N-1)+K          MTR40302
310   C(I)=C(I)+A(J)*B(JB)  MTR40303
      GO TO 500              MTR40304
400   IC = I+MAXC          MTR40306
      C(IC) =0.               MTR40307
      DO 410 N=1,NIZ         MTR40309
        J= (N-1)*KA+L         MTR40311
        JH= (N-1) +K           MTR40312
        JC= J+MAXA             MTR40313
        JRC= JR+MAXH           MTR40314
        C(I)=C(I)+A(J)*B(JB)-A(JC)*B(JRC)  MTR40316
410   C(IC)=C(IC)+A(J)*B(JRC)+A(JC)*B(JH)  MTR40317
500   CONTINUE
600   CONTINUE
700 RETURN
END
$ FORTRAN LSTOU,DECK
C DMULTS
      SUBROUTINE DMULT (A,B,C,LIZ,MIZ,KA,KB,KC,NC)  MTR40327
      DOUBLE PRECISION A(1), B(1), C(1)  MTR40329
      MAXA=KA/2  MTR40330
      MAXR=KB/2  MTR40331
200 DO 600 L=1,LIZ  MTR40332
      DO 500 M=1,MIZ  MTR40334
        K= (M-1)*KR +1  MTR40336
        I= (M-1)*KC +L  MTR40337
        C(I)=0.  MTR40339
        GO TO (500,400),NC  MTR40341
300   DO 310 N=1,NIZ  MTR40343
        J=(N-1)*KA+L  MTR40345
        JR = (N-1)+K  MTR40346
310   C(I)=C(I)+A(J)*B(JB)  MTR40347
      GO TO 500  MTR40348
400   IC=I+KC/2  MTR40350
      C(IC) =0.  MTR40351
      DO 410 N=1,NIZ  MTR40353
        J= (N-1)*KA+L  MTR40355
        JR= (N-1) +K  MTR40356
        JC= J+MAXA  MTR40357
        JR'= JR+MAXH  MTR40358
        C(I)=C(I)+A(J)*B(JR)-A(JC)*B(JRC)  MTR40360
410   C(I')=C(IC)+A(J)*B(JRC)+A(JC)*B(JR)  MTR40361
500   CONTINUE
600   CONTINUE
700 RETURN
END
$ FORTRAN LSTOU,DECK
C POLMS
      SUBROUTINE POIM (PN,PN1,ON,ON1,E2,LMRD1,LMRD2,NC,IR,IGO)  MTR40372
      DIMENSION PN(1), PN1(1), ON(1), ON1(1), E2(1), LMRD1(1), LMRD2(1)  MTR40374
      DOUBLE PRECISION PN, PN1, ON, ON1, LMRD1, LMRD2, A(?)  MTR40375
      IR=0  MTR40376
      DO 10 (100,100,100),IGO  MTR40377
100   DO 10 (110,200),NC  MTR40379
110   IF ( DAHS( (PN-PN1)/(DSORT( DAHS(ON) )) ) -E2 ) 12,120,112  MTR40381
112   IF ( DAHS( PN-PN1 ) - E2**2 ) 120,120,1/0  MTR40382
120   IF ( DAHS( (ON/ON1)-1. ) - E2 ) 13,130,1/0  MTR40384
130   LMRD2 = (PN*PN -4.*ON)  MTR40386
      LMRD2 = DSORT (DAHS(LMRD2) )  MTR40387
      LMRD1 = (-PN + LMRD2) /2.  MTR40388
      LMRD2 = (-PN - LMRD2) /2.  MTR40389

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    IF ( ABS(LMRD1) = ABS(LMRD2) )           140,150,160      MTR40391
140 A=LMRD1                                MTR40392
    LMRD1=LMRD2                                MTR40393
    LMRD2=A                                MTR40394
    GO TO 160                                MTR40395
150 IF ( LMRD1 )           140,160,160      MTR40396
160 IR=NC                                MTR40398
170 RETURN                                MTR40400
180 GO TO (130,220),NC                    MTR40401
200 A=DSORT( QN(1)*QN(1) + QN(2)*QN(2) )
    IF ( DSORT( ( (PN-PN1)*(PN-PN1) + (PN(2)-PN1(2))*(PN(2)-PN1(2)) ) )
1           / A ) -F2)           210,210,170      MTR40405
210 A = QN1*QN1 + QN1(2)*QN1(2)
    IF ( ( ( (QN+QN1-QN(2)*QN1(2))/A )*( (QN+QN1-QN(2)*QN1(2))/A ) +
1           ( (QN+QN1(2)+QN1*QN(2))/A )*( (QN+QN1(2)+QN1*QN(2))/A ) )
2           -1. ) - F2)           220,220,170      MTR40406
MTR40407
MTR40409
MTR40410
MTR40411
220 A(1) = PN*PN - PN(2)*PN(2) -4.*QN
    A(2) = 2.*(PN*PN(2)-2.*QN(2))
    IF ( A(1) )           230,250,250      MTR40412
MTR40413
MTR40415
230 A(1) = DSQRT( (-A(1)+DSQRT( A(1)*A(1)+A(2)*A(2) ) ) /2. )
    A(2) = A(2) / (2.*A(1))           MTR40417
MTR40418
232 LMRD1(1) = (-PN+A(2))/2.
    LMRD1(2) = (-PN(2)+A(1))/2.
    LMRD2(1) = (-PN-A(2))/2.
    LMRD2(2) = (-PN(2)-A(1))/2.
    IF ( DSQRT( LMRD1*LMRD1+LMRD1(2)*LMRD1(2) ) - DSQRT( LMRD2*LMRD2 )
1           LMRD2(2)*LMRD2(2) )           240,160,160      MTR40425
MTR40426
MTR40427
MTR40428
MTR40429
MTR40430
240 A=LMRD1(2)
    LMRD1(2)=LMRD2(2)
    LMRD2(2)= A
    GO TO 140
250 A(1) = DSQRT( (A(1)+DSQRT( A(1)*A(1)+A(2)*A(2) ) ) /2. )
    A(2) = A(2) / (2.*A(1))           MTR40432
MTR40433
LMRD1=A(1)
A(1)=A(2)
A(2)=LMRD1
GO TO 232
FND
    FORTRAN LST010,DFCK
POS
SURROUNIQUE PO (FL, HN, HN1, HN2, HN3, P, Q, NC, MAXR )
DIMENSION FL(1), HN(1), HN1(1), HN2(1), HN3(1), P(1), Q(1),
1          A(3), B(3)                                MTR40441
DOUBLE PRECISION FL, HN, HN1, HN2, HN3, P, Q, A, B
MAXR = MAXR/2
GO TO (200,100), NC
100 A(1) = FL(1)*HN - FL(2)*HN(MAXR+1)
    A(2) = FL(3)*HN1 - FL(4)*HN1(MAXR+1)
    A(3) = FL(5)*HN2 - FL(6)*HN2(MAXR+1)
    B(1) = FL(1)*HN(MAXR+1)+ FL(2)*HN
    B(2) = FL(3)*HN1(MAXR+1)+FL(4)*HN1
    B(3) = FL(5)*HN2(MAXR+1)+FL(6)*HN2
    P(1) = A(3)*HN1 - B(3)*HN1(MAXR+1)-A(1)*HN3 + B(1)*HN3(MAXR+1)
    P(2) = A(3)*HN1(MAXR+1)+B(3)*HN1 - A(1)*HN3(MAXR+1)-B(1)*HN3
    Q(1) = A(1)*HN" - B(1)*HN2(MAXR+1)-A(2)*HN1 + B(2)*HN1(MAXR+1)
    Q(2) = A(1)*HN2(MAXR+1)+B(1)*HN2 - A(2)*HN1(MAXR+1)-B(2)*HN1
    A(1) = A(2)*HN3 - B(2)*HN3(MAXR+1)-A(3)*HN2 + B(3)*HN2(MAXR+1)
    R(1) = A(2)*HN3(MAXR+1)+B(2)*HN3 - A(3)*HN2(MAXR+1)-B(3)*HN2
    A(2) = A(1)*P(1) + B(1)*P(2)
    R(2) = A(1)*P(2) - B(1)*P(1)
    A(3) = A(1)*Q(1) + B(1)*Q(2)           MTR40442
MTR40443
MTR40445
MTR40447
MTR40448
MTR40449
MTR40450
MTR40451
MTR40452
MTR40454
MTR40455
MTR40456
MTR40458
MTR40459
MTR40461
MTR40462
MTR40464
MTR40465
MTR40467
MTR40468
MTR40469

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B(3) = A(1)*Q(2) - B(1)*Q(1) MTR40470
A(1) = A(1)*A(1) + B(1)*B(1) MTR40471
A(2) = A(2)/A(1) MTR40472
B(2) = B(2)/A(1) MTR40473
A(3) = A(3)/A(1) MTR40474
B(3) = B(3)/A(1) MTR40475
P(1) = FL(3)*A(2) - FL(4)*B(2) MTR40476
P(2) = FL(3)*B(2) + FL(4)*A(2) MTR40477
A(2) = FL(3)*FL(5) - FL(4)*FL(6) MTR40478
B(2) = FL(4)*FL(5) + FL(3)*FL(6) MTR40479
Q(1) = A(2)*A(3)-B(2)*B(3) MTR40480
Q(2) = A(2)*B(3)+A(3)*B(2) MTR40481
MAXR = 2*MAXR MTR40482
RETURN MTR40483
200 A(1) = (FL(2)*HN1*HN3 - FL(3)*HN2*HN2) MTR40484
P(1) = (FL(3)*HN2(1)*HN1(1) - FL(1)*HN1(1)*HN3(1)) / A(1) MTR40485
Q(1) = (FL(1)*HN1(1)*HN2(1) - FL(2)*HN1(1)*HN1(1)) / A(1) MTR40486
P(1) = P(1)*FL(2) MTR40487
Q(1) = Q(1)*FL(2)*FL(3) MTR40488
MAXR = 2*MAXR MTR40489
RETURN MTR40490
FND MTR40500

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## FORTRAN LSTOU,DECK

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C CLOSES
C SUBROUTINE CLOSES. COMPUTES 2 CLOSE ROOTS. MTR40501
C
C U = MATRIX, DIMENSIONED (MAXR,2*NC*MAXR) MTR40502
C H = STARTING GUESS, DIMENSIONED((MAXR,2*NC*4)+2*NC*N) MTR40503
C NSIZE = SIZE OF MATRIX MTR40504
C MAXR = DIMENSIONED NUMBER OF ROWS OF U AND H MTR40505
C MAXTRY = MAXIMUM NUMBER OF DOUBLE PRECISION ITERATIONS. MTR40506
C EPS1 = SINGLE ROOT CONVERGENCE CRITERIA MTR40511
C EPS2 = DOUBLE ROOT CONVERGENCE CRITERIA MTR40512
C R= AIKENS CONVERGENCE CRITERIA MTR40513
C IRR = ERROR RETURN INDICATOR. =1, OVERFLOW MTR40514
C =2, DIVIDE CHECK MTR40515
C =3, BOTH OVERFLOW AND DIVIDE MTR40516
C CHECK. MTR40517
C
C ITERS= NUMBER OF ITERATIONS PERFORMED, - FOR DOUBLE ROOT MTR40518
C + FOR SINGLE ROOT MTR40519
C
C NC = 1, REAL ? , COMPLEX MTR40520
C SURROUTINE CLOSES (U,H,NSIZE,MAXR,R,EPS1,EPS2,NC,IRR,MAXTRY,ITERS,MTR40521
C 1 NAITKN,INDEX1,INDEX2,VALUE,MSIZE) MTR40522
C
C DIMENSION U(1), H(1), VALUE(1) MTR40523
C CALL OVRFLL ( IOVFLW ) MTR40524
C CALL DVCHK ' IDVDC1' MTR40525
C IRR=0 MTR40526
C NX=2*NSIZE MTR40527
C N2C=2*NC MTR40528
C CALL CHANGE (U,MSIZE,NC*MSIZE,MA1,1) MTR40529
C CALL CHANGE (H,NSIZE,NC,NSIZE,1) MTR40530
C I6=N2C*NSIZE MTR40531
C I1=1 MTR40532
C I2=I1+16 MTR40533
C I3=I2+16 MTR40534
C I4=I3+16 MTR40535
C I5=I4+16 MTR40536
C K1=11 MTR40537
C K4=12 MTR40538
C K4=13 MTR40539
C K2=14 MTR40540

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ITERS = 0 MTR40545
100 K=0 MTR40547
100 IGO = 1 MTR40548
120 ITERS=ITERS+1 MTR40549
120 IF ( ITERS-MAXTRY ) 140,140,130
130 IF ( K=0 ) 132,140,132
132 ITERS = ITERS-1
80 TO 800
140 K=K+1
140 I=K1
140 K1=K4
140 K4=K3
140 K3=K2
140 K2=I
140 CALL MULT ( 0 , H(K2),H(K1),NSIZE,NSIZE,1,MAXR,NCIZE,NSIZE,
1        NC,2 )
140 INDEX=0
140 IK=15+(4-K)*NPC
140 CALL NORM ( H(K1),H(K1),NSIZE,H(IK),INDEX,NSIZE,NC,2 )
140 CALL OVERFL ( IOVFLW )
140 GOTO (150,160) .IOVFLW
150 IRR=IRR+1
160 CALL DVCHK ( IDVDCT )
160 GOTO (170,180) .IDVDCT
170 IRR=IRR+2
180 IF ( IRR ) 200,200,640
C TEST FOR CONVERGENCE TO A SINGLE ROOT
200 DO 220 I=1,16,2
200 J2 = K2+I-1
200 J3 = K1+I-1
200 IF ( ABS(H(J2)-H(J3))-EPS1 ) 220,220,300
220 CONTINUF
220 GOTO 750
300 GOTO (120,120,120,320),K
320 J1=15+(IGO+5)*N2C
320 J2=15+(IGO+5)*N2C
320 J=2*INDEX-2
320 J3=K1+J
320 J5=K2+J
320 J7=K3+J
320 J9=K4+J
C COMPUTE P N AND Q N.
320 CALL PD (H(15), H(J3), H(J5), H(J7), H(J9), H(J1), H(J2), NC, NX)
320 GOTO (330,340),IGO
340 J1= 15+4*N2C
340 J2= J1+N2C
340 J3= J2+N2C
340 J4= J3+N2C
340 J5= 15+N2C
340 J6= J5+N2C
C TEST FOR DOUBLE ROOT CONVERGENCE AND IF SO, COMPUTE LAMBDA 1 AND 2.
340 CALL POLM (H(J2),H(J1),H(J4),H(J3),EPS2,H(J5),H(J6),NC,IR,IGO)
340 GOTO (344,344,400),IGO
344 IF ( IR ) 346,346,400
346 IF ( ITFRS-MAXTRY ) 347,800,800
347 DO 348 I=1,N2C
347 H(J1)=H(J2)
347 H(J3)=H(J4)
347 J1=J1+1
347 J2=J2+1
347 J3=J3+1

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348 J4=J4+1
350 K=3
1GO=?
DO 354 J=1,3
L=15+(3-J)*N?C
L1=15+(4-J)*N?C
DO 354 I=1,NC
L=L+(I-1)*NC
L1=L1+(I-1)*NC
H(L1)=H(L)
H(L1+1)=H(L+1)
354 CALL AITKNS (H(K1), H(K2), H(K3), H(K4), R, E, NSIZE, NC, 2,
1 IF ( IR )           360,120,360
360 I=K1
K1=K4
K4=K3
K3=K2
K2=1
NAITKN = NAITKN+1
GOTO 100
400 CALL POH (H(J5), H(J5), H(J6), H(K1), H(K2), H(K3), H(K4), NSIZE,
1 NC)
GOTO (404,402),NC
402 VALUE(?)=H(J5+?)
VALUE(4)=H(J6+?)
404 INDFX=0
VALUF(1)=H(J5)
VALUE(NC+1)=H(J6)
CALL NORM (H(K3),H(K3),NSIZE,H(J1),INDEX,NSIZE,NC,0)
INDFX1 = INDEX
ITFRS = -ITERS
i=K4+2*INDEX-2
H(J1)=H(I)
H(J1+1)=H(I+1)
GOTO (420,410),NC
410 I = J+NX
H(J1+2)=H(I)
H(J1+3)=H(I+1)
420 INDEX=-INDEX
CALL NO_M (H(K4),H(K4),NSIZE,H(J1),INDFX,NSIZE,NC,0)
IF ( K = ? )           440,500,480
440 J3=13
442 J4=14
450 K=1
460 DO 462 J=1,16
J1=J3+J-1
J2=J4+J-1
462 H(J1)=H(J2)
GOTO (520,510,514,600),K
470 J3=11
GOTO 442
480 IF ( K3=13 )           490,490,470
490 K=3
J3=11
J4=13
GOTO 460
500 K=2
J3=13
J4=11
GOTO 460
MTR40620
MTR40622
MTR40623
MTR40624
MTR40625
MTR40626
MTR40627
MTR40628
MTR40629
MTR40630
MTR40631
MTR40632
MTR40633
MTR40634
MTR40635
MTR40636
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MTR40680
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MTR40682
MTR40683
MTR40684
MTR40685
MTR40686
MTR40687

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510 J3=11          MTR40688
512 J4=12          MTR40689
514 GOTO 450       MTR40690
514 J3=13          MTR40691
514 GOTO 512       MTR40692
520 CALL MADS (H(11),H(15),H(12),NSTZF,NC) MTR40693
580 CALL CHANGE (H(11),NSIZE,2*NC,NSTZF,?) MTR40695
604 J=NC*NSIZE+1  MTR40697
INDEX=0           MTR40698
CALL NORM (H(J),H(J),NSIZE,H(15),INDEX,NSIZE,NC,1) MTR40700
J=J+INDEX1-1     MTR40701
J1=J+(NC-1)*NSIZE MTR40702
H(J)=0.            MTR40703
H(J1)=0.           MTR40704
INDEX2 = INDEX    MTR40705
606 CALL OVERFL ( IOVFLW ) MTR40707
GOTO (610,620) ,IOVFLW MTR40708
610 IRR=IRR+1      MTR40709
620 CALL DVCHK ( IDVDCT ) MTR40711
GOTO (630,640) ,IDVDCT MTR40712
630 IRR=IRR+2      MTR40713
640 CALL CHANGE (I,MSIZE,NC*MSIZE,MAXR,?) MTR40715
700 RETURN         MTR40717
750 IK=I5+(4-K)*N2C MTR40719
VALUE(1) = H(IK)   MTR40720
IK=IK+2*(NC-1)     MTR40721
VALUE(NC)=H(IK)    MTR40722
INDEX1=INDEX       MTR40723
K=4                MTR40724
J3=11              MTR40725
J4=K1              MTR40726
IF ( K1=11 )        460,600,460 MTR40727
800 IGO=3           MTR40729
INDEX1=INDEX       MTR40730
J=15               MTR40731
J1 = I5+4*N2C      MTR40732
806 CALL LEGIS ( H(J),H(J1),FPS1,EPS2,NC,IR ) MTR40733
IF ( IR )          340,340,750 MTR40734
END               MTR40736

FORTRAN LISTING.DFCK

C MITERS
C A IS STORED IN CORE AT A. (MAXR X NC*NP*NSIZE) MTR40738
C NTAPUT IS A UTILITY TAPE, FOR CHECK VECTORS IF DESIRED. MTR40739
C EPS1 = EPSILON ONE = SINGLE PRECISION CONVERGENCE TEST NUMBER MTR40740
C EPDP = EPSILON TWO = DOUBLE PRECISION .. .. .. MTR40741
C NC = 1, IF REAL NP = 1, IF SINGLE PRECISION MTR40742
C 2, IF COMPLEX      = 2, IF DOUBLE .. MTR40743
C NGUESS = 0, IF FIRST GUESS IS TO BE A COLUMN OF ONES. MTR40744
C MODOUT = NO. OF MODES TO BE COMPUTED. MTR40745
C NAKSR = NO. TIMES ALTKNS ACCELERATION WAS USED IN SINGLE PRECISION. MTR40746
C NAKDR = .. .. .. .. .. .. .. .. .. .. .. .. .. .. .. .. MTR40747
C MAXSR = MAXIMUM ITERATIONS ALLOWED IN SINGLE PRECISION. MTR40748
C MAXDR = .. .. .. .. .. .. .. .. .. .. .. .. .. .. .. .. .. MTR40749
C IRN = ERROR RETURN = 1, FOR OVERFLOW MTR40750
C          2, FOR DIVIDE CHECK MTR40751
C          3, FOR BOTH OVERFLOW AND DIVIDE CHECK MTR40752
C NSIZE = NO. OF ROWS AND COLUMNS OF A MTR40753
C RSP = R, ALTKNS ACCELERATION CONVERGENCE CONTROL FOR SINGLE PRECIS. MTR40754
C RDP = R ALTKNS ACCELERATION CONVERGENCE CONTROL FOR DOUBLE PRECIS. MTR40755
C MAXR = DIMENSIONED NUMBER OF ROWS OF A AND GUESS MTR40756
C SUBROUTINE MITERS(A,GUESS,NGUESS,NSIZE,MODOUT,MAXR,NC,FPS1,EPDP, MTR40758

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1 NAKSR, NAKDR, MAXSR, MAXDR, RSP, RDP, IR>, H, VECTOR. MTR40759
2 VALHF, NITER, NTAPUT, NTAPOT) MTR40760
1 DIMENSION A(1), GUFS(1), H(1), NITER(1), NAKSR(1), NAKDR(1), MTR40763
1 ATITLE(9), VFCOR(1), VALUE(1) MTR40764
1 DATA (ATITLE(I), I=1,9) / 10H OVERFLOW. , 10H MTR40766
1 10H DIVIDE . 10H CHECK . 10H IN , MTR40767
2 10H CLOSF . 10H SWEEP . 10HSUBROUTINE, MTR40768
3 10H / MTR40769
10 FORMAT (1H0 5X, 6H MODE 14X, 11H EIGENVALUE 10X, MTR40771
1 24H ITERATIONS S.P. D.P. 6X, 20H AITKENS S.P. D.P. MTR40772
2 // ) MTR40773
12 FORMAT (1H 1111, 2F19.8, 1122, 11/, 1119, 11/) MTR40774
14 FORMAT (1H 1111, 1F29.8, 1131, 11/, 1119, 11/) MTR40775
16 FORMAT (1H0 116, 43H MODES ARE CORRECT, COMPUTATION TERMINATED.) MTR40776
18 FORMAT (15H MODIFIED MODE 11A, 22H IS CORRECT, TRUE MODE MTR40777
1 20H CANNOT BE COMPUTED. ) MTR40778
20 FORMAT (1H0 // 1H0 46X, 14H EIGENVECTORS // ) MTR40779
22 FORMAT (1H1 10X, 36H CHECK EIGENVALUES AND EIGENVECTORS // MTR40780
1 (6E16.8) ) MTR40781
24 FORMAT (5H MODE 11A, 20H HAS NOT CONVERGED IN MAXIMUM MTR40782
1 12H ITERATIONS ) MTR40783
26 FORMAT (37H***** ERROR IN ITERATION SUBROUTINE PA10 ) MTR40784
CALL OVERFL ( IOVFLW )
CALL DVCHK ( IDVDC )
MSIZE = NSIZE
ISIZE = NC*MAXR
IRR=0
C FIND A AND STORE ON TAPE IF NECESSARY.
IF ( NTAPUT ) 102,102,100
100 REWIND NTAPUT
M=NSIZE*ISIZE
WRITE ( NTAPUT ) (A(I),I=1,M)
REWIND NTAPUT
102 IF ( FPSP ) 106,104,106
104 FPSP = .5E-18 MTR40799
106 IF ( FPDp ) 110,108,110 MTR40800
108 EPDP = .5E-18 MTR40802
110 JS17E=NSIZE*(NC-1) MTR40803
MTR40805
C DEFINE FIRST GUESS. IF NOT GIVEN.
IF ( NGUESS ) 111,114,111 MTR40807
111 IF ( MAX -NS17F ) 116,114,112 MTR40810
112 DO 113 I=1,NSIZE MTR40811
J= NS17F+1 MTR40812
JI= MAXR+1 MTR40813
113 GUESS(J)=GUESS(J1) MTR40814
BOTO 116 MTR40815
114 DO 115 I=1,NSIZE MTR40817
J=JS17F+1 MTR40818
GUESS(J) = 0. MTR40819
115 GUESS(1)=1. MTR40820
C DEFINE PROGRAM CONSTANTS.
116 MODE = II MTR40822
117 M=1 MTR40824
12 = 11+ISIZE MTR40825
13 = 12+ISIZE MTR40826
C SET FOR MODE COUNT
130 MODE=MODE+1 MTR40827
KSIZE = NC*MSIZE MTR40829
11 ( MODE-MODOUT ) 140,140,500 MTR40831
140 NSRAKE=0 MTR40832
MTR40833
MTR40834

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NDRAK=0          PTR40836
ITERSR=0         MTR40837
ITERDR=0         MTR40838
K1=11            MTR40840
K2=13            MTR40841
K3=12            MTR40842
DO 150 K=1,NC   MTR40844
    J1=(K-1)*NSIZE
    J= (K-1)*MSIZE+K1-1
    DO 150 J=1,MSIZF
        J=J+1
        J1=J1+1
150   H(J)=GUESS(J1)           MTR40845
152 NAK=0          MTR40850
150 NAK=NAK+1      MTR40853
152 ITERSR=ITERSR+1  MTR40855
    IF (ITERSR-MAXSR)      1/0,1/0,2/0
170 I=K1           MTR40857
    K1=K3           MTR40860
    K3=K2           MTR40861
    K2=1            MTR40862
C SET .... NOW MAKE ONE ITERATION.
C
    CALL MULT (A,H(K2),H(K1),MSIZE,MSIZE,1,MAXR,MSIZE,MSIZE,NC,1)
    INDFX=0          MTR40865
    IK= I3+KSIZE+NC*(I-NAK)
    CALL NORM (H(K1),H(K1),MSIZE,H(IK),INDEX,MSIZE,NC,1)
    CALL OVERFL ( IOVFLW )
    CALL DVCHK ( IDVDCT )
    GOTO (180,182) ,IOVFLW
180 IRR=IRR+1      MTR40876
182 GOTO (184,186) ,IDVDCT
184 IRR=IRR+2      MTR40878
186 IF (IRR)      190,190,600
190 GOTO (160,200,200),NAK
200 DO 210 I=1,KSIZE
    J1=K1+I-1
    J2=K2+I-1
    IF (ABS(H(J1)-H(J2))-EPSP)      210,210,220
210 CONTINUE       MTR40887
    GOTO 400          MTR40888
220 GOTO (160,160,230),NAK
230 CALL AITKNS ( H(K1), H(K2), H(K3), H(K3), RSP, MSIZE, MSIZE, NC,
    1, IR )           MTR40893
    IF (IR)          240,242,240
242 I=2*NC          MTR40896
    J=IK+1          MTR40897
    DO 244 I=1,I,NC
        J1=J+NC-1
        J2=J-1+1
        J3=J1-NC
        J4=J2-NC
        H(J1)=H(J3)
244   H(J2)=H(J4)
    GOTO 162          MTR40904
248 I=K1           MTR40907
    K1=K3           MTR40908
    K3=K2           MTR40909
    K2=1            MTR40910
    NSRAK=NSRAK+1   MTR40911
    GOTO 142          MTR40912

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250 CALL OVERFL ( IOVFLW )
CALL BVCHK ( IVDRCT )
GOTO (260,262) ,IOVFLW
260 IRR=IRR+1
262 GOTO (264,266) ,IVDRCT
264 IRR=IRR+2
266 IF ( IRR ) 270,270,600
270 IF (K1-I1) 272,280,272
272 DO 274 I=1, KSIZE
    J=KL+I-1
    J1=I1+I-1
274 H(J1)=H(J)
280 J=(MODE-1)*NC+1
ITERSR=ITERSR-1
CALL CLOSES(A,H(I1),MSIZE,MAXR,RDP,EPSP,EPDP,NC,IRR,MAXDR,ITERUR,MTR4093,
1 NDRAK,INDEX1,INDEX2,VALUE(J), NSIZE ) MTR40931
IF ( IRR ) 282,282,610 MTR40945
282 IF ( ITERDR ) 283,288,288 MTR40946
283 IF ( KSIZE-1SIZE ) 284,288,288 MTR40948
284 J1 = I1+2*KSIZE MTR40950
    I2 = I2+KSIZE MTR40951
    DO 286 I=1, KSIZE MTR40952
        J1= J1-1 MTR40953
        J2= J2-1 MTR40954
286 H(J2)=H(J1) MTR40955
288 INDEX = INDEX1 MTR40957
    INDEX = INDEX MTR40958
290 M1 = NSIZE-1 MTR40959
    J1=INDEX MTR40960
    IF ( J1-M1 ) 292,292,298 MTR40961
292 DO 296 K=1,1SIZE MTR40962
    L=(K-1)*MAXR MTR40963
    L1=L+INDEX MTR40964
    HOLD=A(L1) MTR40965
    DO 294 J=J1,M1 MTR40966
        I=L+J MTR40967
        A(I)=A(I+1) MTR40968
294 A(I+1)=HOLD MTR40969
296 L=NSIZE-MODE+1 MTR40970
    J = (MODE-1) * NC * MAXR +1 MTR40972
CALL SWEPX (VECTOR(J),A, H, A(L), VALUE, MODE, MSIZE, MAXR, NC, MTR40977
1 INDEX, EPSP, NSIZE, NITER(MODOUT+1) , IRR) MTR40978
CALL OVERFL ( IOVFLW )
CALL BVCHK ( IVDRCT )
GOTO (300,302) ,IOVFLW
300 IRR=IRR+1
302 GOTO (304,306) ,IVDRCT
304 IRR=IRR+2
306 IF ( IRR ) 310,310,620
310 I=(NC-1)*NSIZE
    DO 312 J=INDEX,NSIZE
        I=I+J
        GUESS(I)=GUESS(L+1)
312 GUESS(J)=GUESS(J+1)
    MSIZE = MSI/F-1
    NITER(MODE) = ITERSR+ITERDR
    NAKSR(MODE) = NSRAK
    NAKDR(MODE) = NDRAK
    IF ( ITERDR ) 320,360,360 MTR40998
320 MODE=MODE+1 MTR40999
    ITERDR=-ITERDR MTR41000

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NITER(MODE-1)= 0.          MTR41001
INDEXX=INDEXZ              MTR41002
IF ( INDEX-NSIZEF )        326,330,330
326 IF ( INDEX1-INDEX2 )    330,330,340
330 INDEX=-INDEX           MTR41003
-INDEXX=INDEX-1            MTR41004
GOTO 342                  MTR41005
340 INDEX=-INDEX           MTR41006
342 CONTINUEF              MTR41007
   11=11+ISIZE              MTR41008
   12=12+ISIZE              MTR41009
   13=13+ISIZE              MTR41010
NAKSR(MODE-1) = 0.          MTR41011
NAKDR(MODE-1) = 0.          MTR41012
GOTO 290                  MTR41013
348 11=11+ISIZE              MTR41014
   12=12+ISIZE              MTR41015
   13=12+ISIZE              MTR41016
GOTO 130                  MTR41017
400 IF ( K1-11 )           410,413,410
410 DO 412 I=1,KSIZE      MTR41018
   J=K1+I-1                MTR41019
   J1=I1+I-1
412 H(J1)=H(J)             MTR41020
413 DO 414 J=1,NC          MTR41021
   I= NC*(MODE-1)+1
   J1=IK+J-1
414 VALUE(I)= H(J1)        MTR41022
INDEXX=INDEX               MTR41023
GOTO 290                  MTR41024
500 MODE=MODE-1             MTR41025
IF ( MODE )                 510,530,502
502 IF ( NTAPUT )           510,510,504
504 READ ( NTAPUT ) (A(I),I=1,M)
CALL MULT (A,VECTOR, H,NSIZE,NSIZEF,MODE,MAXR,MAXR,MXR,NC,1)
DO 506 I=1,MODE
   J= (I-1)*ISIZE
   J1= (I-1)*NC+1
   INDEX=II
506 CALL NORM (H(J),H(I),NSIZEF,GUSS(J),INDEX,MAXR ,NC,1)
510 IF ( NTAPOT )           530,530,512
512 WRITE (NTAPOT,10 )
DO 522 I=1,MODE
   J1= MAXSR
   J2= NITER(I)-MAXSR
   IF ( J2 )                 514,515,515
514 J1=NITER(I)
   J2=0
   GO TO 517
515 IF ( J2-MAXDR )         517,516,516
516 WRITE (NTAPOT,21) !
517 GO TO (518,520),NC
518 WRITE (NTAPOT,11)        I, VALUE(I), J1,J2, NAKSR(I),NAKDR(I)
GOTO 522
520 I= 2*I
   WRITE (NTAPOT,12) I, VALUE(I-1), VALUE(I), J1,J2, NAKSR(I),
   NAKDR(I)
522 CONTINUEI
   J=NC*MODE
   WRITE (NTAPOT,20)
CALL MPRINT (VECTOR,NSIZE,J,MAXR,NTAPOT)

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IF ( NTAPUT )          530,534,524
524 WRITE (NTAPOT,22) ((GUSS(I),I=1,J))      MTR41071
CALL MPRINT (H,NSIZE,J,MAXR,NTAPOT)          MTR41072
530 RETURN                                MTR41073
530 NITER(MODE) = ITERSR+ITEROR            MTR41074
NAKSR(MODE) = NSRAK                         MTR41075
NAKDR(MODE) = NDRAK                         MTR41081
IF ( NTAPOT )          530,530,501           MTR41082
501 J=1
J1=4
GOTO (602,604,606),IRR
602 J1=2
GOTO 606
604 J=3
606 WRITE (NTAPOT,26) (ATITLE(I),I=J,J1)     MTR41088
GOTO 630
610 J2=6
612 NITER(MODE) = ITERSP+ITEROR            MTR41091
NAKSR(MODE) = NSRAK                         MTR41092
NAKDR(MODE) = NDRAK                         MTR41093
IF ( NTAPOT )          530,530,613           MTR41094
613 J=1
J1=4
GOTO (614,616,618),IRR
614 J1=2
GOTO 618
616 J=3
618 WRITE (NTAPOT,26) (ATITLE(I),I=J,J1), (ATITLE(5)),1
1   (ATITLE(J2)), (ATITLE(1),I=8,9)          MTR41102
1   IF ( J2=6 )          630,630,622           MTR41103
620 J2=1
GOTO 612
622 WRITE (NTAPOT,18) MODE
IRR=0
J= (MODE-1)*NC*MAXR
DO 624 I=1,ISIZE
J1=J+1
J2=J+(NC-1)*MAXR+1
VECTOR(J2)=0.
624 VECTOR(J1)=0.
GOTO 310
630 I=MODE-
WRITE (NTAPOT,16) I
GOTO 500
END
$  FORTRAN LSTOII.DCK
C SWEPS
C SWEPX SUBROUTINE
C COMPUTES TRUE MODE AND SWEPS IT FROM THE MATRIX. (REAL OR COMPLEX)
C HTRUE = TRUE MODAL COLUMNS, AS COMPUTED. U = DYNAMIC MATRIX.
C H = SERIES OF MODIFIED MODAL COLUMNS. FL = COLUMN OF EIGENVALUES.
C US = SERIES OF MODIFIED MODAL ROWS OF U.
C MODE = MODE NOW BEING COMPUTED.      N = SIZE
C MD = DIMENSIONED NUMBER OF ROWS OF U.US,H,HTRUE
C NX = 1 IF PROBLEM IS REAL.
C = 2 IF PROBLEM IS COMPLEX.
C SUBROUTINE SWEPX (HTRUE, U, H, US, FL, MODE, N, NC, ND, INDEX,
C EP, MSIZE, INDIS, IRR)
C DIMENSION H(1), US(1), U(1), HTRUE(1), FL(1), Q(4) INDIS(1)
C
MTR41126
MTR41127
MTR41128
MTR41129
MTR41130
MTR41131
MTR41132
MTR41133
MTR41134
MTR41135
MTR41136
MTR41137
MTR41138
MTR41139

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INDEX=IARS(INDEX)
INDIS(MODE) = INDEX          MTR41150
M=MODE-1                     MTR41151
K1=M*NC*MD                   MTR41152
NN=NC*MD                      MTR41153
K2=MSIZE-M                   MTR41154
IF ( M )                      MTR41155
70 GOTO (140,72),NC           MTR41156
12 IF ( MSIZE-MD )            MTR41157
74 L=K1+2*NN+1                MTR41158
K=K1+MD+NN+1                 MTR41159
DO 76 I=1,N                   MTR41160
  K=K-1                        MTR41161
  I=L-1                        MTR41162
  H(K)=H(L)                   MTR41163
76 H(L)=0.                     MTR41164
  GOTO 140                     MTR41165
80 DO 94 I=1,M                MTR41166
  J1=MODE+1                    MTR41167
  INDIS(J1)=INDIS(I)          MTR41168
100 IF ( INDEX )              102,104,104 MTR41169
102 K2=K2+1                   MTR41170
  M=M-1                        MTR41171
104 J1=K1+K2*NC+1             MTR41172
  J2=K1+MSIZE*NC               MTR41173
  IF ( J1-J2 )                  105,105,107 MTR41174
105 DO 106 I=J1,J2            MTR41175
  H(I)=0.                       MTR41176
107 GO TO (114,108),NC         MTR41177
108 J1=K1+K2*MD+1             MTR41178
  J2=K1+K2*NC+1               MTR41179
  DO 110 I=1,K2               MTR41180
    J1=J1-1                     MTR41181
    J2=J2-1                     MTR41182
  110 H(J1)=H(J2)              MTR41183
  IF ( M )                      118,118,111 MTR41184
111 DO 112 I=1,M              MTR41185
  H(J2)=0.                      MTR41186
  112 J2=J2+1                  MTR41187
114 IF ( M )                  118,118,120 MTR41188
120 II=1                       MTR41189
  DO 130 I=1,M                MTR41190
  121 DO 122 J=1,M              MTR41191
    J1=MODE+J                   MTR41192
    IF ( II + INDIS(J1) )        122,123,122 MTR41193
    CONTINUE                     MTR41194
    II=II+1                     MTR41195
    GOTO 121                     MTR41196
123 INDIS(J1)=0                 MTR41197
  IF ( INDIS(MODE)-II )          125,124,124 MTR41198
124 INDIS(MODE)+INDIS(MODE)+1   MTR41199
125 I=MSIZE-II                 MTR41200
  II ( I )                      129,129,126 MTR41201
126 J1= K1+MSIZE               MTR41202
  J2= K1 +MSIZE +(NC-1)*MD     MTR41203
  DO 128 J=1,I                 MTR41204
    J1=J1-1                     MTR41205
    J2=J2-1                     MTR41206
    H(J2+1) = H(J2)              MTR41207
    H(J1+1) = H(J1)              MTR41208
  128 J1=K1+II                  MTR41209
129 J1=K1+II                  MTR41210

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J2=J1+(NC-1)*MD          MTR41217
H(J1)=0.                  MTR41218
H(J2)=0.                  MTR41219
130  CONTINUE              MTR41220
    IF ( INDX )           118,131,131
118  M=M+1
131  DO 132  I=1,M
    J1=MODE+I
132  INDIS(J1)=INDIS(I)
    II=1
    DO 133  I=1,M
    J1=MODE+I
    IF ( II-INDIS(J1) )   1134,1135,1134
133  DO 1134  J=1,M
    J1=MODE+J
134  CONTINUE
    II=II+1
    GOTO 133
1135  L1=(NC*MSIZE-1)*MD+MODE+1
    L2=(MSIZE-1)*NN
    INDIS(J1) = " "
    DO 138  J=1,NC
    J2=L1-(J-1)*MD-1
    IF ( L2-NN )           138,134,134
134  DO 136  I=1,L3,NN
        J1=L1-I
        J2=J1-NN
136  US(J1)=US(J2)
        L1=L1-MD
138  US(J2)=0.
140  DO 142  I=1,NN
    J1=K1+I
142  HTRUE(I)=H(J1)
    IF ( N )               31,31,8
    R DO 25  I=1,N
    K=MODE+I
    L1=NC*MD*(K-1)
    CALL  MULT (US( K ), HTRUE, G, 1, MSIZE, 1, MD, MI, 1, NC, 1 ) MTR41253
    IF ( R(1) )             12,9,12
    R DO 10 (11,1P),NC
10  IF ( R(1) )             12,11,12
11  IRR=IRR+2
12  CONTINUE
    GOTO (14,19),NC
14  IF (AHS(F1(K)-FL(MODE))-1.0) - FP )   15,15,16
15  Q=1.0
    GOTO 17
16  Q=(F1(K)-FL(MODE))/0
17  DO 18  J=1,MSIZE
    I=L1+J
18  HTRUE(J)=H(I)+Q(1)*HTRUE(J)
    GOTO 25
19  K=2*K
    I=2*MODE
    IF ( AHS((F1(K-1)+F1(J-1)+FL(K)*FL(J))/(FL(J-1)**2+FL(J+2)-1.0) -FP) 20,24,26
20  IF ( AHS((F1(K)+F1(J-1)-F1(K-1)*FL(J))/(FL(J-1)**2+FL(J)**2)) -FP) 21,21,22
21  Q(1)=1.0
    Q(2)=0.0
    GOTO 25
22  Q(3)=Q(1)**2+Q(2)**2

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G(4)=(FL(K)-FL(J))*G(1)+(FL(K-1)-FL(J-1))*G(2)
G(1)=((FL(K-1)-FL(J-1))*G(1)+(FL(K)-FL(J))*G(2)) / G(3)
G(2)= G(4) / G(3)
13 DO 24 J1=1,MSIZE
      K2=J1+MD
      L=L1+J1
      I2=I+MD
      G(3)=HTRUE(J1)
      HTRUE(J1) = H(L) + G(2)*HTRUE(K2) - G(1)*HTRUE(J1)
      HTRUE(K2)= H(L2)- G(1)*HTRUE(K2)-G(2)*G(3)

24 CONTINUE
25 CONTINUE
I=0
CALL NORM ( HTRUE,HTRUE, MSIZE, G, 1, MD, NC, 1)
11 J1 = 1
12 = 1
L4 = MODE
DO 43 I=1,MSIZE
   I1=J1
   I2=J2
   I3=K1+1
   DO 33 MM=1,MODE
      IF ( I-INDIS(MM) ) 33,39,35
CONTINUE
43 DO 37 J=1,MSIZE
      DO 35 MM=1,MODE
         IF ( J-INDIS(MM) ) 35,37,35
CONTINUE
U(L1) = U(I2) - H(I3)*US(L4)
GOTO (3H,3K),NC
56 J3= L1+MD
J4= L2+MD
J5= L4+MD
J6= L3+MD
U(J3)=U(J4)-H(I3)*US(J5) - H(J6)*US(L1)
U(L1)= U(I1) + H(J6)*US(J5)
58 CONTINUE
I1=L1+1
I2=L2+1
I3=L3+1
GOTO 41
59 IF ( I-INDIS(MODE) ) 43,42,43
41 J1=J1+NN
42 J2=J2+NN
43 I4=L4+NN
I4=(MSIZE-MODE)*NN+1
DO 52 J=1,NC
   I4 = I4 + (J-1)*MD
I1=I4+(MSIZE-MODE)-1
DO 52 I=L4+1
52 U(I)=0.
RETURN
END
FORTRAN 1STO1.DCK
C CHANGES
SUBROUTINE CHANGE (A,M,N,MAXR,ICHUZ)
DIMENSION A(1)
NR=2*MAXR
BO 10 (1N,2N) ,ICHUZ
10 DO 12 I=1,N
   K=(N-1)*MAXR+M+1
                                MTR41283
                                MTR41284
                                MTR41285
                                MTR41286
                                MTR41287
                                MTR41288
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                                MTR41343
                                MTR41345
                                MTR41346
                                MTR41347
                                MTR41348
                                MTR41349
                                MTR41350

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KK=(N-1)*MR+2*M+1          MTR41351
DO 12 J=1,M                  MTR41352
  IGET=K-J                   MTR41353
  IPUT=KK-2+J                 MTR41354
  A(IPUT)=A(IGET)             MTR41355
12   A(IPUT+1)=0.              MTR41356
    GO TO 100                 MTR41357
20 K=0                         MTR41358
  KK=0                         MTR41359
  DO 24 I=1,N                  MTR41360
    DO 22 J=1,M                  MTR41361
      IGET = KK+2+J-1           MTR41362
      IPUT=K+J                  MTR41363
22   A(IPUT) = A(IGET)         MTR41364
      K=K+MAXR                  MTR41365
24   KK=KK+MR                  MTR41366
100 RETURN                      MTR41367
  END                         MTR41368

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S E C T I O N 9

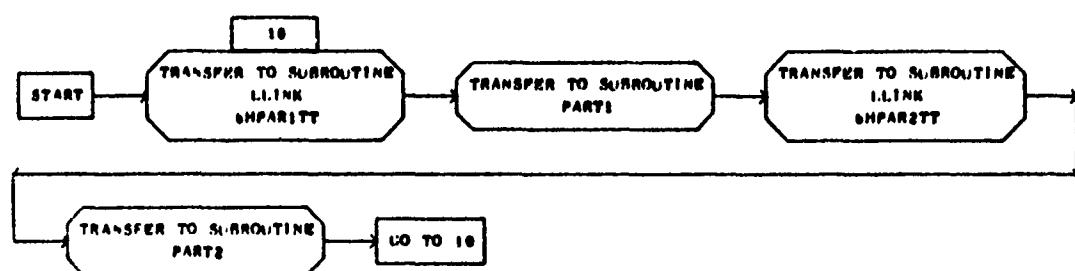
F L O W D I A G R A M S

MAIN PLUTTER OVERLAY

JAN 11, 1967

COMMON IT(216)

PAGE 1



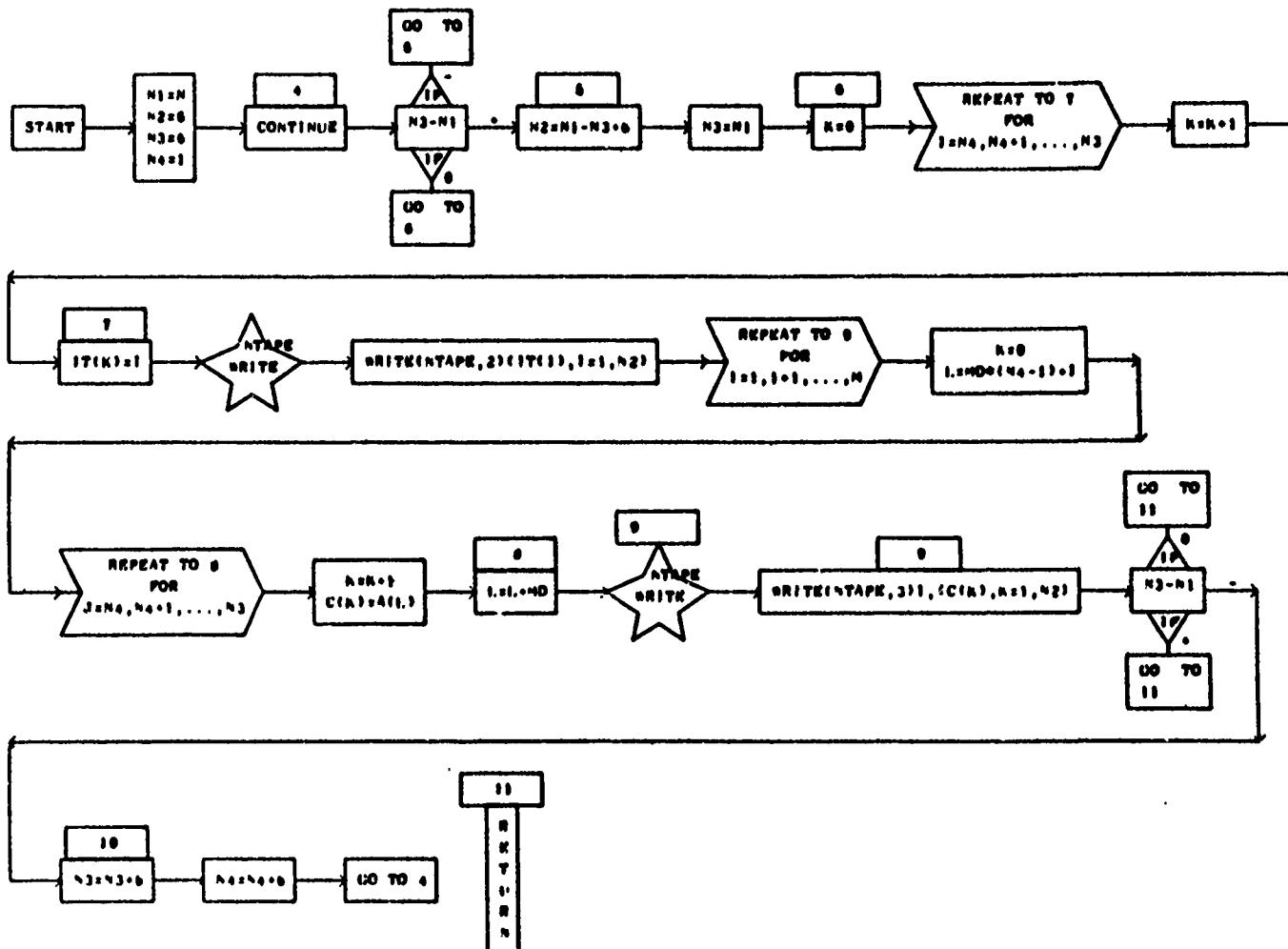
MPRINT

DIMENSIONED : VARIABLES

SYMBOL	STORAGES								
A	1	I	17	S	0	C	0	K	0

SUBROUTINE MPRINT (A,N,N1,ND,NTAPE)

PAGE 1



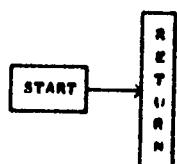
MPUNCH

DIMENSIONED VARIABLES

SYMBOL	STORAGES								
A	I								

SUBROUTINE MPUNCH(A,M,N,IOUT,ITRA,ITOD,RCDZ,MAXM,NTAPE,NCARDS)

PAGE 1



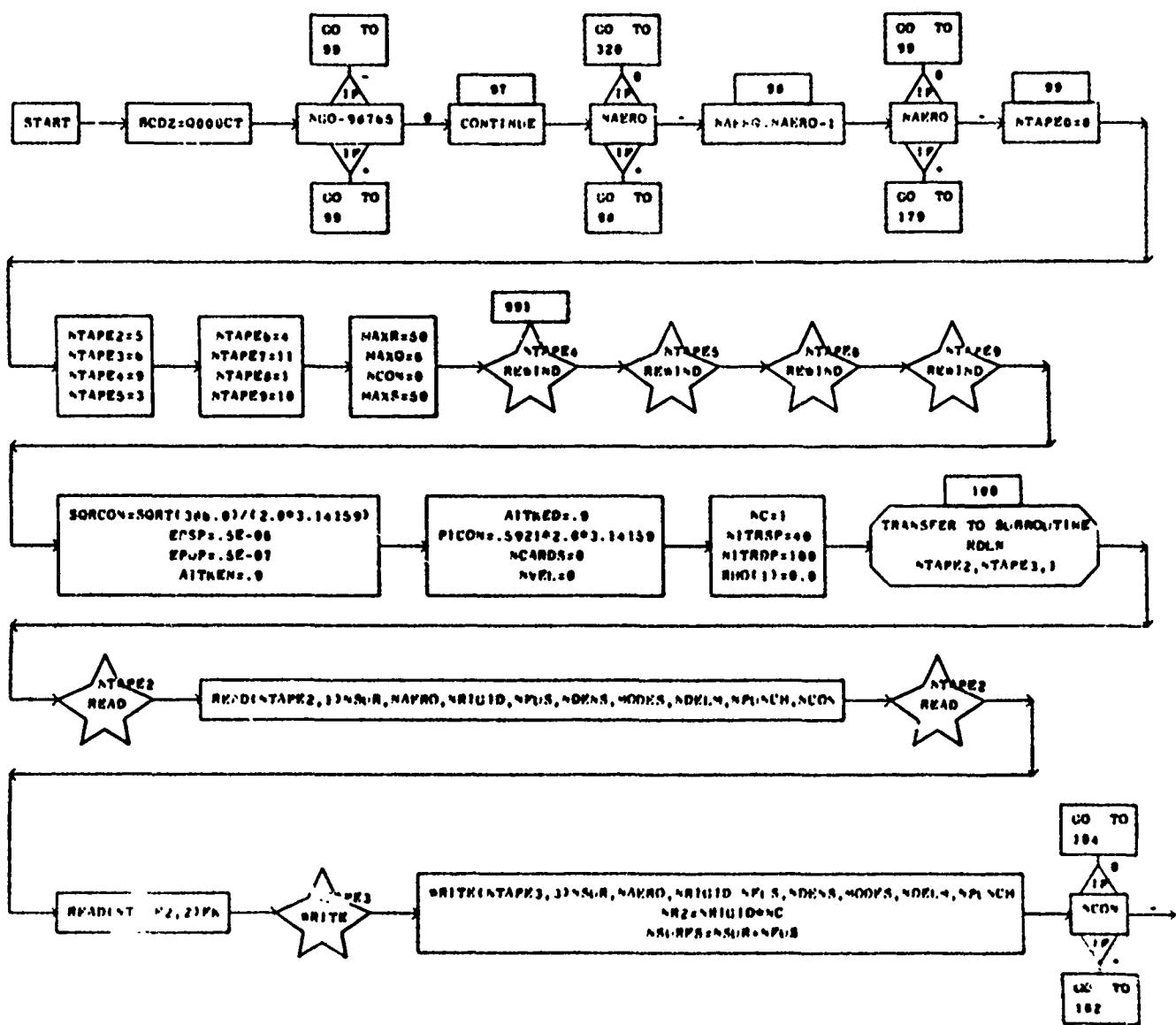
## PARTS

## DIMENSIONED VARIABLES

SYMBOL	STORAGES								
ISXST	20	ISG	20	BR	21	S	21	RWD	20
DH	0,0	DO	0,12	DMEAR	0,12	RARMR	0,12	LOG	00
IHIGH	50	IT	310	VRLCTY	20	NSIZES	20	A	50,100
P	50,100	U	5,100	NR	50,0	HRT	0,100	HY	0,100
G	0,100								

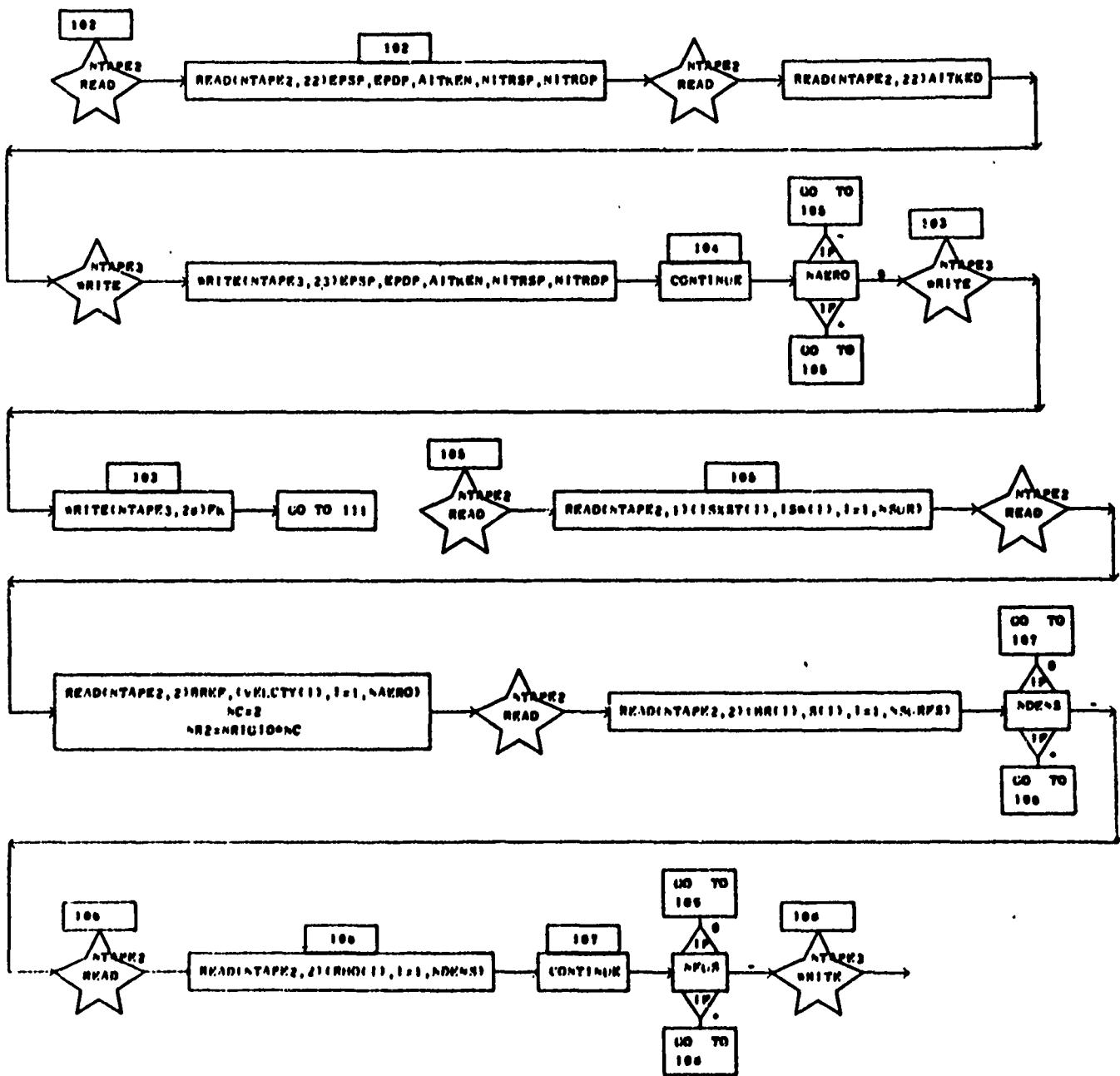
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PAGE 1



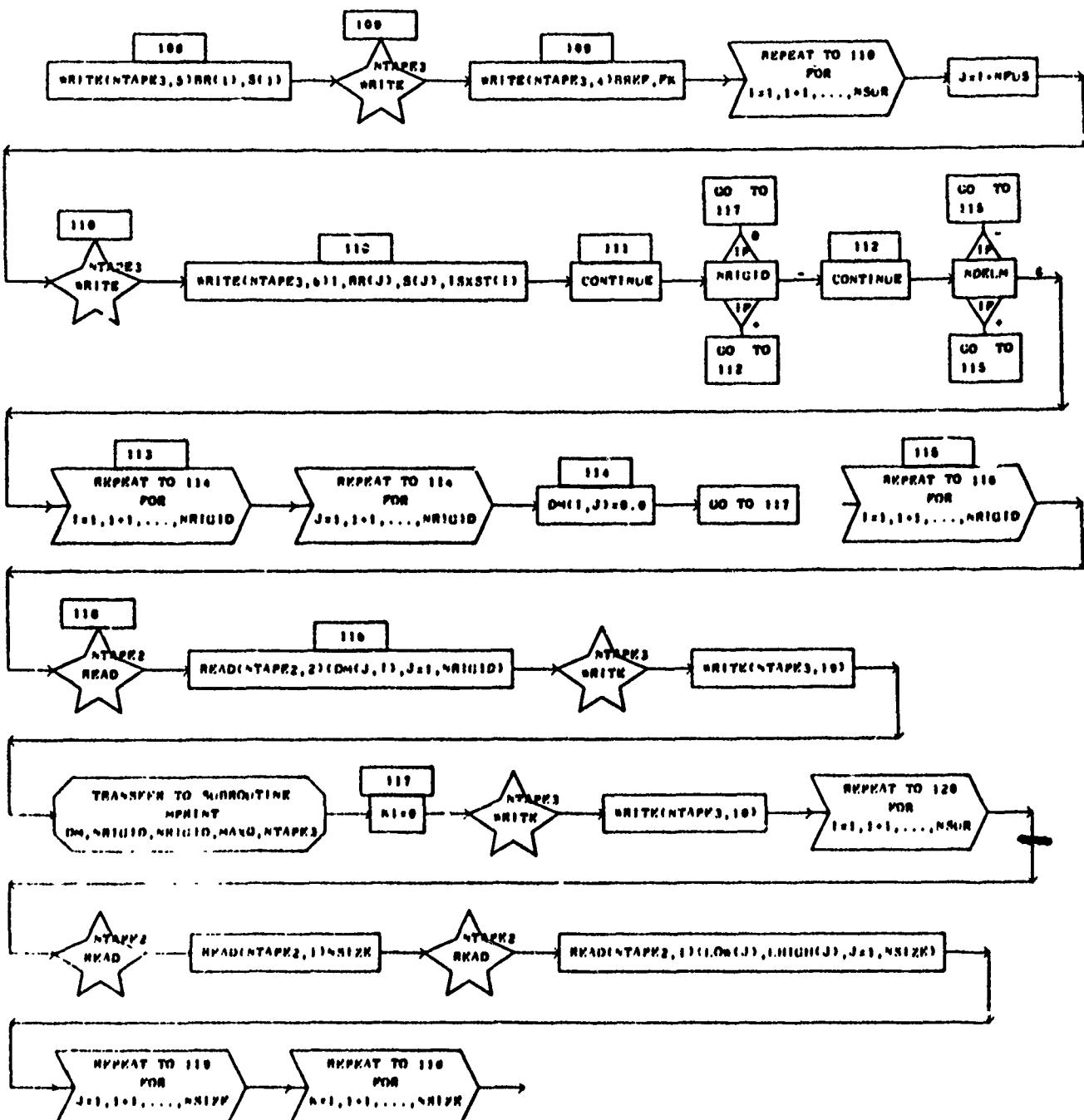
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PAGE 2



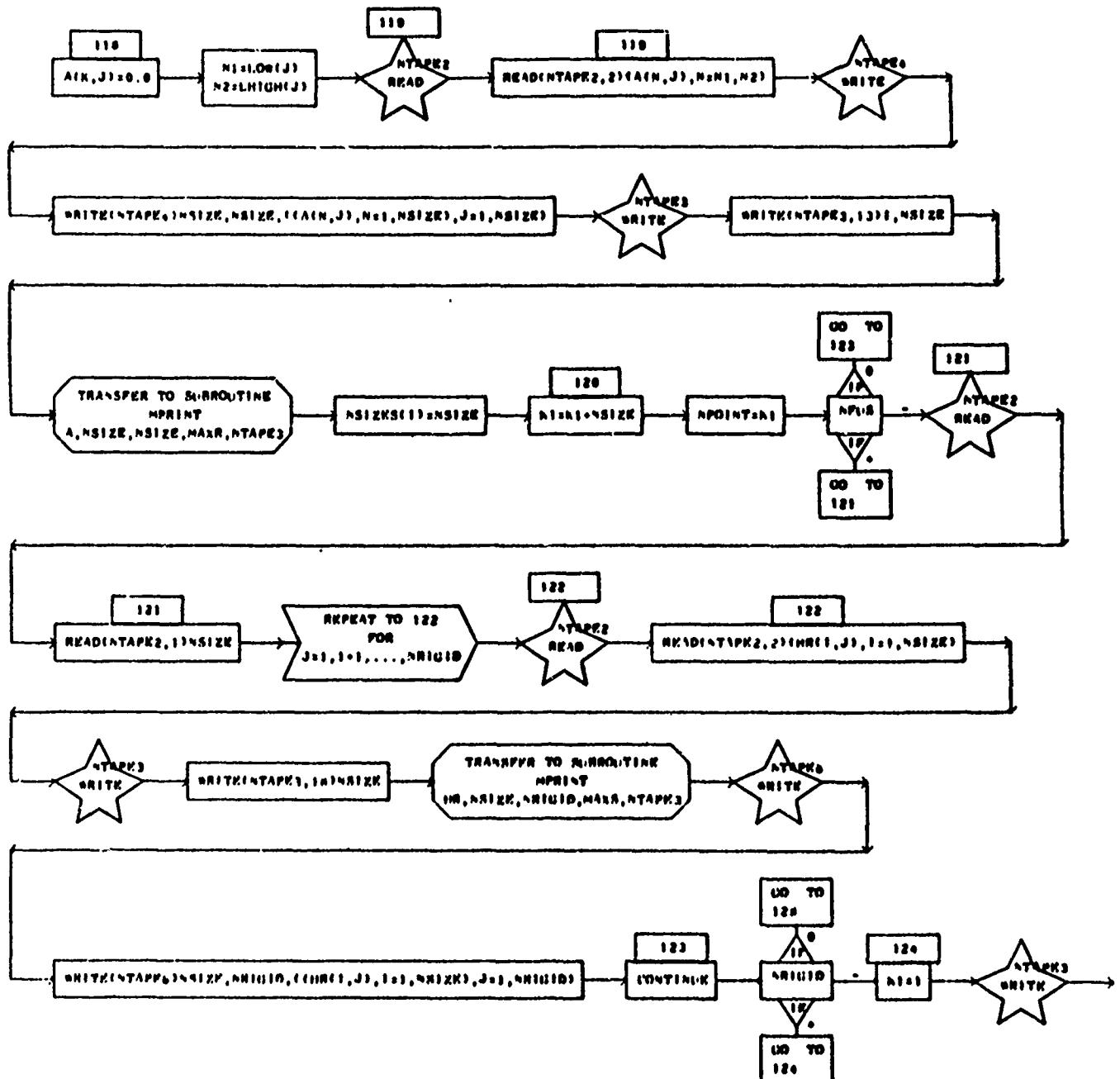
## SUBROUTINE PARTS

PAGE 3



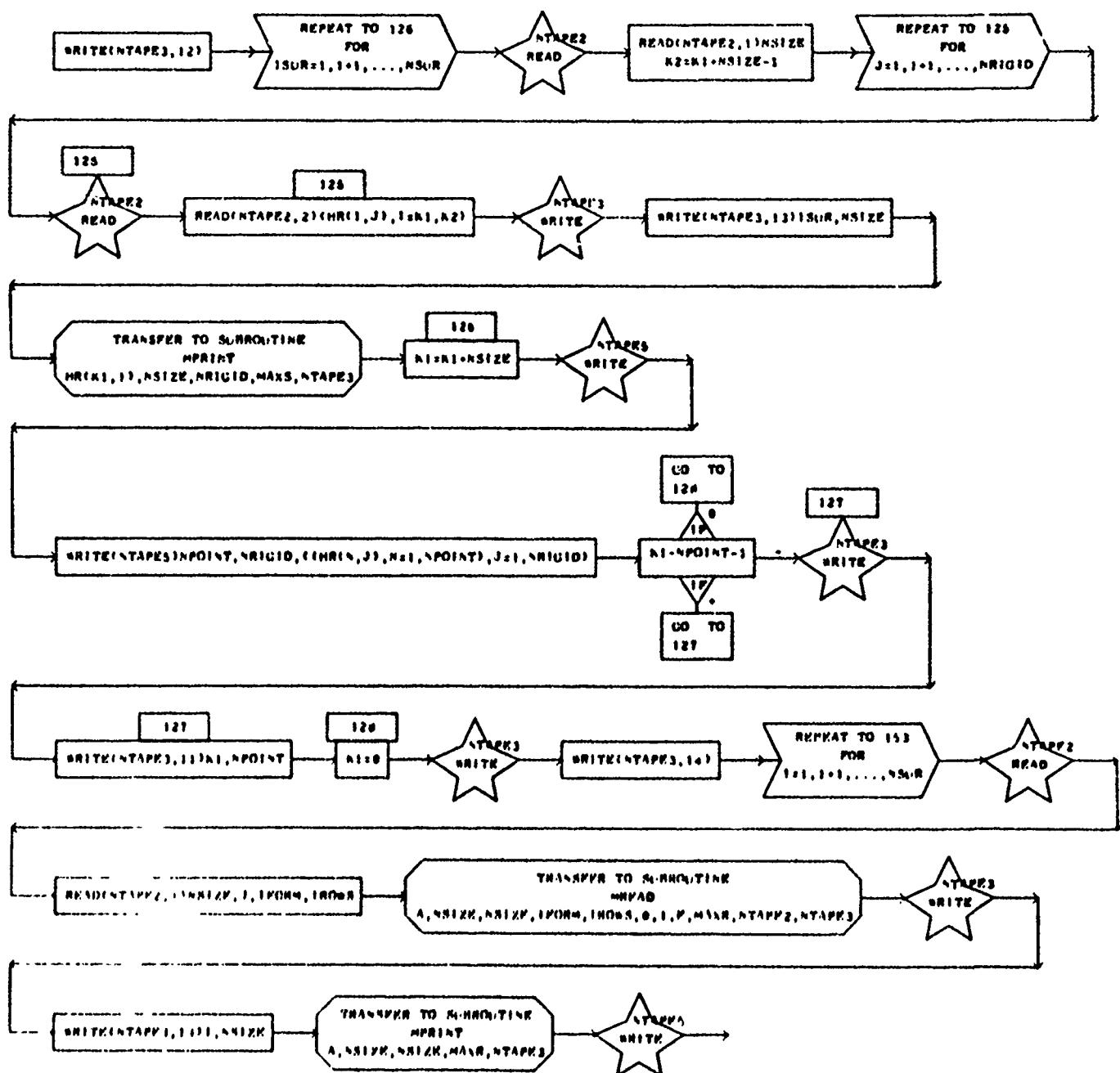
## SUBROUTINE PART I

PAGE 4



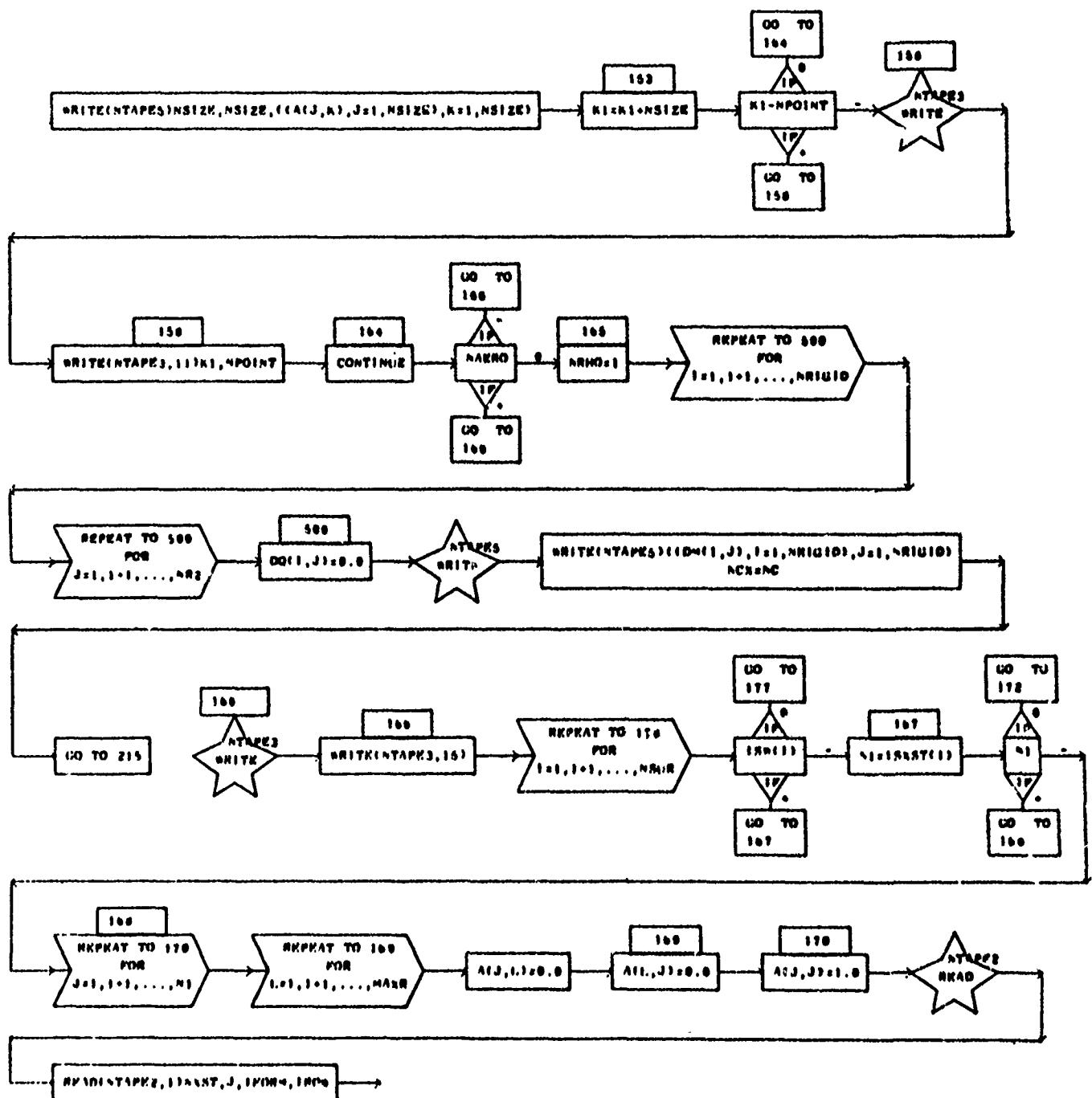
## SUBROUTINE PARTS

PAGE 5



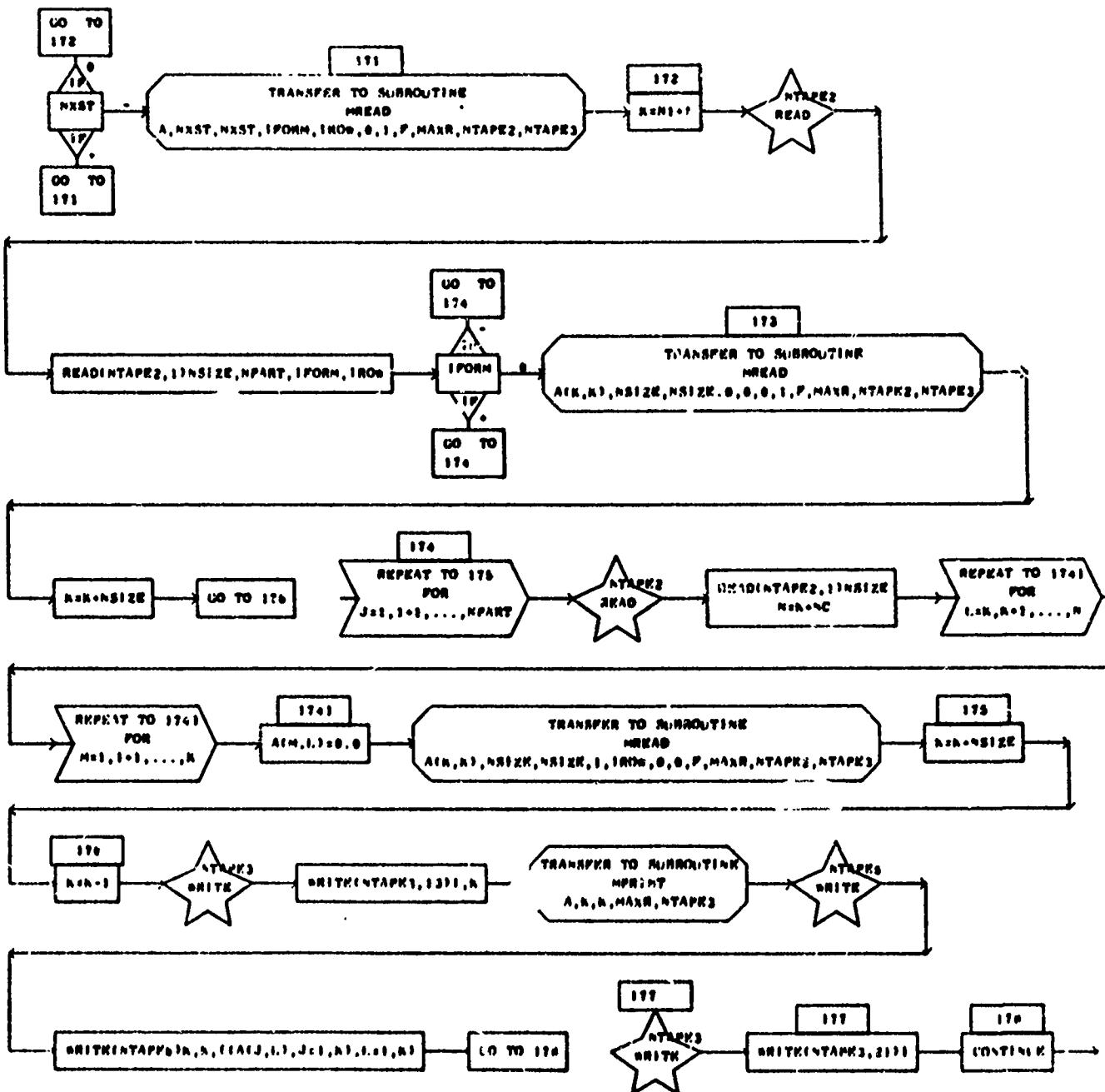
## SUBROUTINE PARTS

PAGE 6



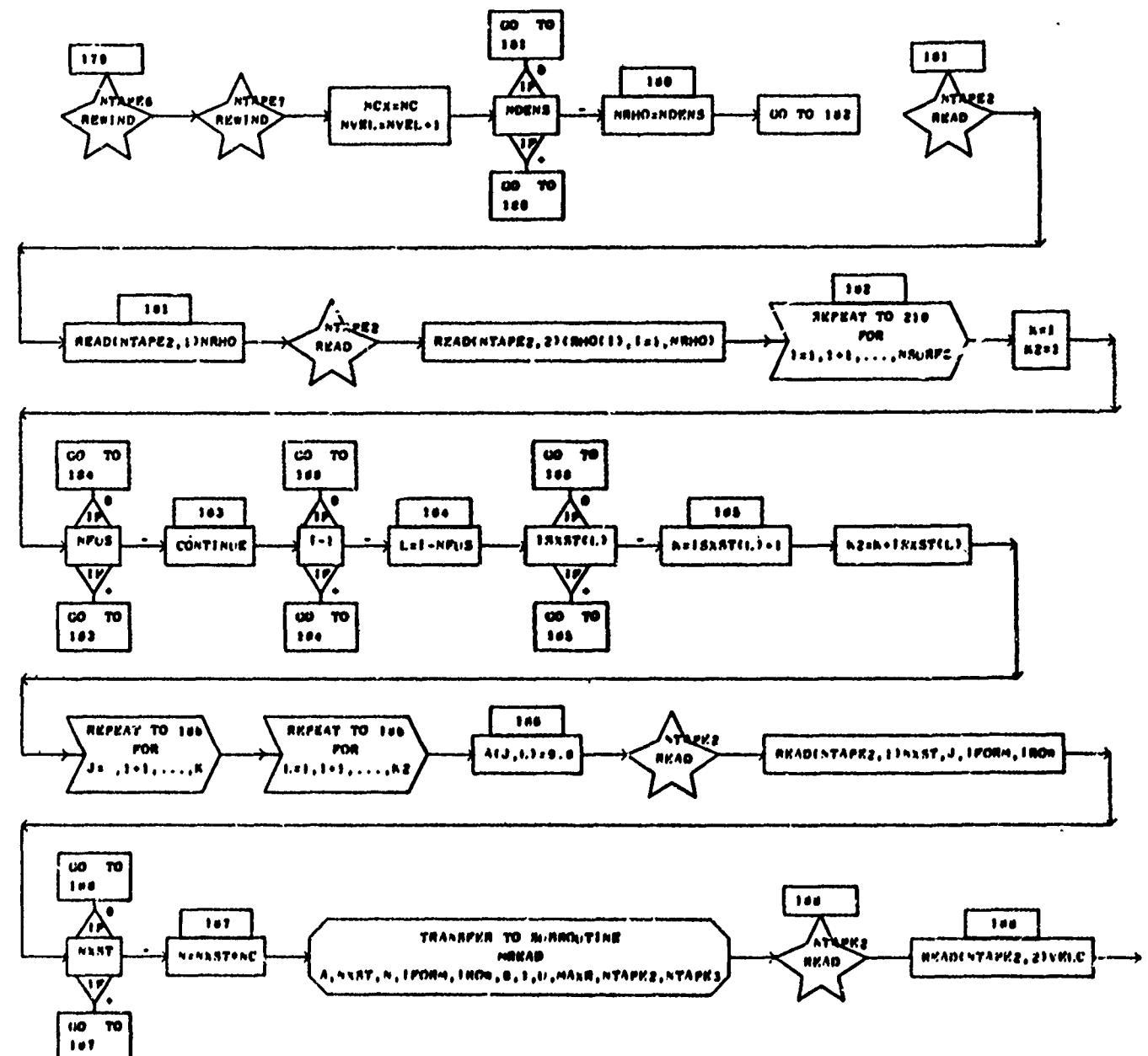
## SUBROUTINE PARTS

PAGE 7



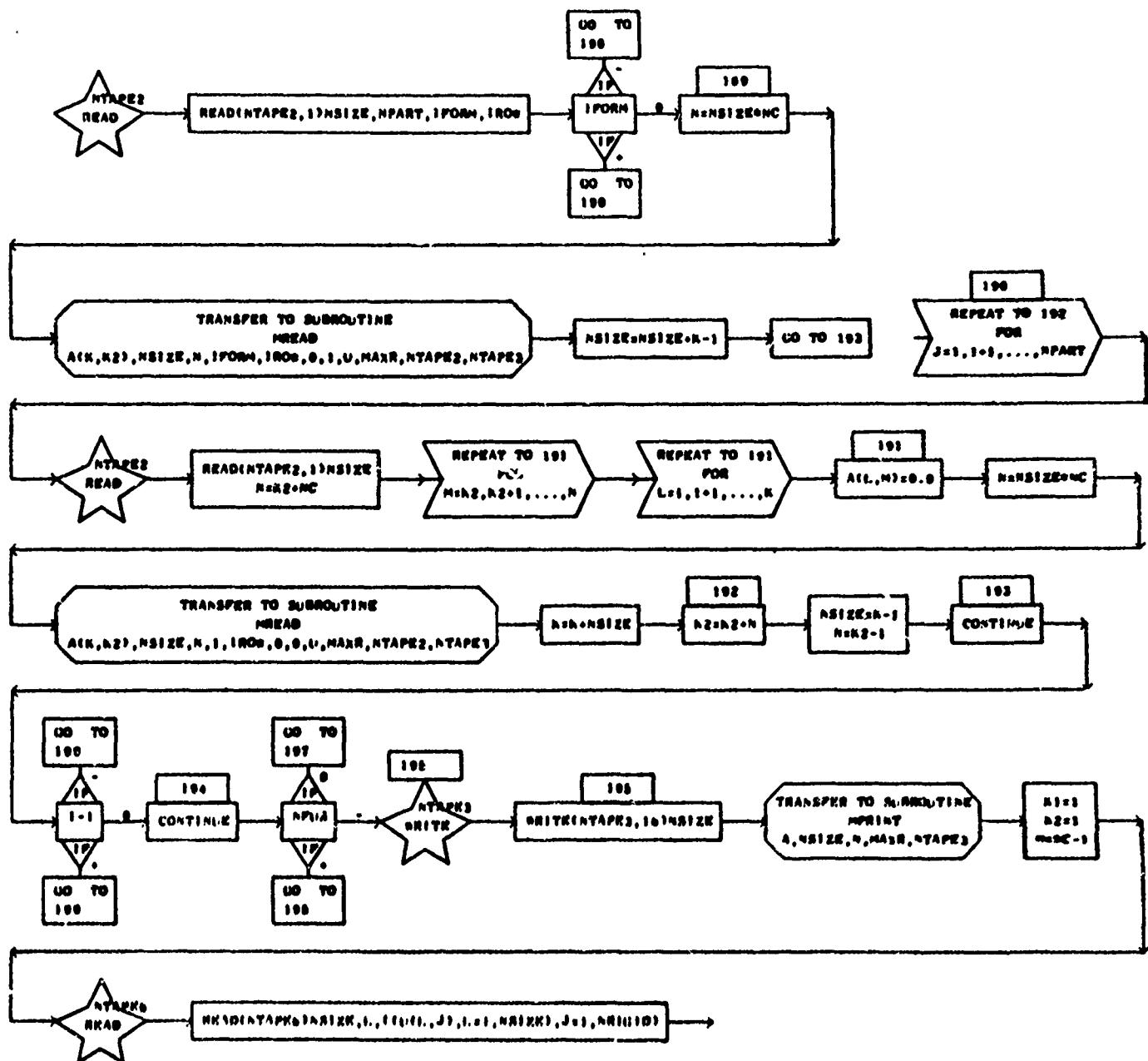
## SUBROUTINE PARTS

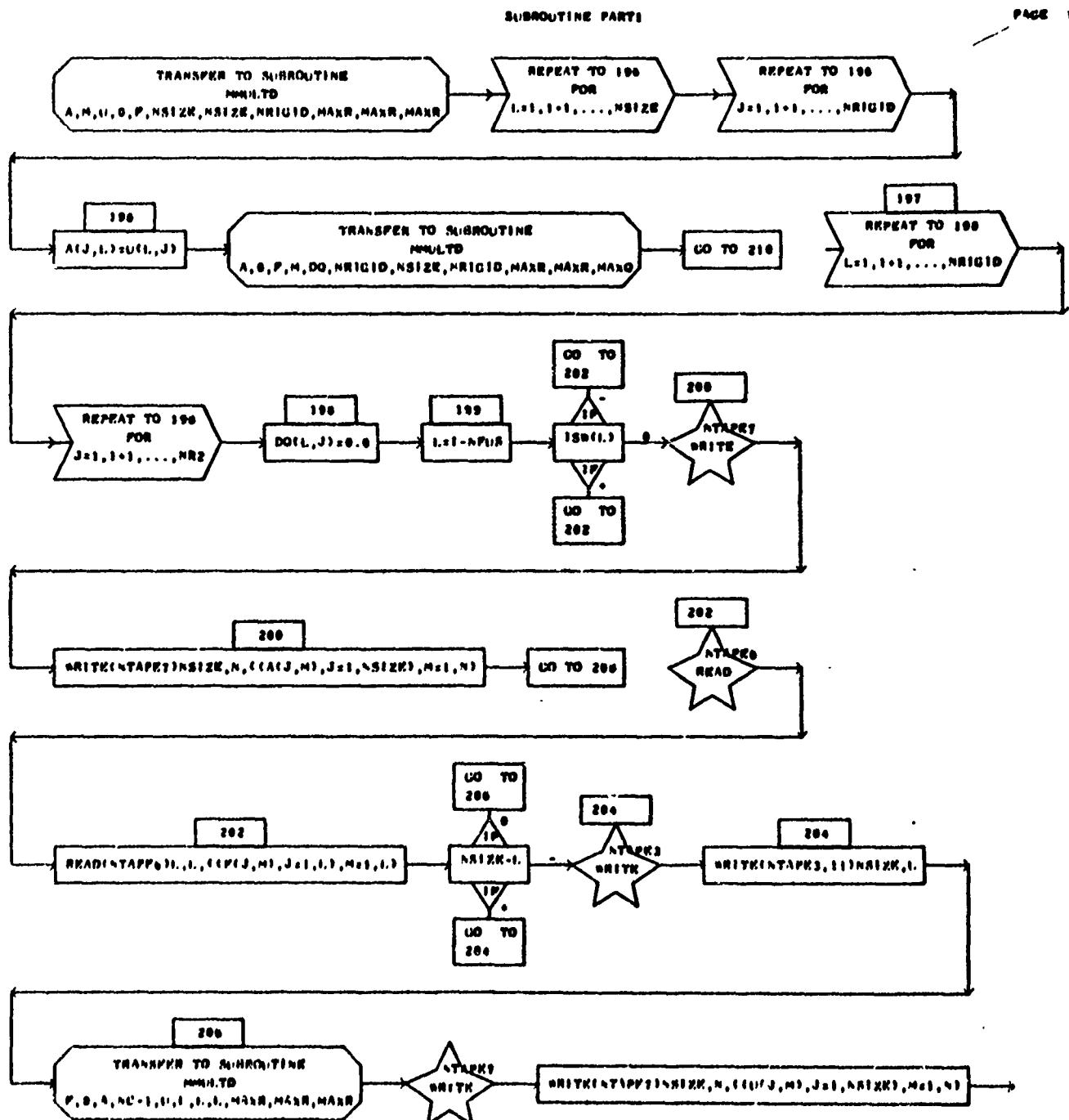
PAGE 6



## SUBROUTINE PARTS

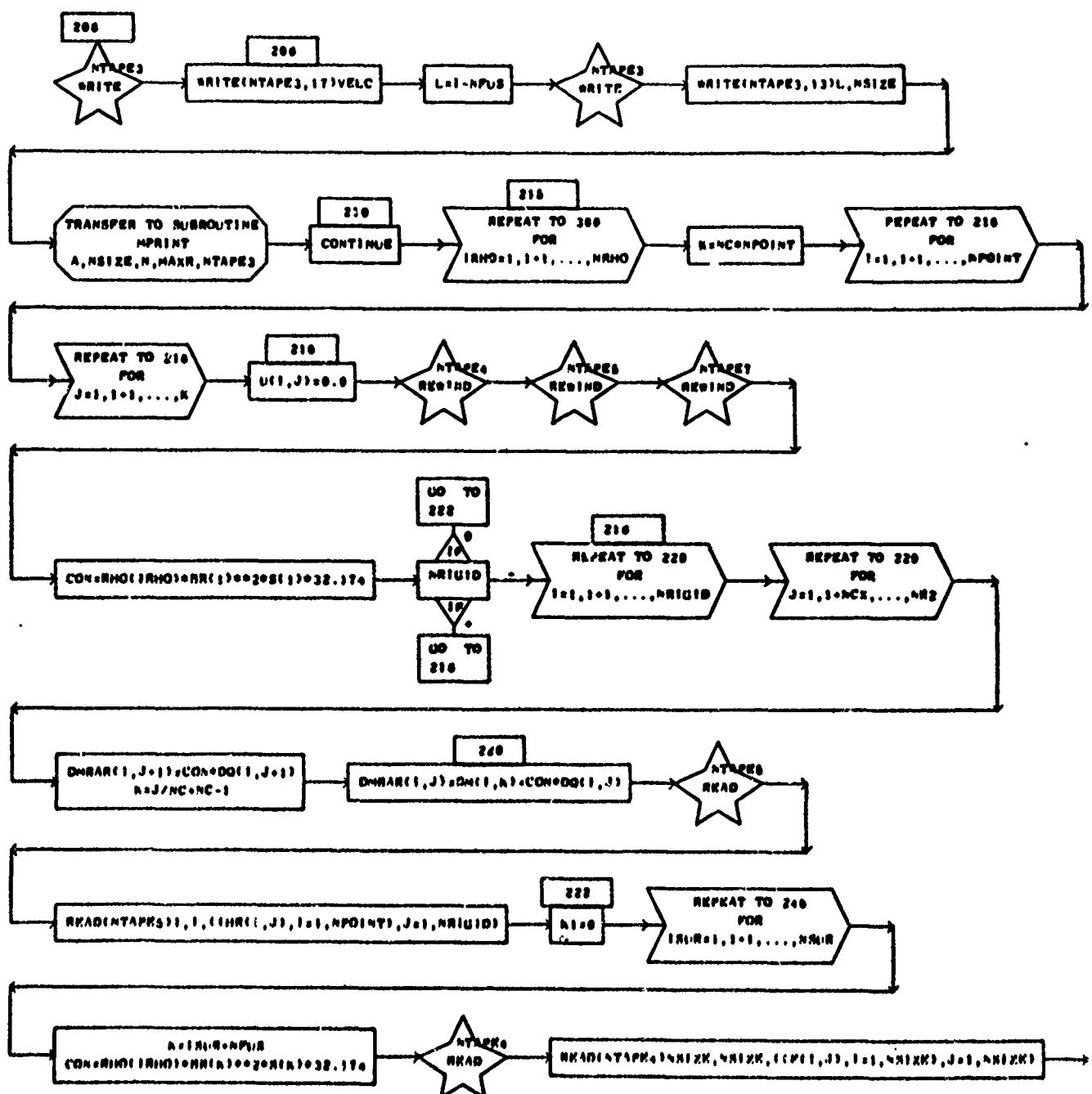
PAGE 9





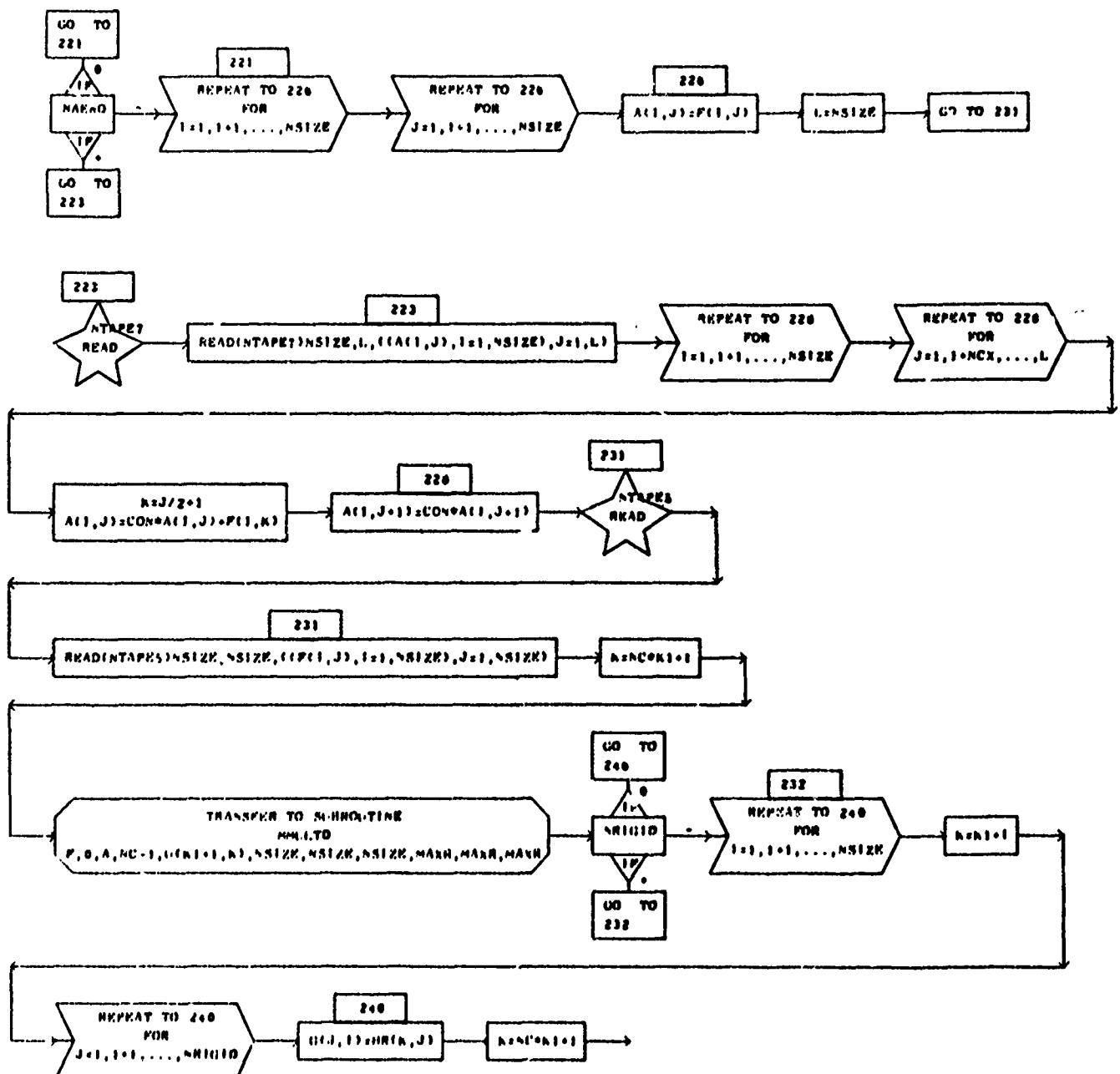
## SUBROUTINE PARTS

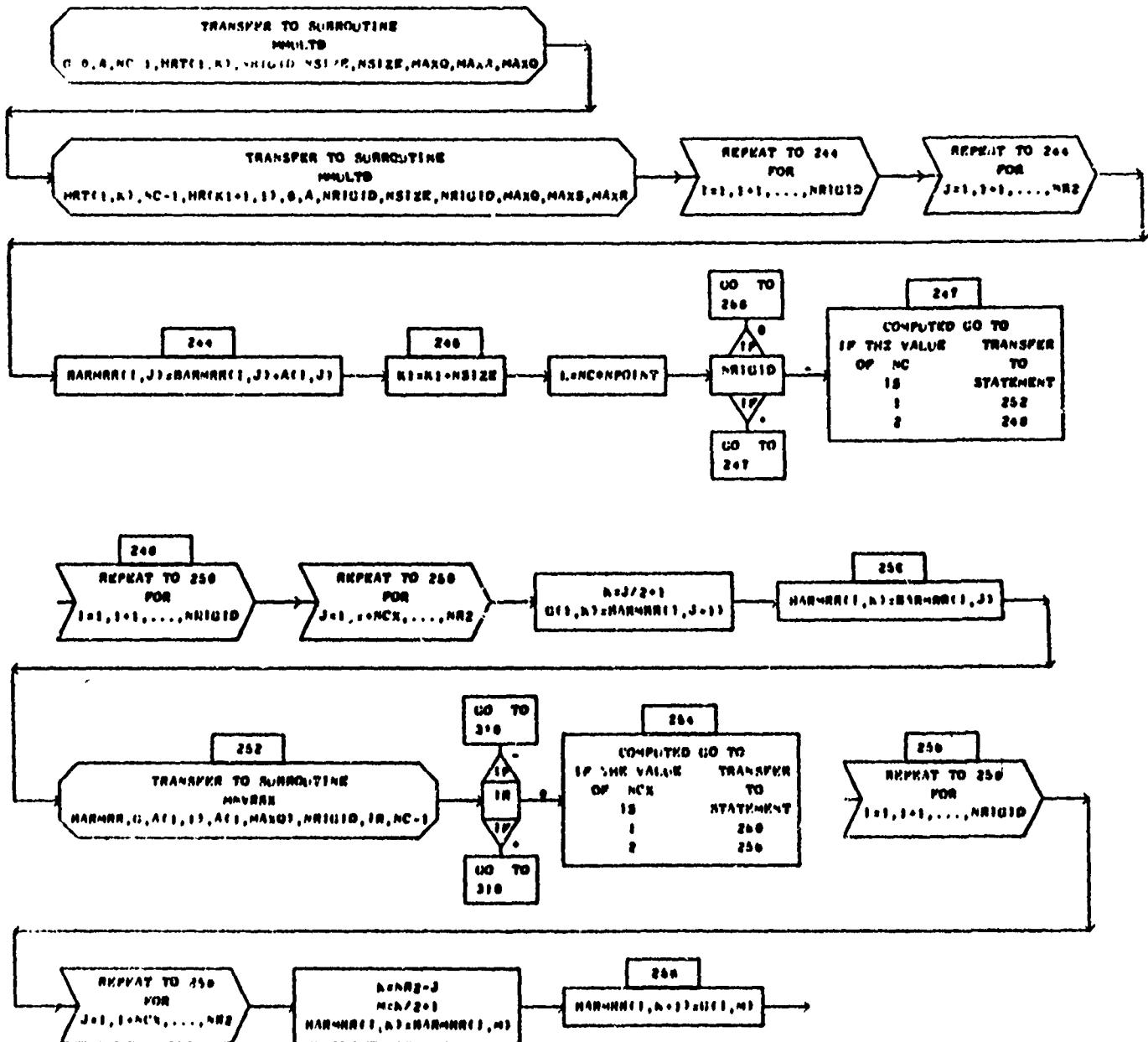
PAGE 11

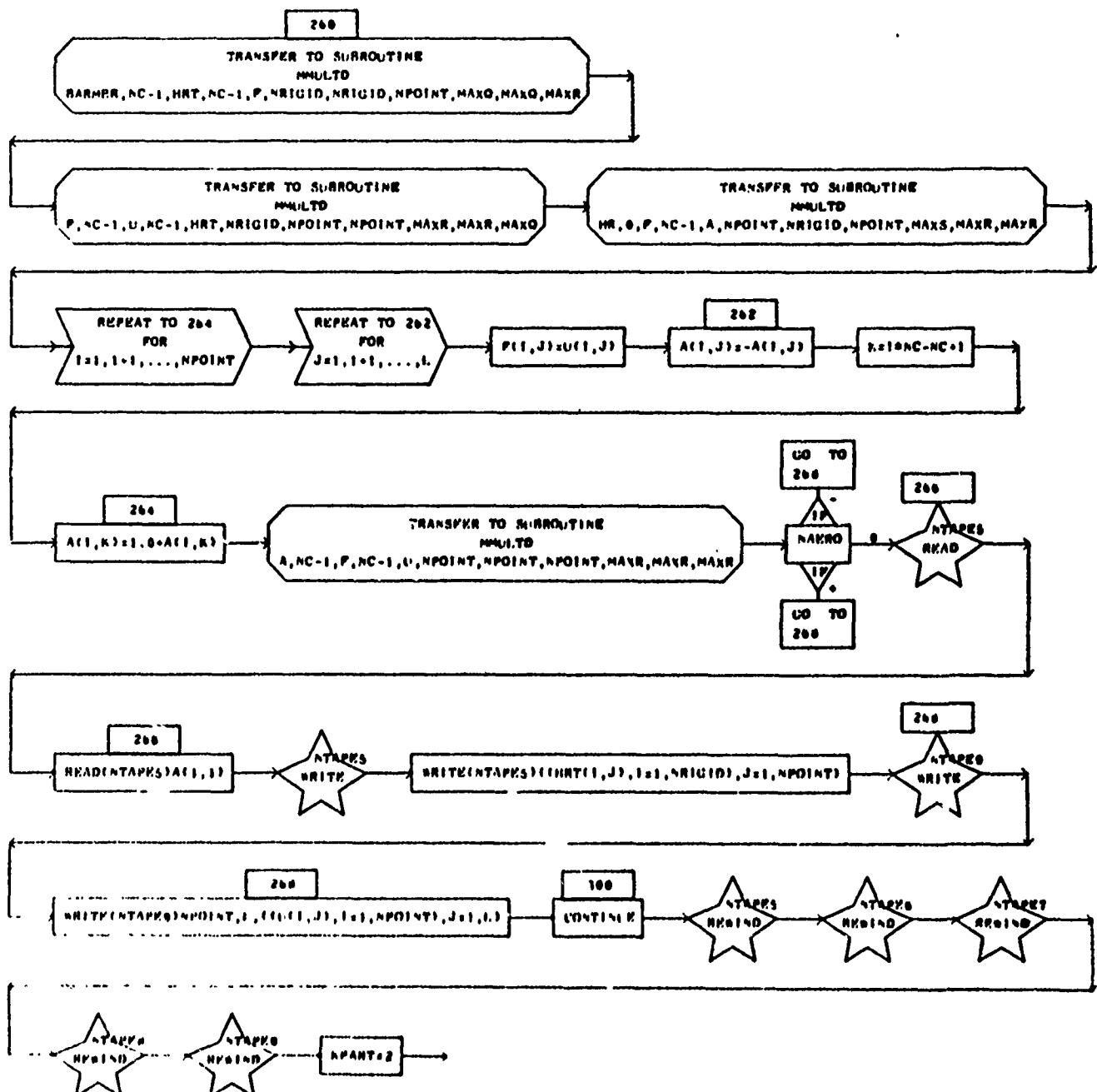


## SUBROUTINE PARTS

PAGE 12

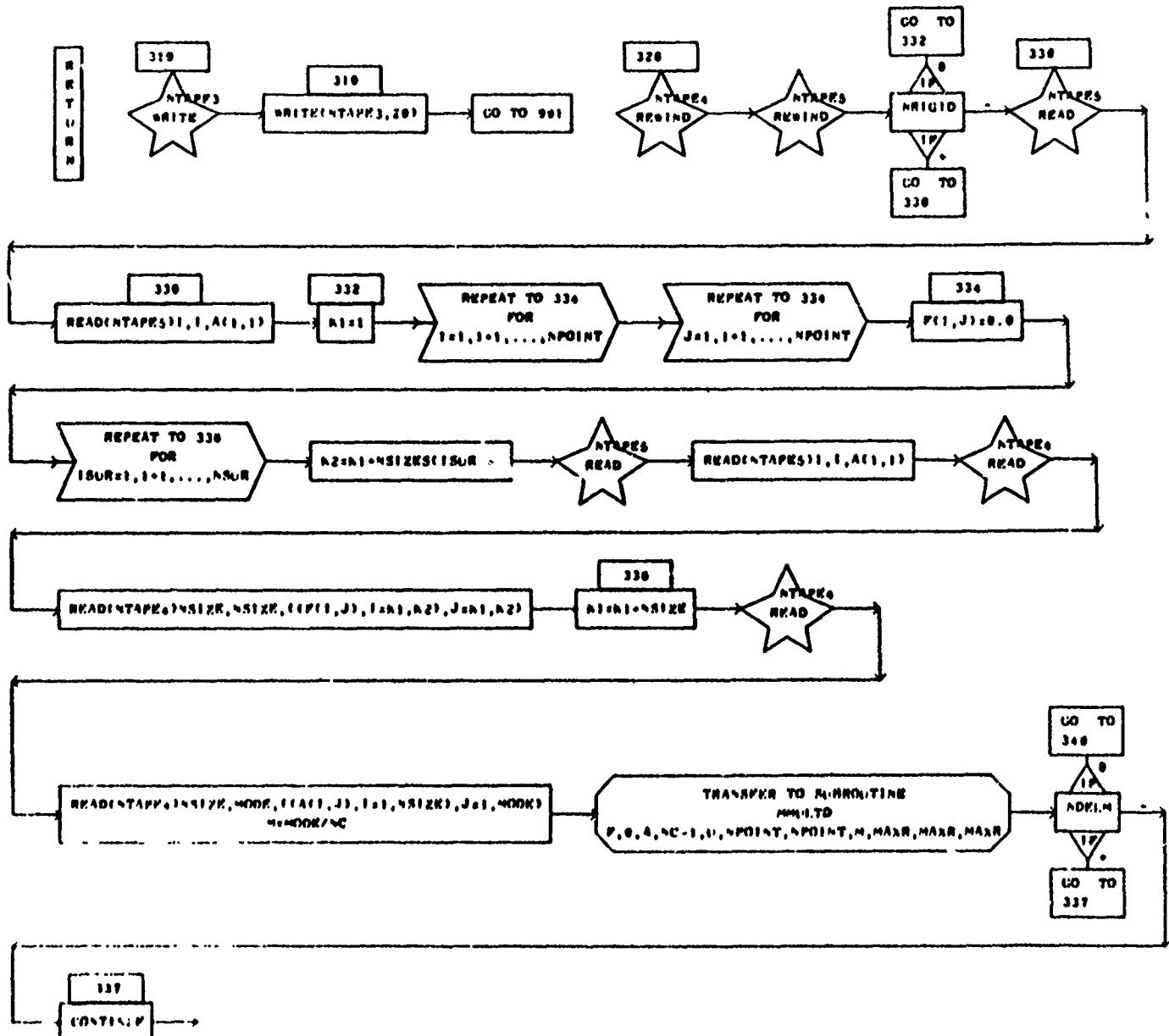






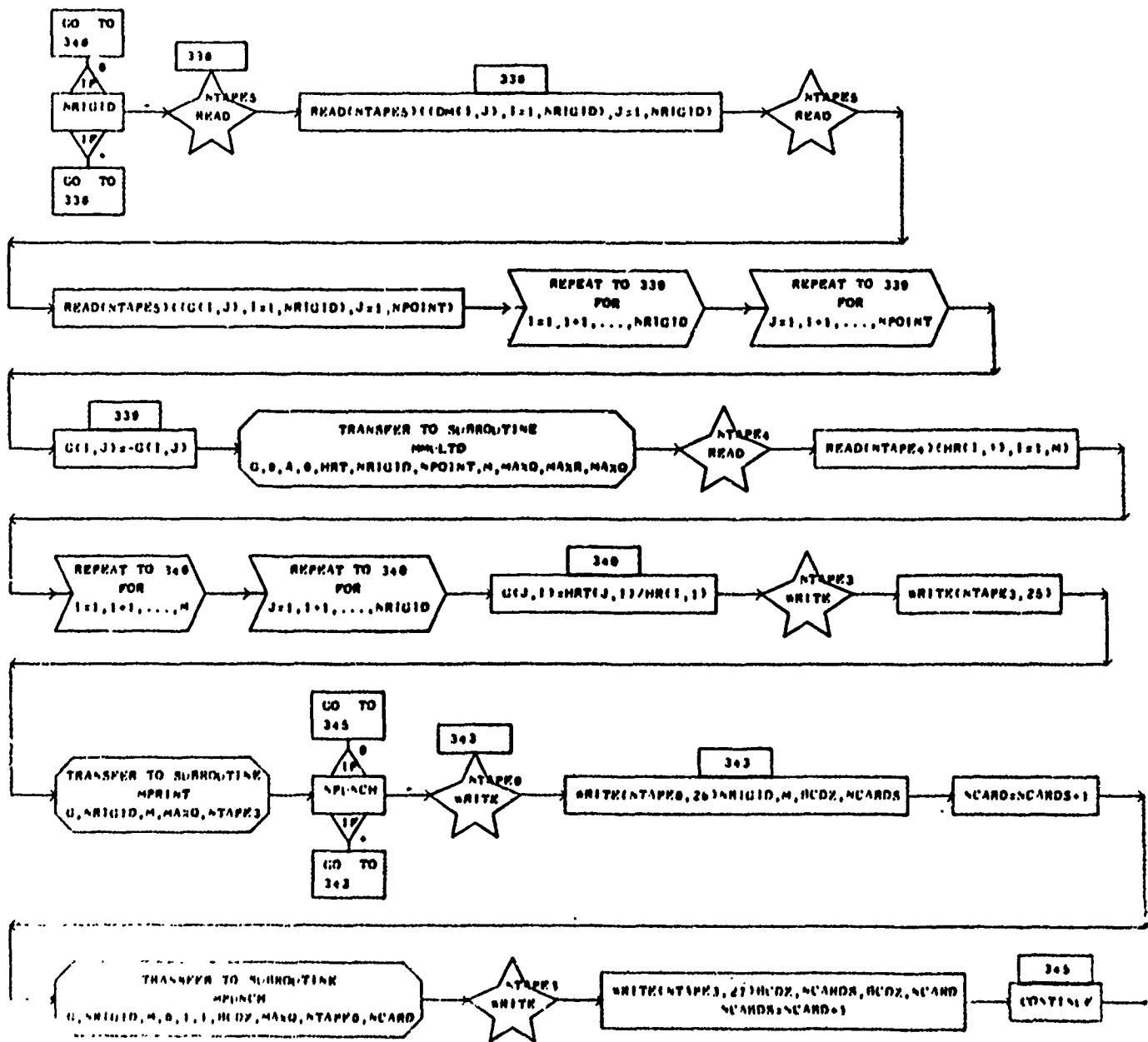
## SUBROUTINE PARTS

PAGE 15



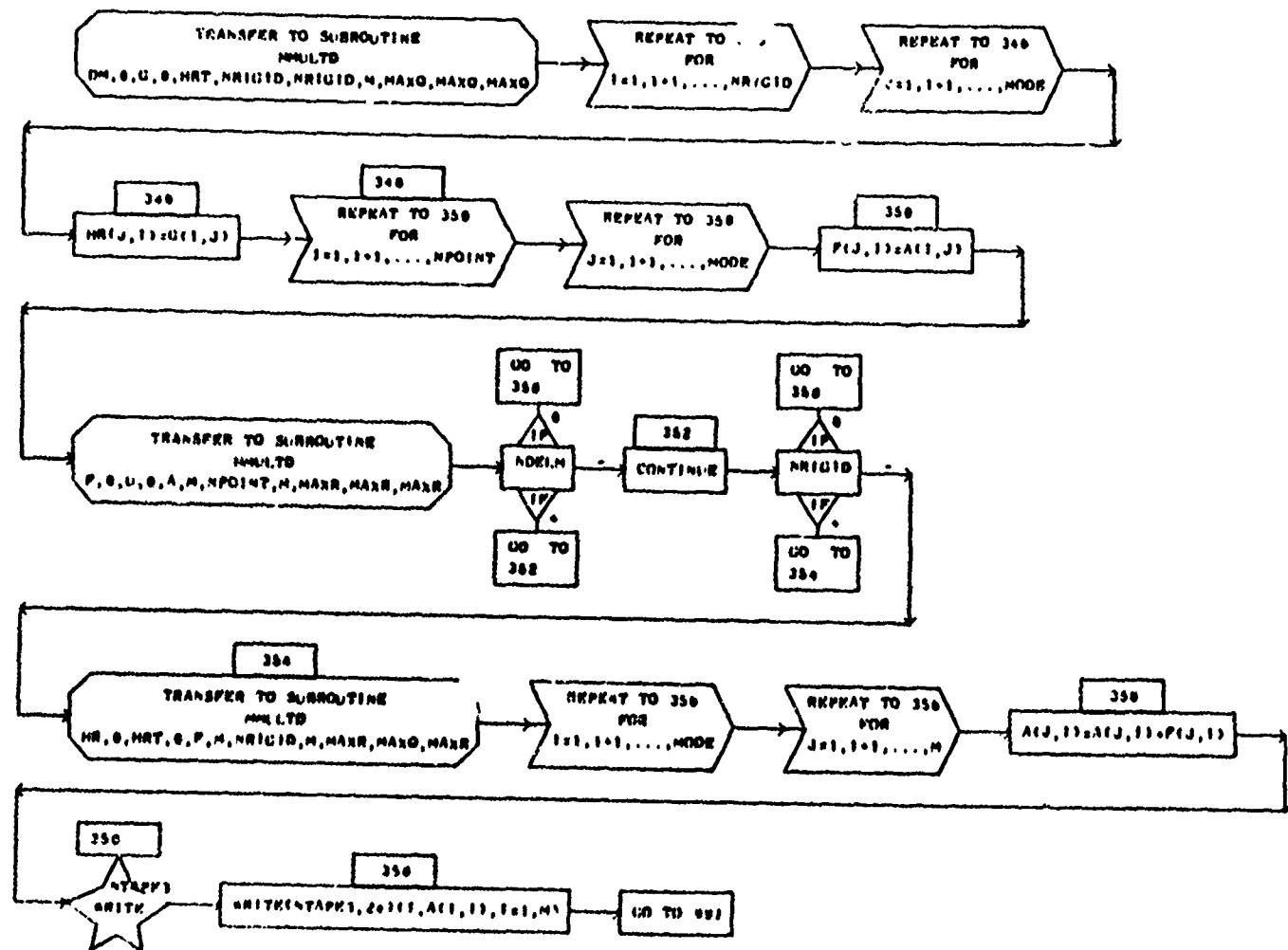
## SUBROUTINE PART I

PAGE 16



## SUBROUTINE PAP--

PAGE 17



MREAD  
MRAD  
MATRIX READ SUBROUTINE  
CALL MREAD (A,N,M,IPRM,IRW,ITRA,ITOU,T,MD,NTAPR2,NTAPR3 )

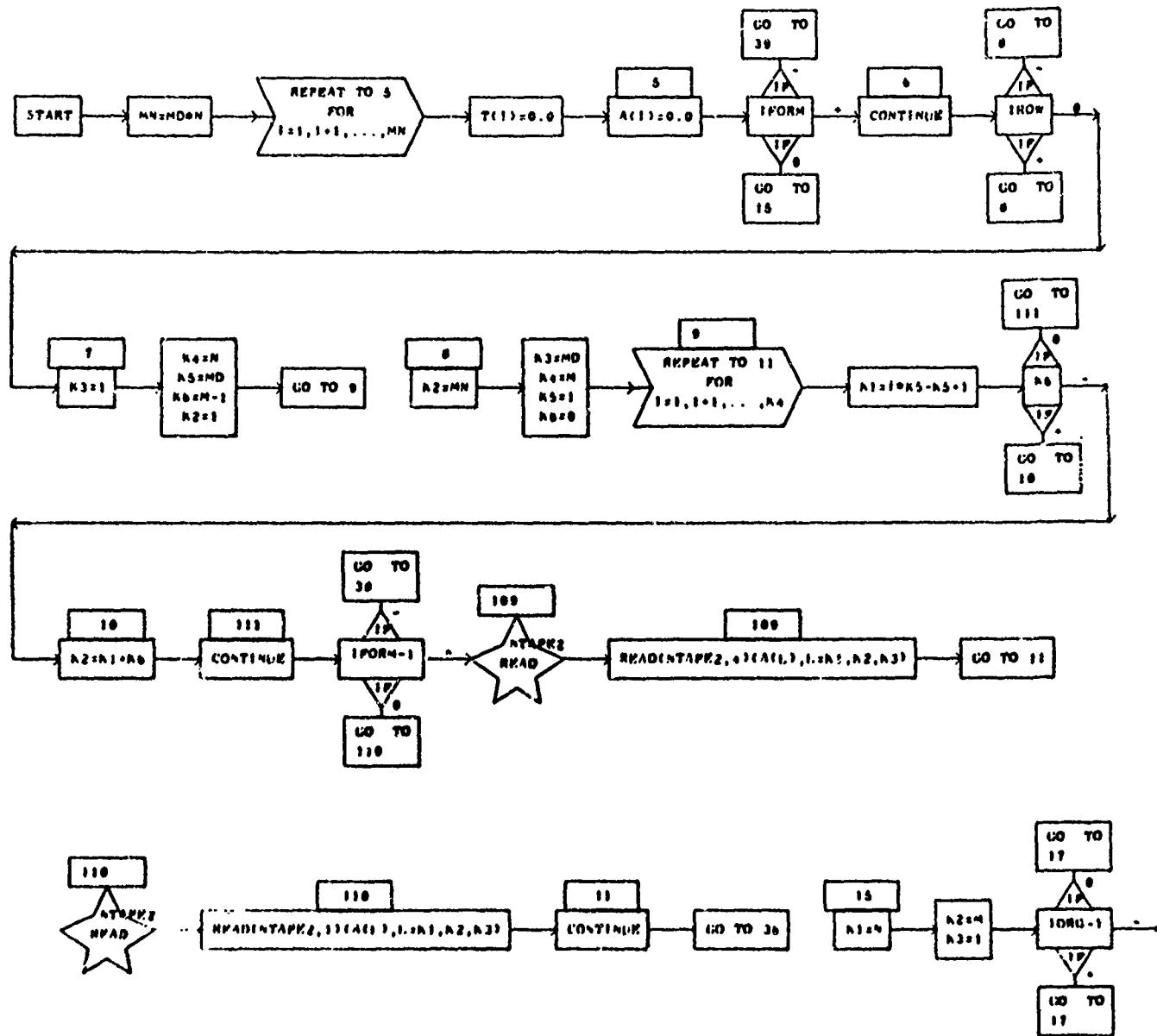
A = MATRIX TO READ IN ITRA = 0, TRA CARD AFTER MATRIX  
M = NUMBER OF ROWS 0+1, TRA CARD AFTER EACH ROW  
N = NUMBER OF COLUMNS FOR COLUMN I  
IPRM = -1, FORMAT(12A8) ITOU = ORIGIN OF FIRST C.B. CARD  
= 0, COLUMN BINARY T AND IN TEMPORARY CELLS  
= +1, FORMAT(5E12.6) MD = DIMENSIONED NUMBER OF ROWS  
IRW = .0, MATRIX BY COLUMNS IN A  
= +1, MATRIX BY ROWS NTAPR2 = INPUT TAPE  
NTAPR3 = OUTPUT TAPE

DIMENSIONED VARIABLES

SYMBOL	STORAGES								
A	I	T	I						

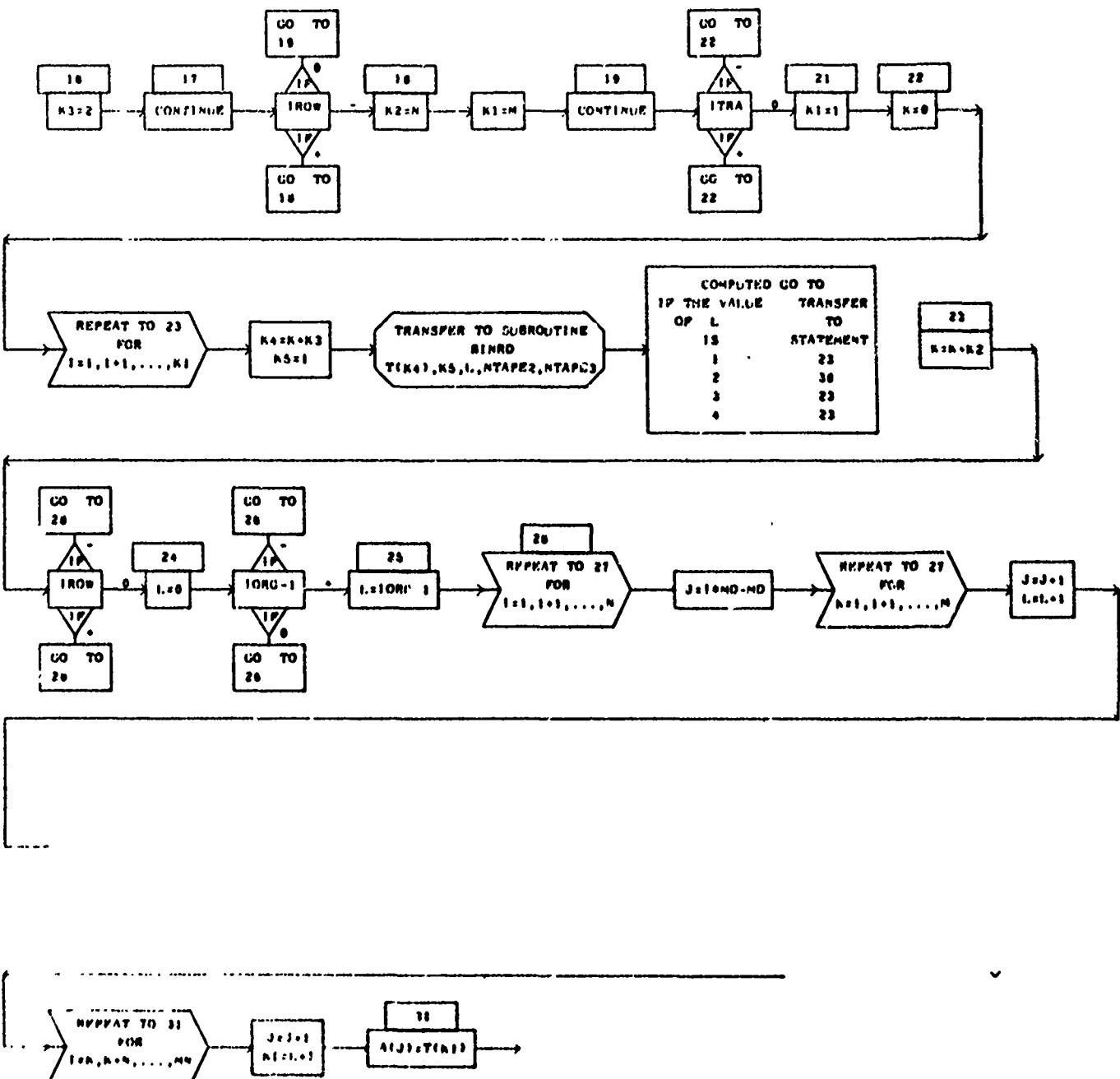
SUBROUTINE MRAD (A,M,N,IPORN,IROW,ITRA,IRU,T,MD,NTAPE2,NTAPE3)

PAGE 1



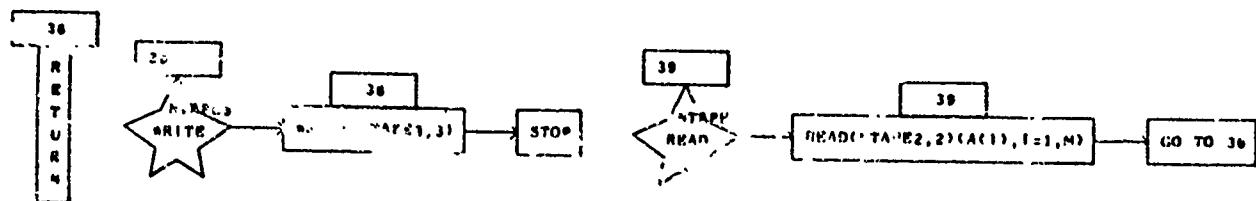
SUBROUTINE MREAD (A,M,N,IPERM,IROW,ITRA,IONU,T,HD,NTAPE2,NTAPE3)

PAGE 2



SUBROUTINE XREAD (A,M,N,IFORM,IROW,ITRA,IORU,T,MD,NTAPE2,NTAPE2) 1

PAGE 2



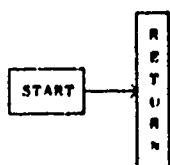
INRD

DIMENSIONED VARIABLES

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBL.	STORAGES	SYMBOL	STORAGES
T	I								

SUBROUTINE INRD (T,A,L,NTAPE1,NTAPE2)

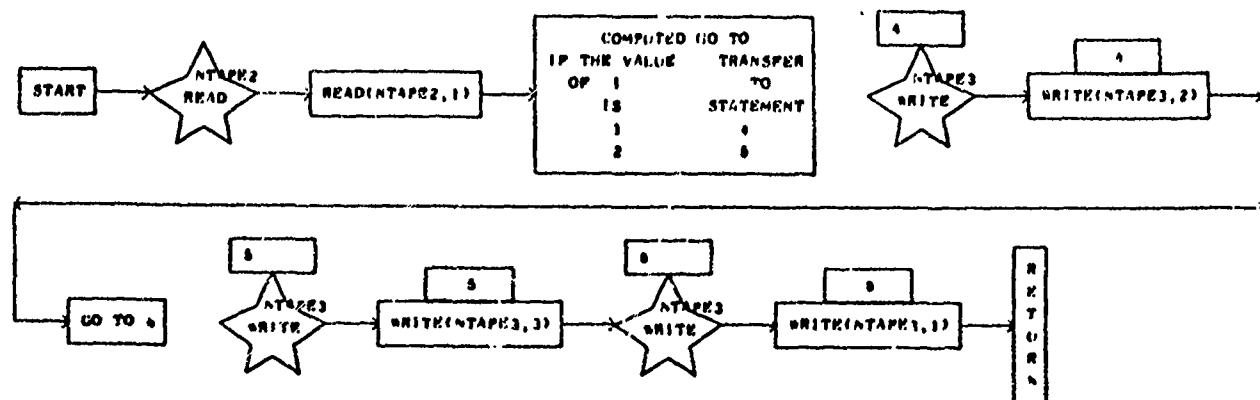
PAGE 1



RDLN

SUBROUTINE RDLN (NTAPE2, NTAPE3, I )

PAGE 1



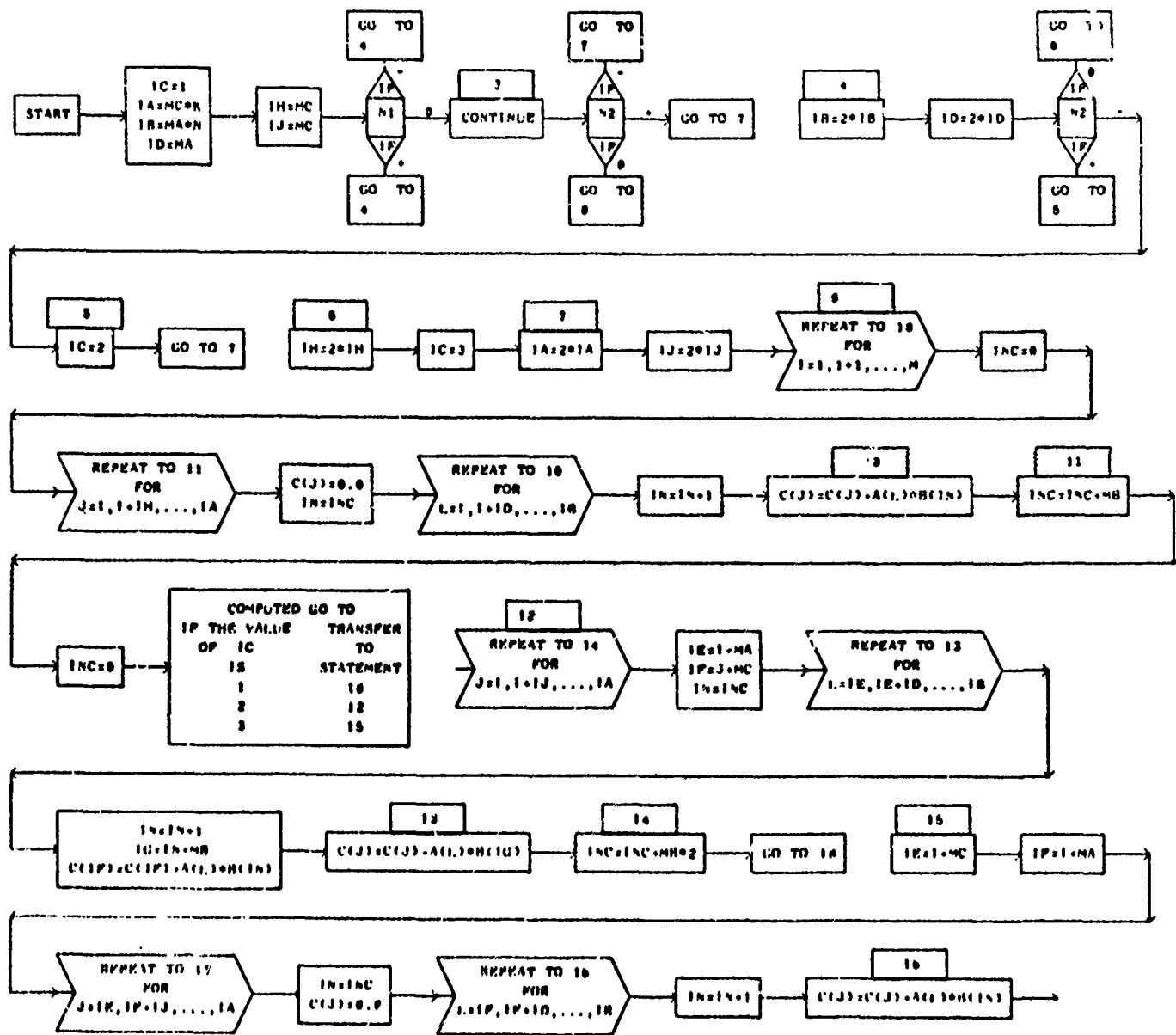
MULTO

D I M E N S I O N E D   V A R I A B L E S

SYMBOL	STORAGES								
A	I	B	I	C	I				

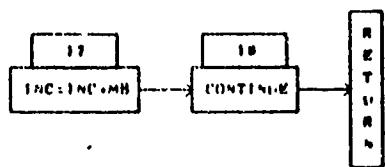
## SUBROUTINE MMULTD (A,N1,B,N2,C,M,N,K,MA,MB,MC)

PAGE 1



SUBROUTINE MMULTD (A,N1,R,N2,C,M,K,MA,MB,MC)

PAGE 2



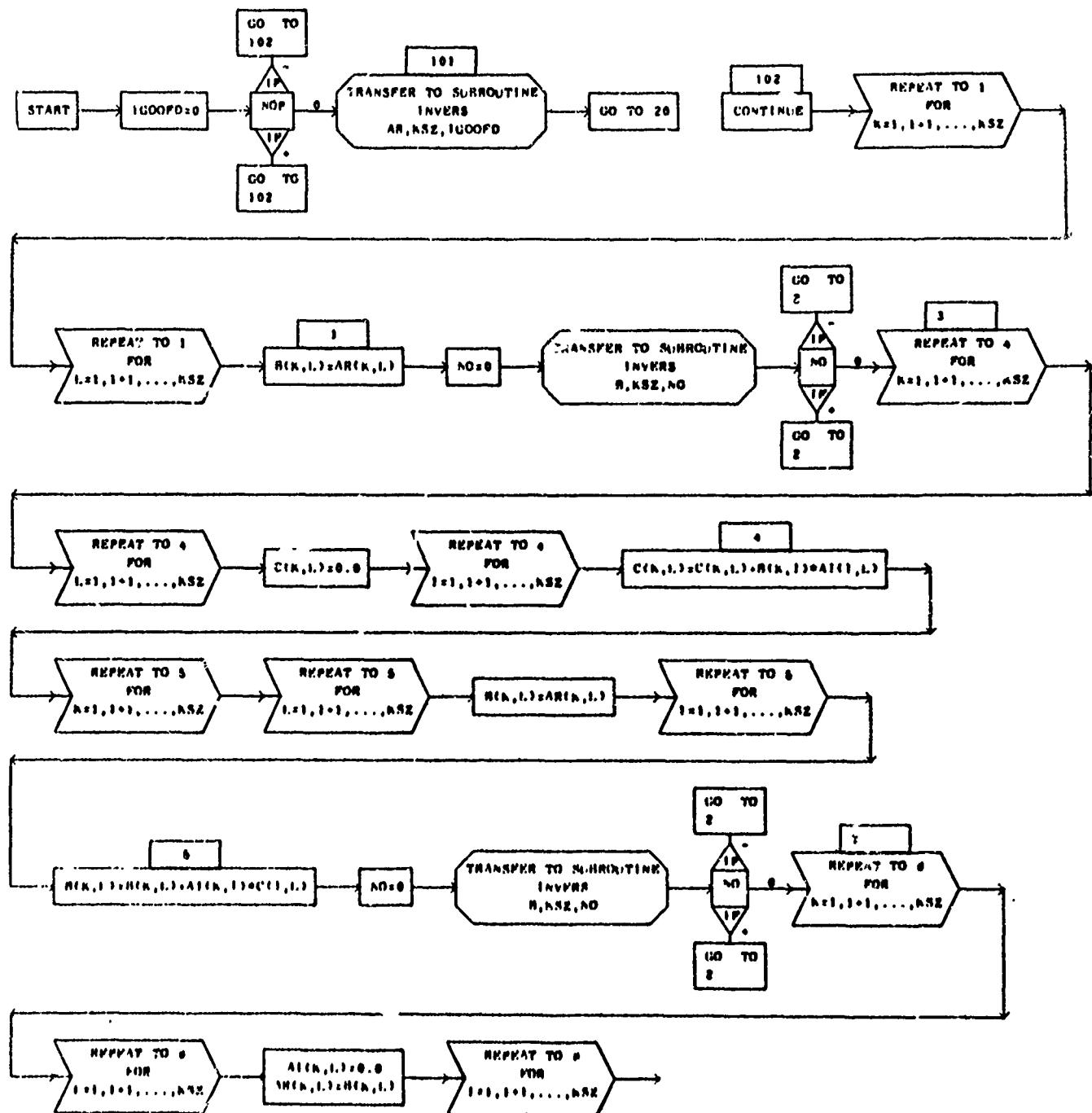
MNVRSS

D I M E N S I O N E D   V A R I A B L E S

SYMBOL	STORAGES								
A8	6,6	A8	6,6	B	6,6	C	6,6		

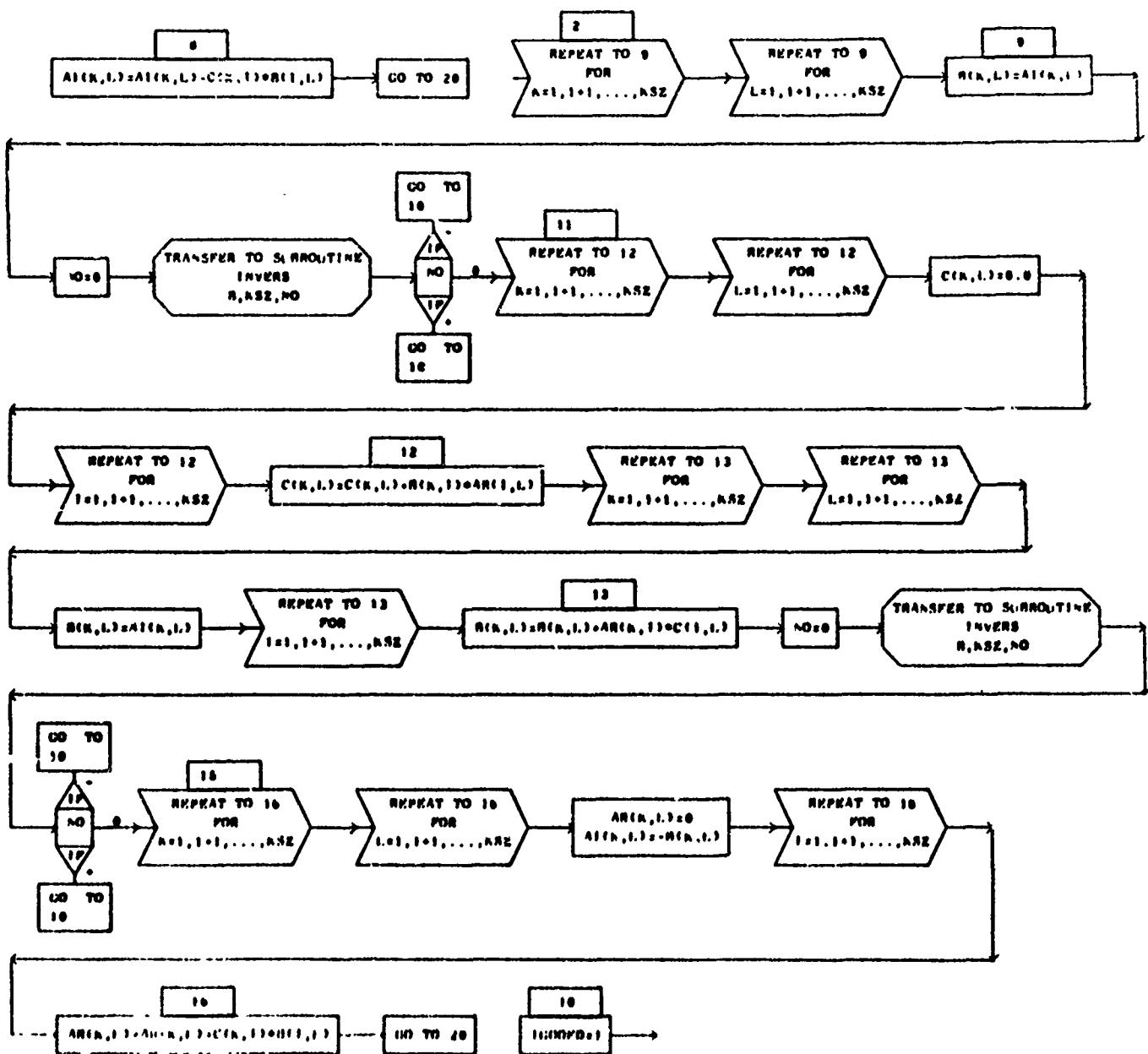
SUBROUTINE MNVRSX (AR,AI,B,C,Y12,1GOOFD,NO?)

PAGE 1



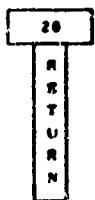
## SUBROUTINE MNVRSX (A,R,A1,B,C,KSZ,IGOOFD,NOP)

PAGE 2



SUBROUTINE MNVRSX (AR,A1,B,C,KSZ,IGOOPD,NOP)

PAGE 3 1



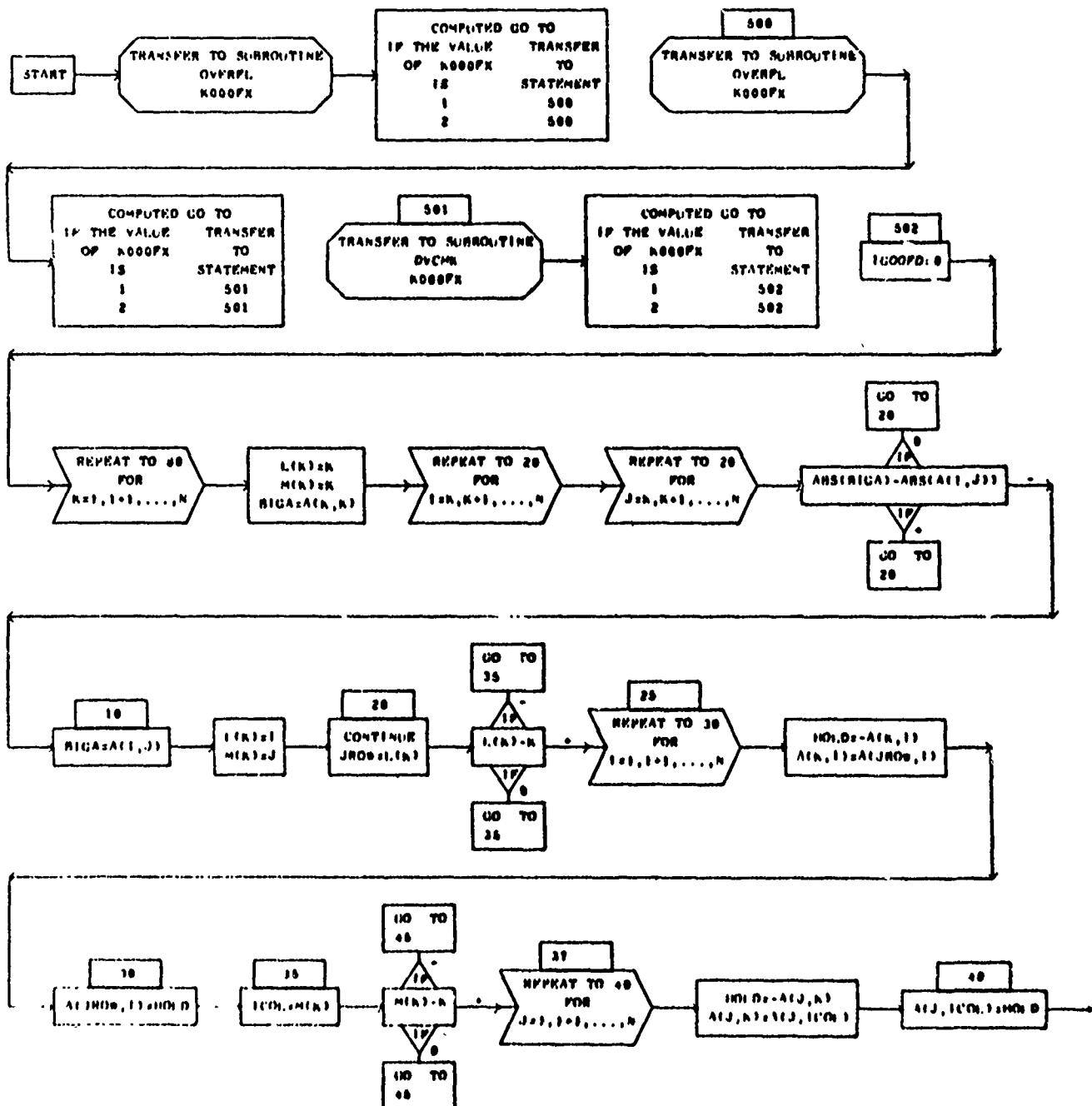
INVERB

DIMENSIONED VARIABLES

SYMBOL	STORAGES								
A	6.0	L	0	M	0	N	0	O	0

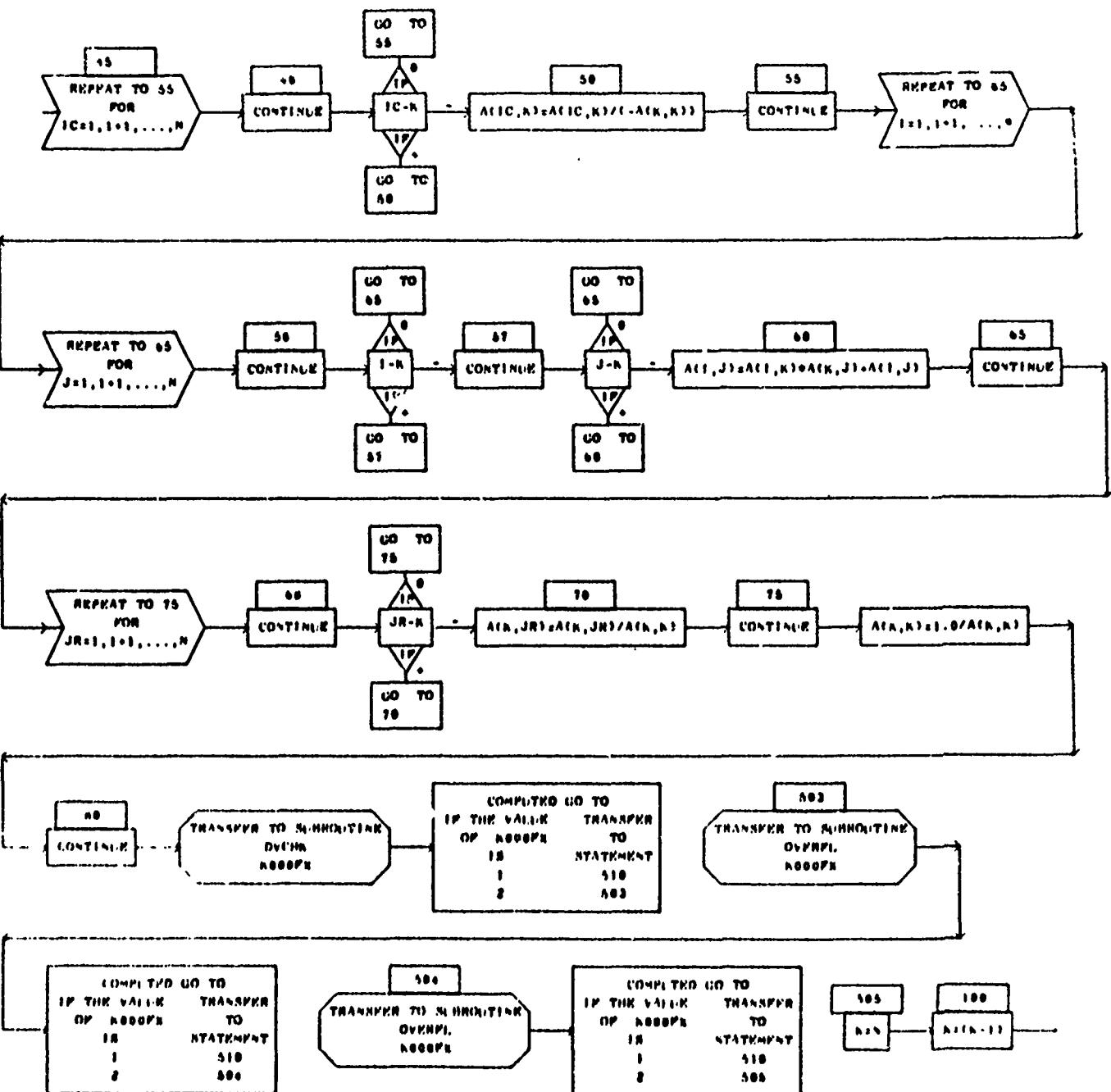
## SUBROUTINE INVERS (A,N,I GOOFD 0)

PAGE 1



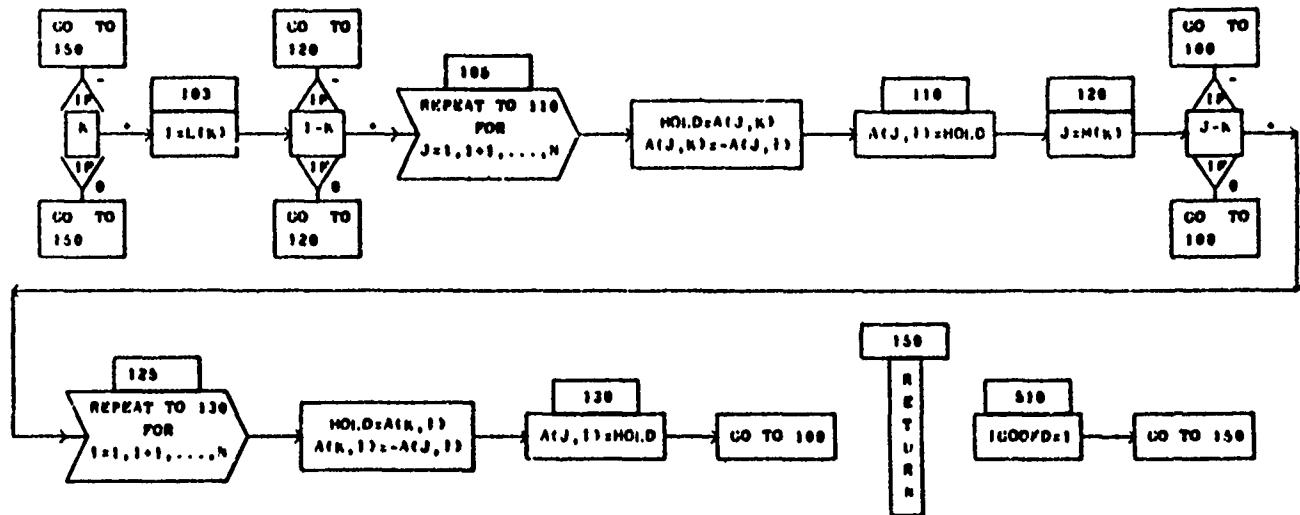
## SUBROUTINE INVERS (A,N,I GOOF D)

PAGE 2



## SUBROUTINE INVERS (A,N,I GOUP D)

PAGE 3



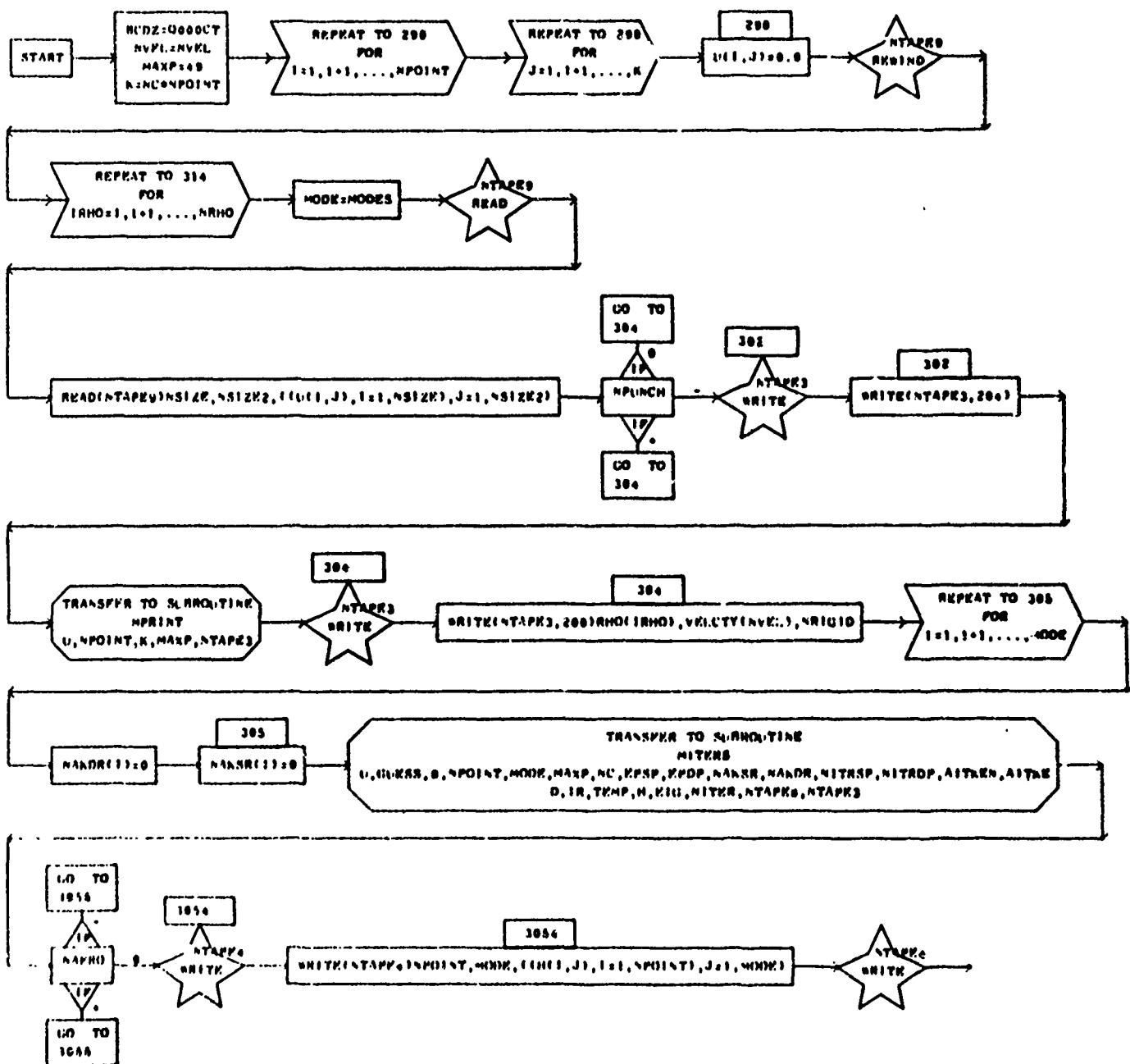
PARTS

DIMENSIONED VARIABLES

SYMBOL	STORAGES								
IT	216	VFLCTY	20	NSIZES	20	DM	0,0	RHO	20

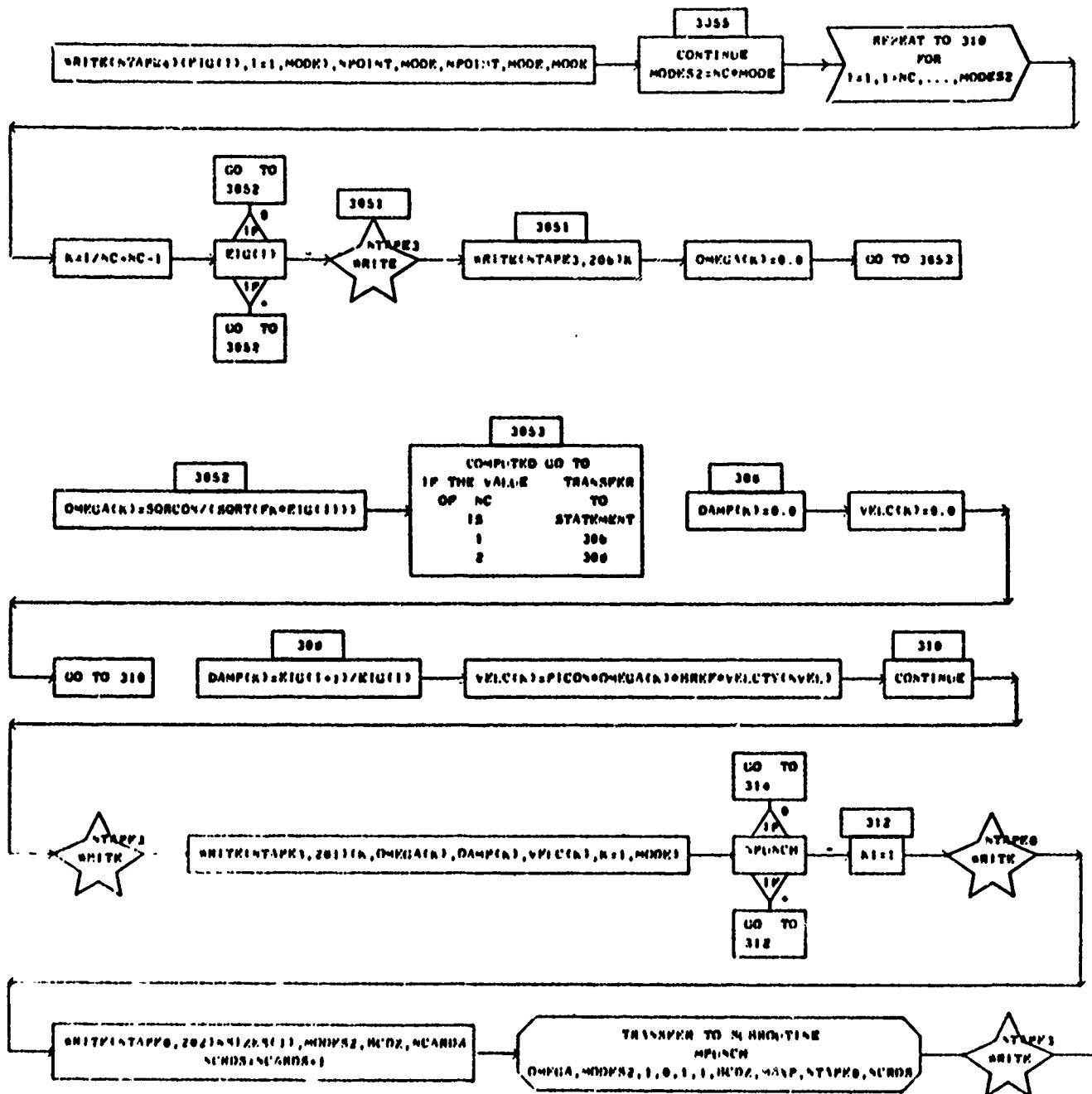
## SUBROUTINE PARTS

PAGE 1



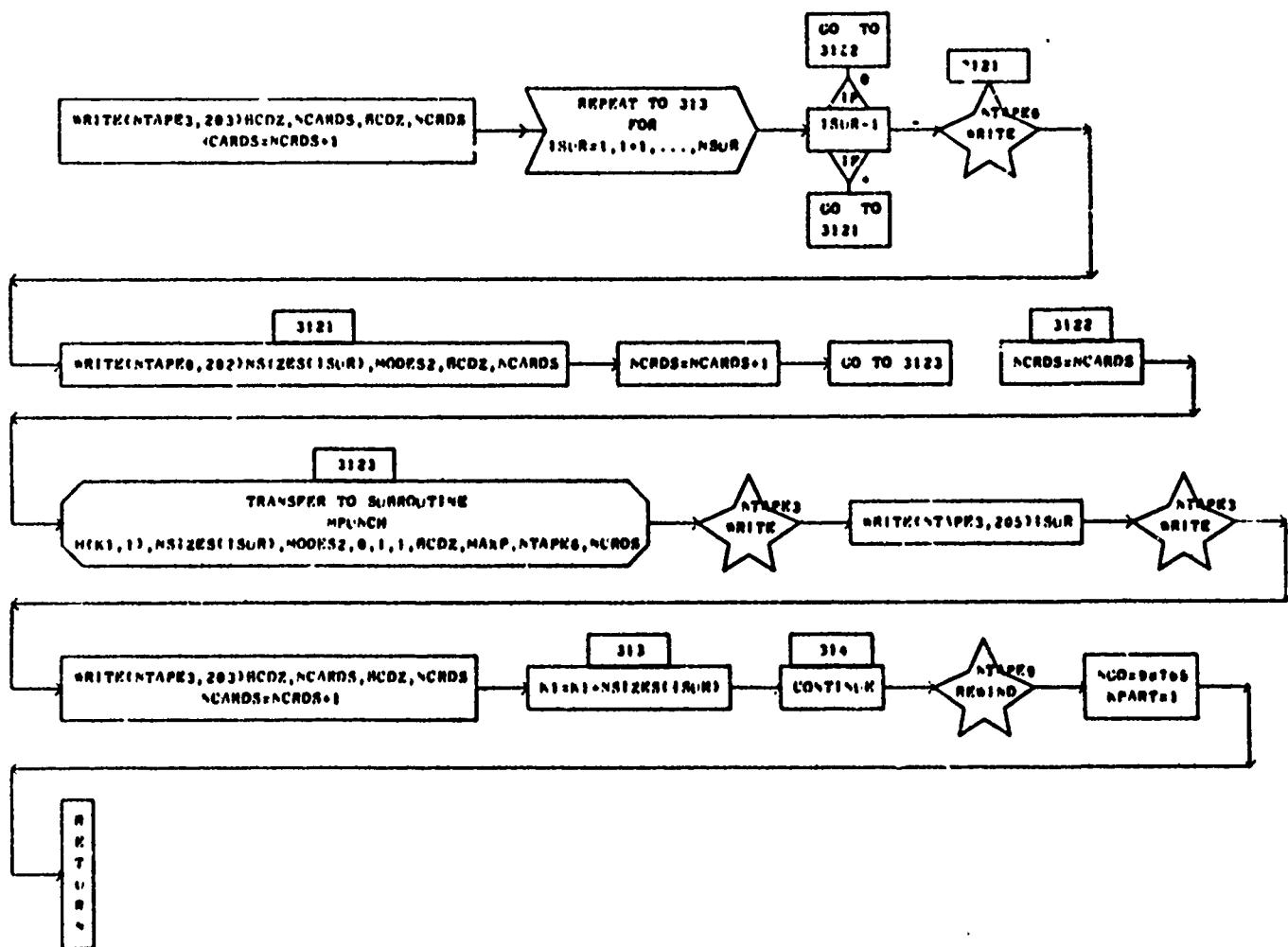
## SUBROUTINE PARTS

PAGE 2



## SUBROUTINE PARTS

PAGE 3



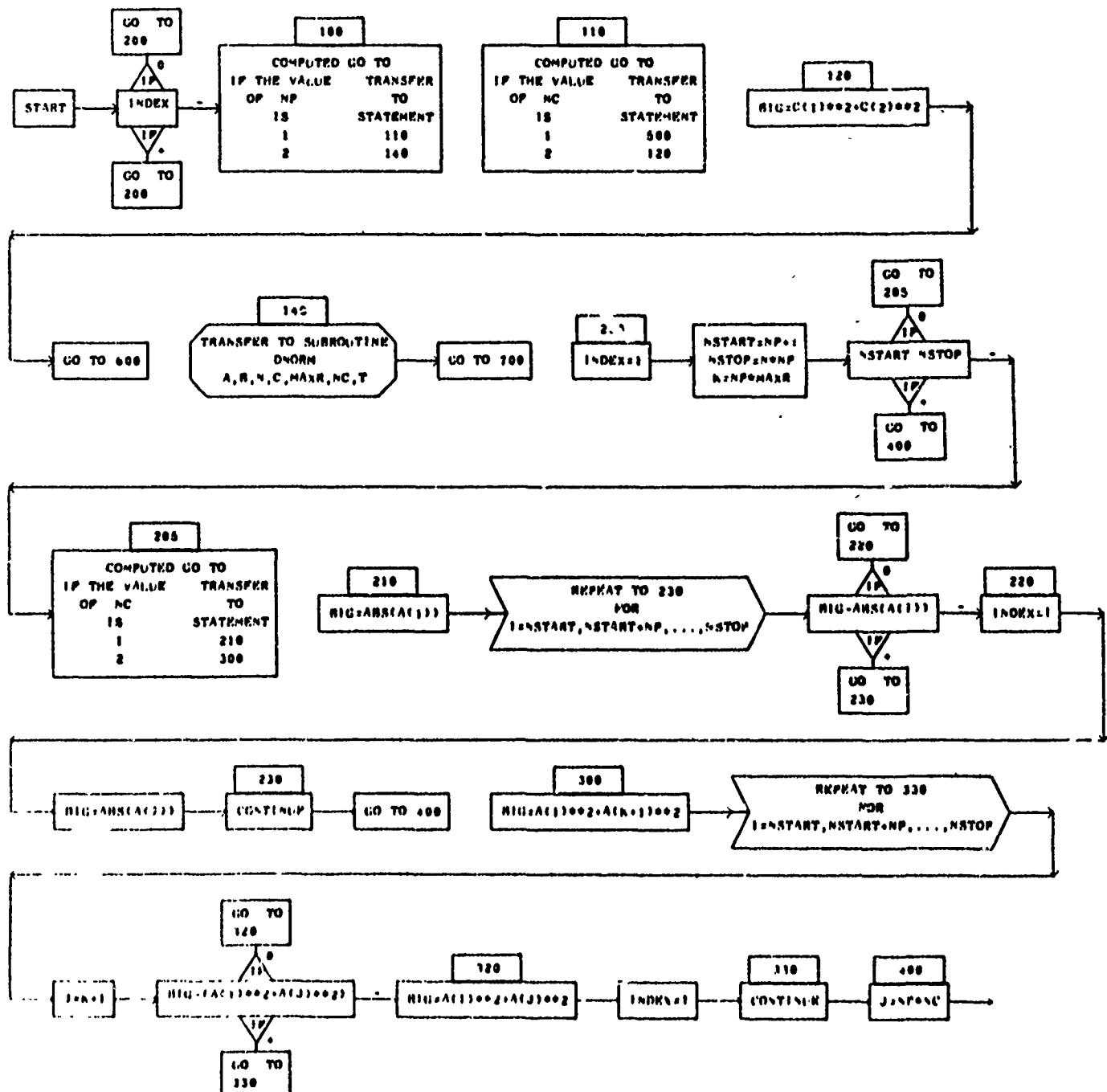
NORMS

DIMENSIONED VARIABLES

SYMBOL	STORAGES								
A	1	B	1	C	1	T	1	Z	1

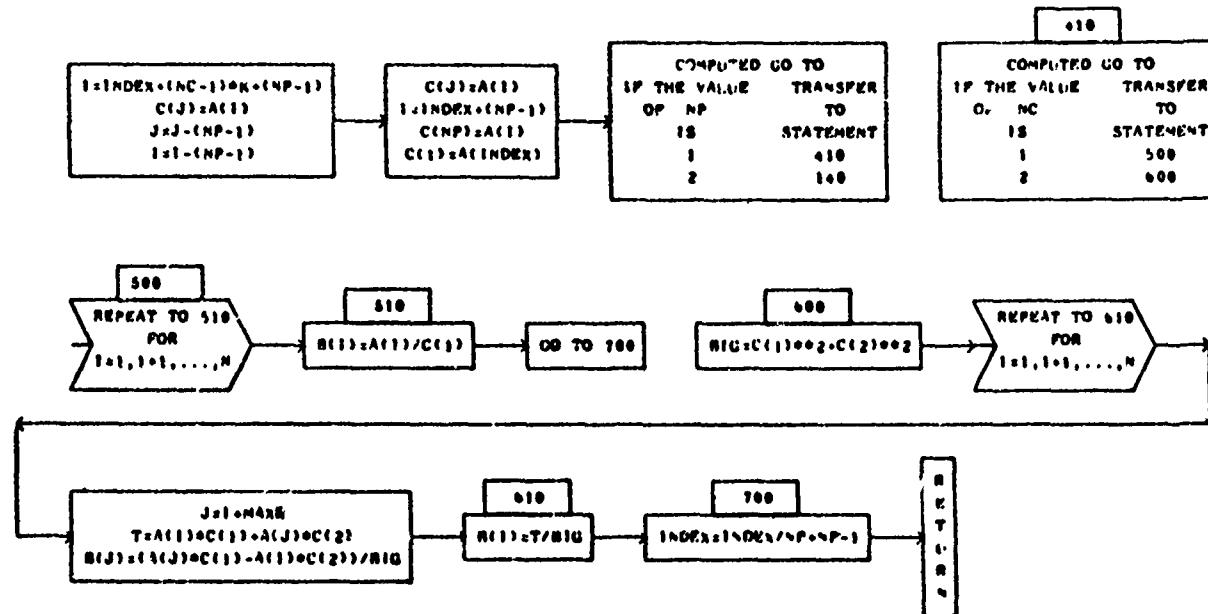
## SUBROUTINE DORM (A,B,N,C,INDEX,MAXR,NC,NP)

PAGE 1



## SUBROUTINE NORM (A,B,N,C,INDEX,MAXR,NC,NP)

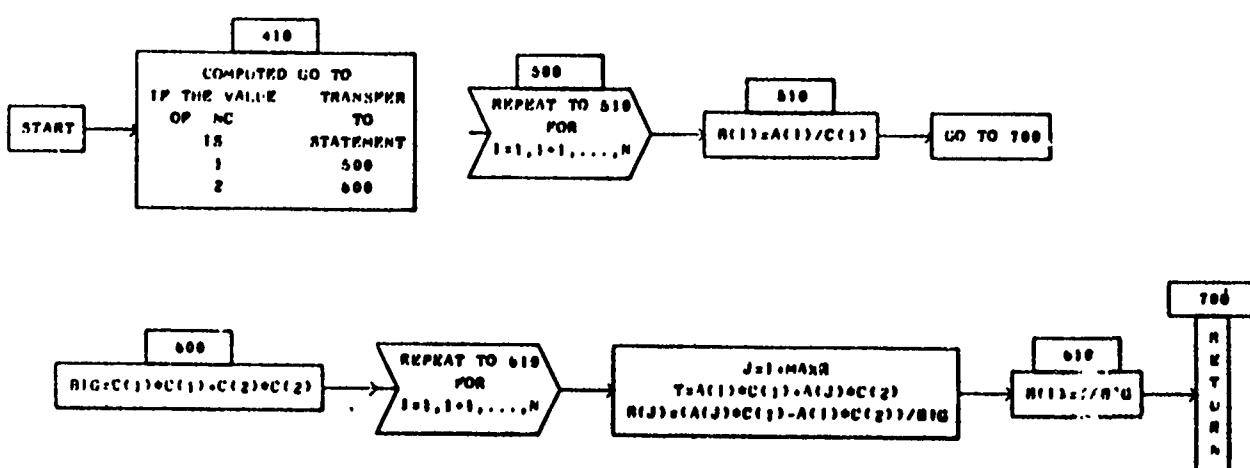
PAGE 2



## DNORMZ

ROUTINE DNORM (A,B,N,C,MAXR,NC,T)

PAGE 1



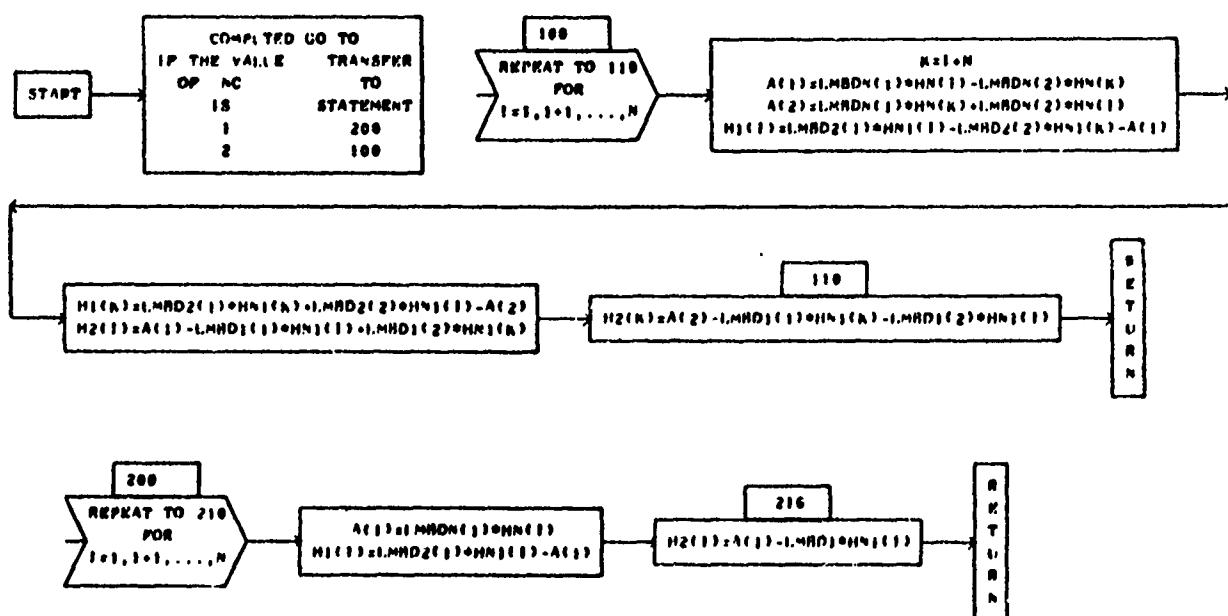
## POHS

## DIMENSIONED VARIABLES

SYMBOL.	STORAGES								
LMBDN	1	LMBD1	2	LMBD2	1	HN	1	HN1	1
H1	1	H2	1	A	2				

SUBROUTINE POHS (LMBDN, LMBD1, LMBD2, HN, HN1, H1, H2, N, NC)

PAGE 1



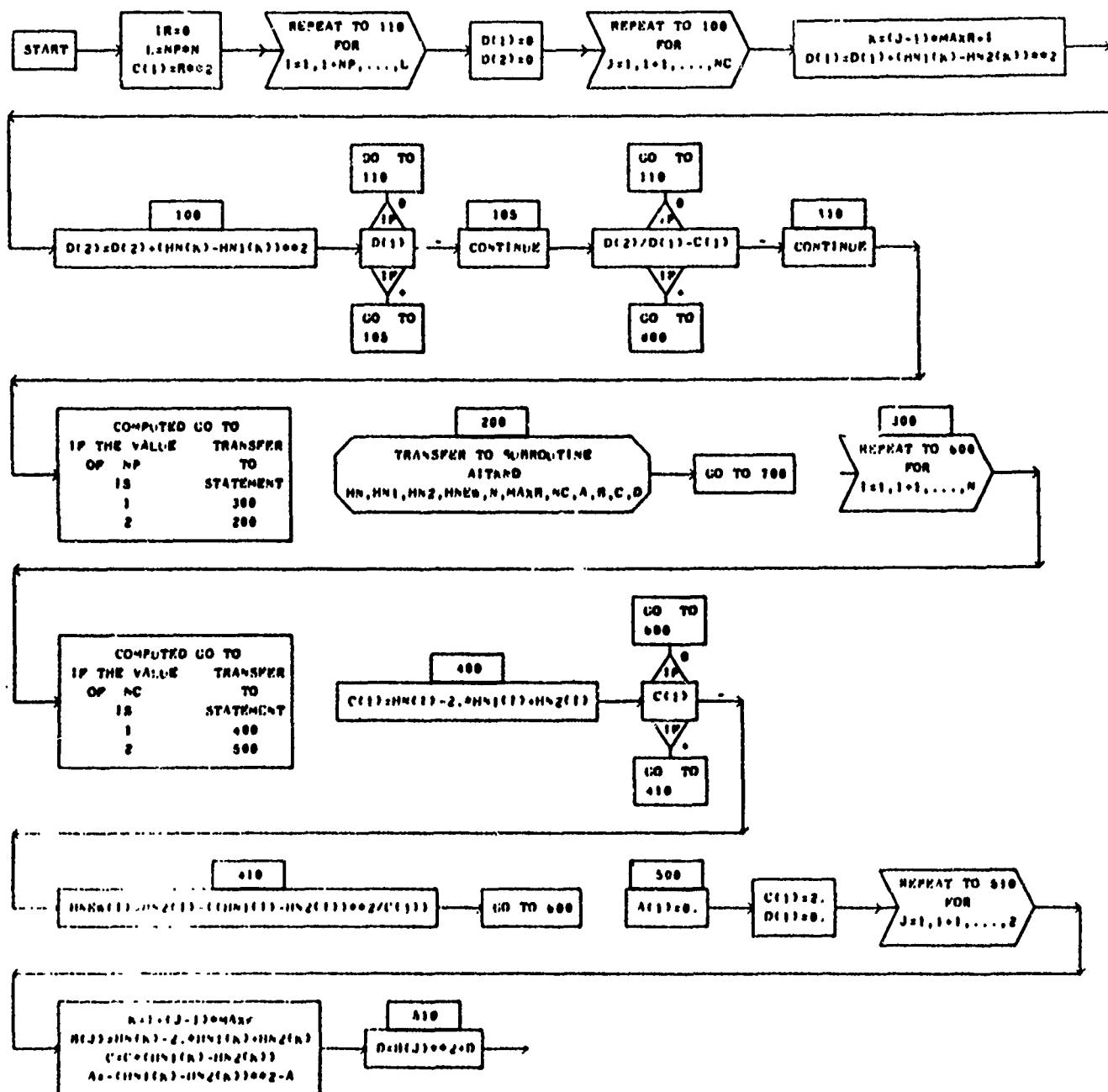
## AITKENS

## DIMENSIONED VARIABLES

SYMBOL	STORAGES								
H4	1	H41	1	H42	1	H420	1	A	2
B	0	C	2	D	2				

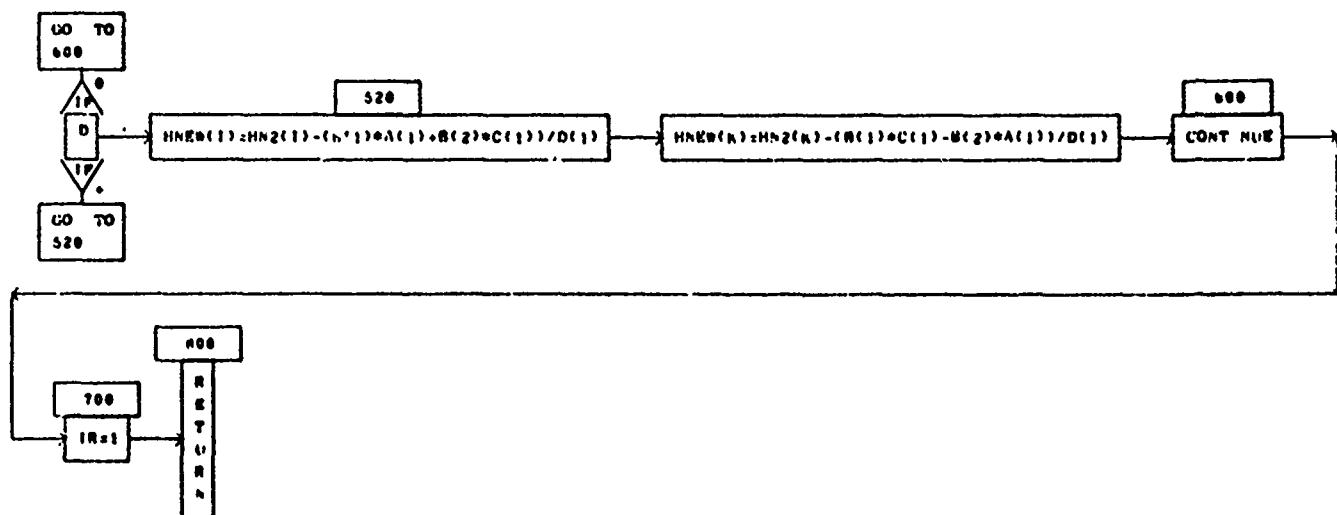
SUBROUTINE AITKNS (HN, HN1, HN2, HNEW, R, N, MAXR, NC, NP, IR)

PAGE 1



## SUBROUTINE ALTANS (HN, HN1, HN2, HNEW, R, N, MAXR, NC, NP, IR)

PAGE 2



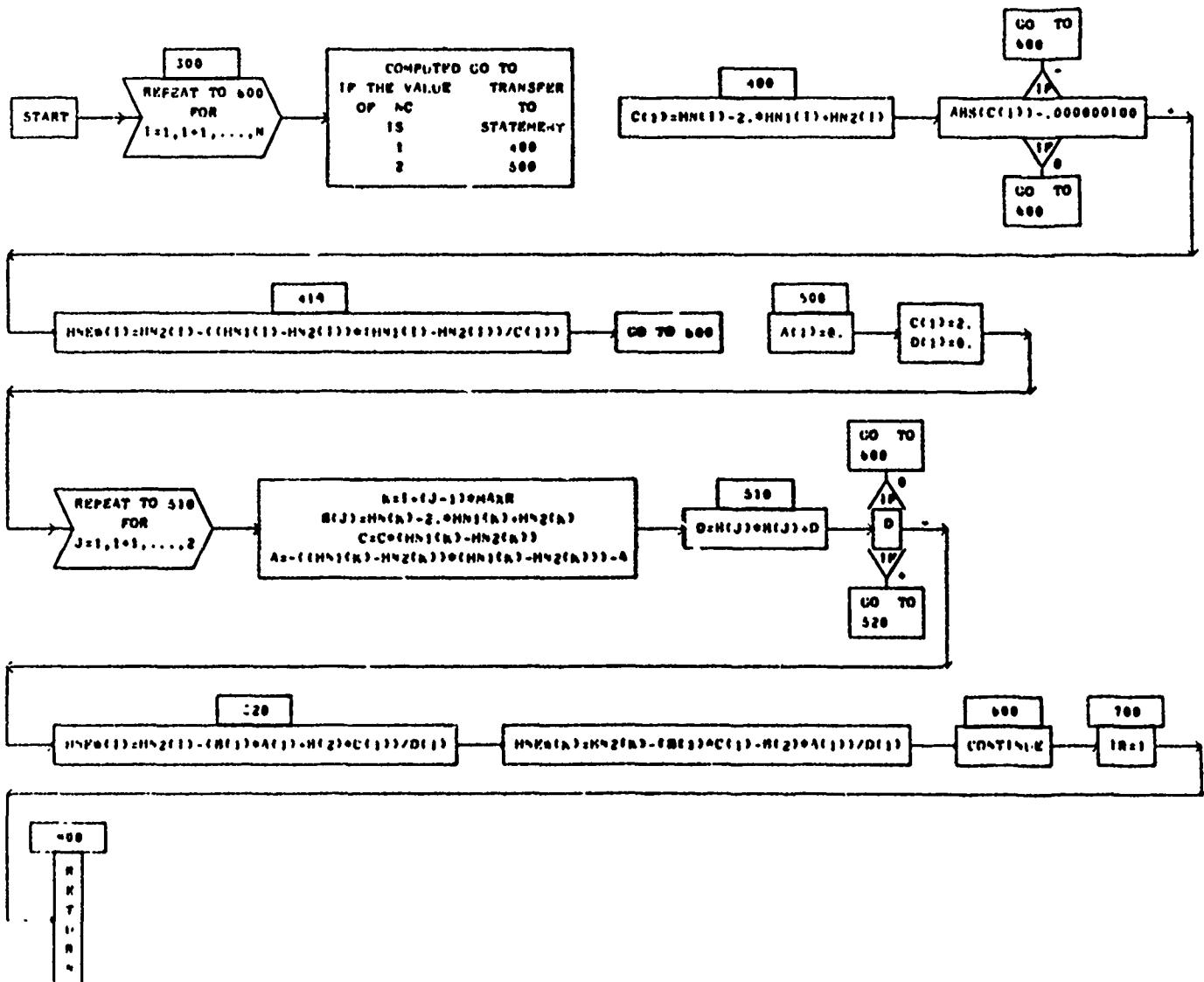
A19KND

DIMENSIONS & VARIABLES

SYMBOL	STORAGES								
HN	I	HN1	I	HN2	I	HNW	I	A	I
S	S	C	I	D	I				

## SUBROUTINE AITAND (HN,HV1,HV2,HNEQ,N,MAXR,NC,A,B,C,D)

PAGE 1



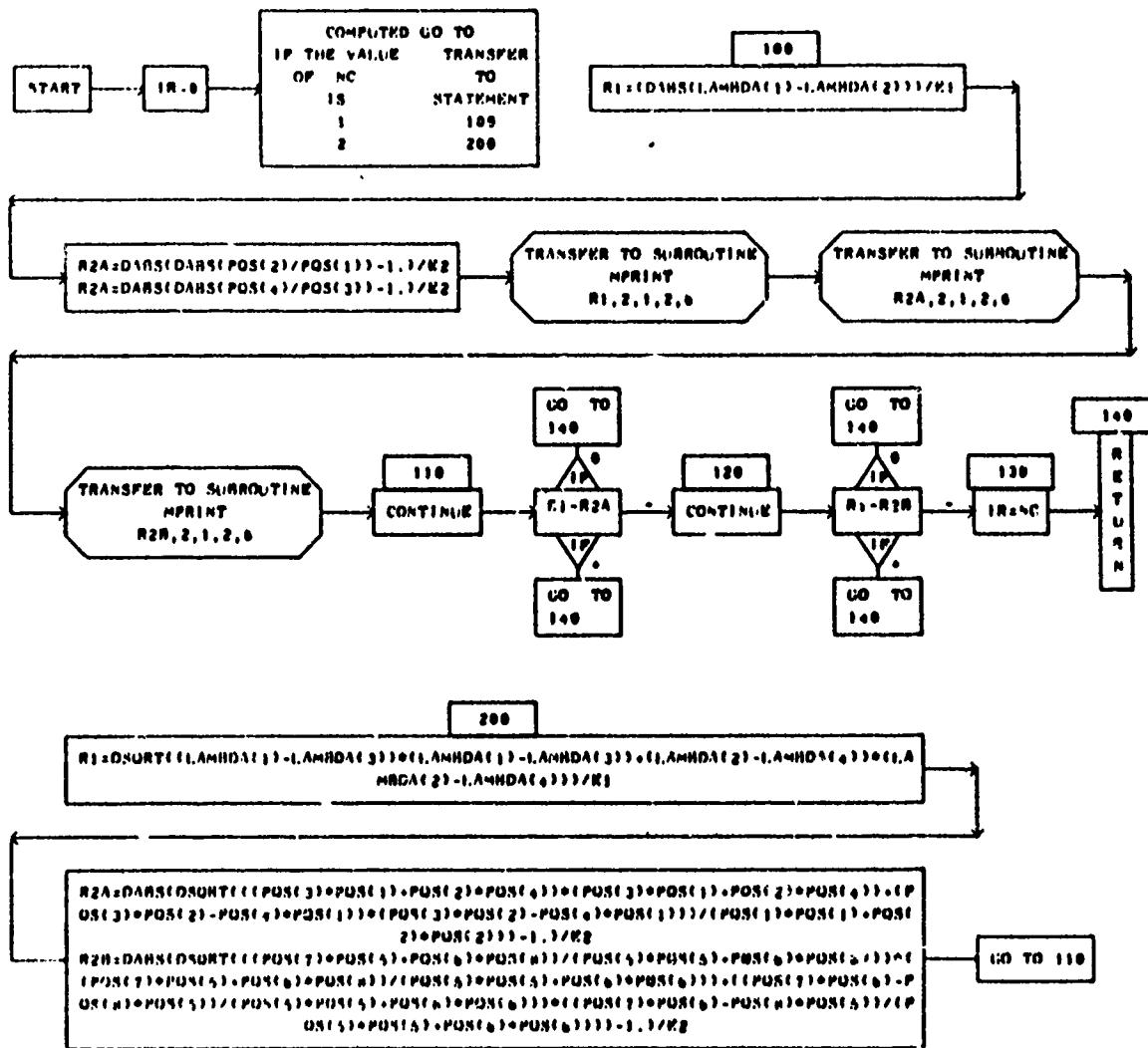
LEO 188

DIMENSIONED VARIABLES

SYMBOL	STORAGES								
LAMBDA	0	POR	1						

## SUBROUTINE CRUIS (LAMHDA, POS, R1, E2, NC, IR)

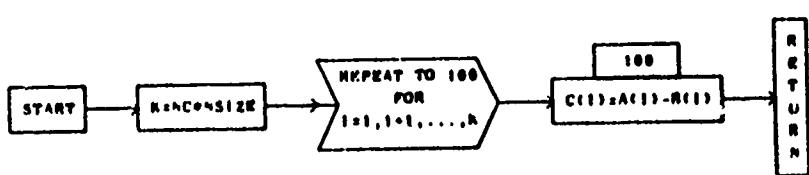
PAGE 1



MAOS

PAGE 1

SUBROUTINE MAOS (A,B,C,NSIZE,NC)



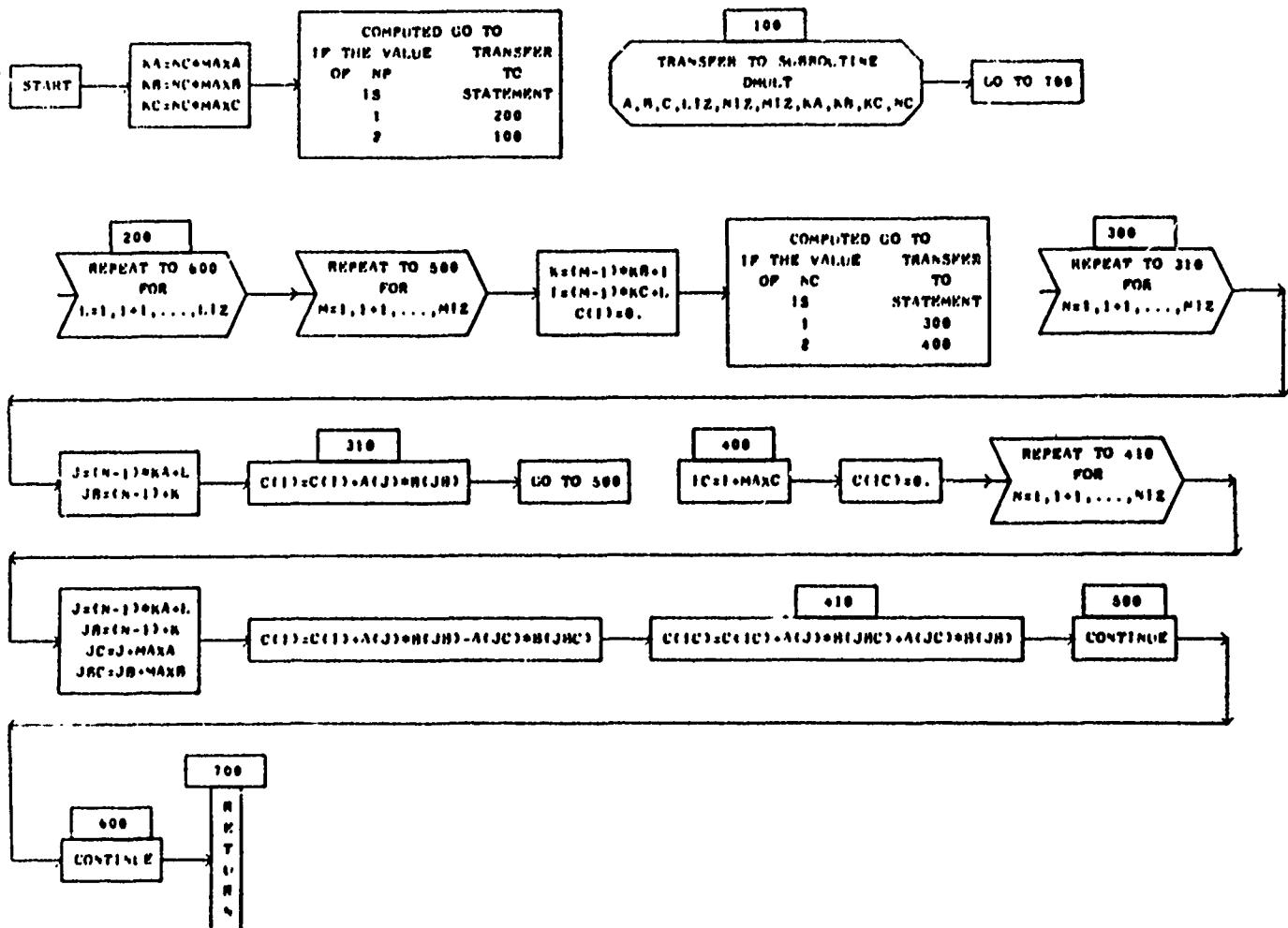
## MULTS

## DIMENSIONED VARIABLES

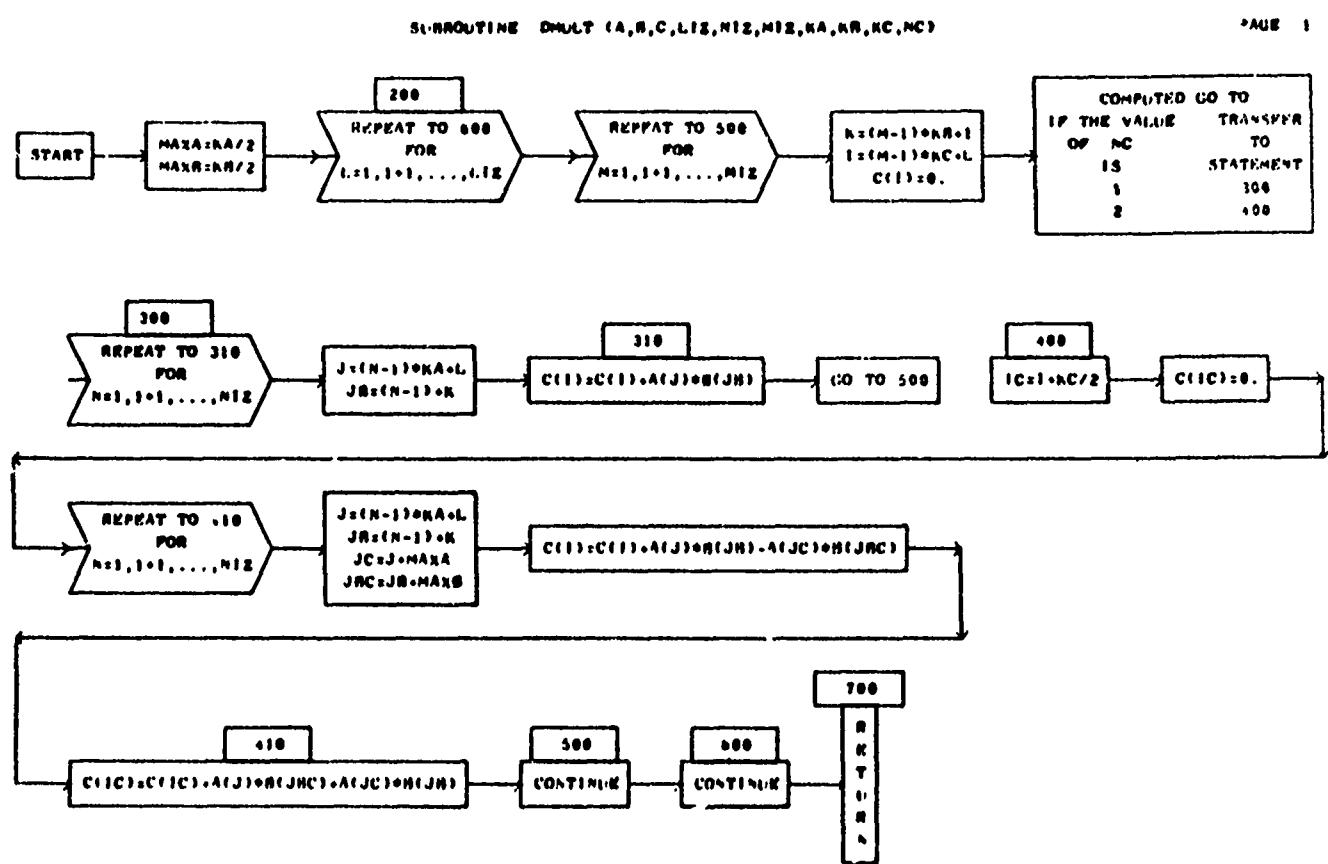
SYMBOL	STORAGES								
A	I	B	I	C	I				

SUBROUTINE MULT (A,B,C,IIZ,MIZ,MAXA,MAXB,MAXC,NC,NP)

PAGE 1



## DMULTS



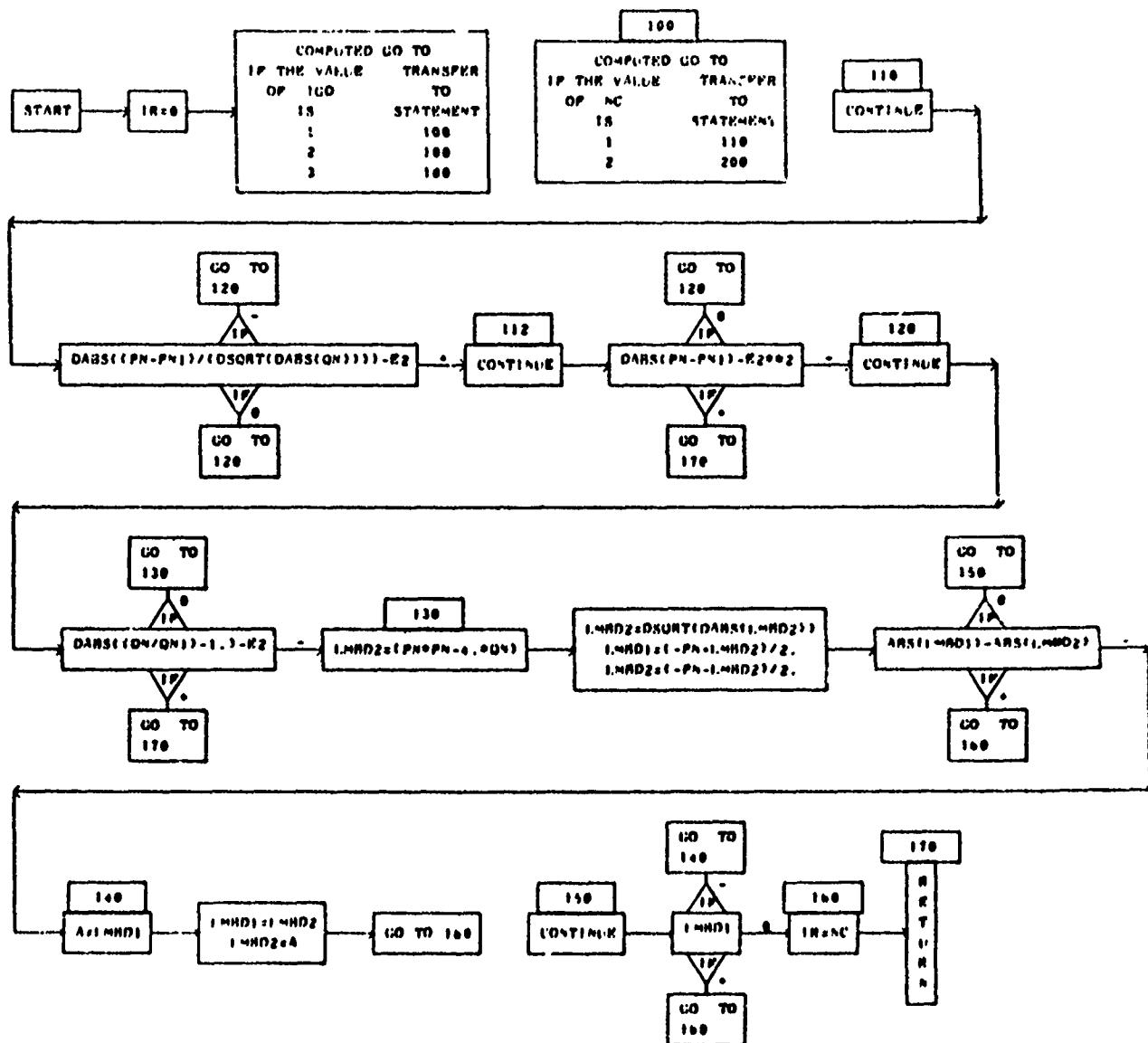
POLMS

D I M E N S I O N E D   V A R I A B L E S

SYMBOL.	STORAGES								
PN	1	PN1	1	ON	1	ON1	1	E2	1
IMBD1	1	IMBD2	1						

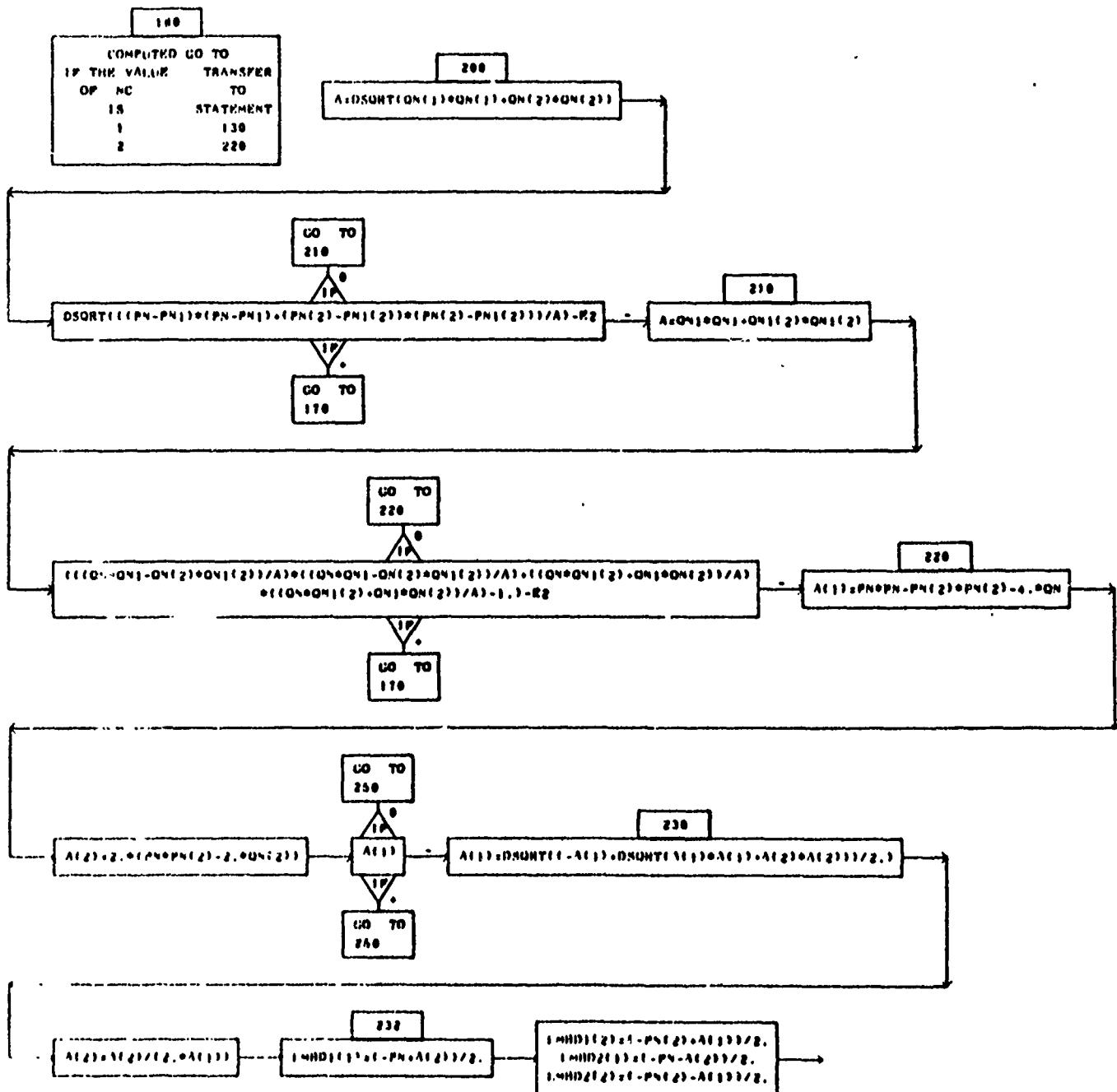
SUBROUTINE POLM (PN,PN1,ON,ON1,E2,LMD01,LMD2,NC,IR,IGO1)

PAGE 1



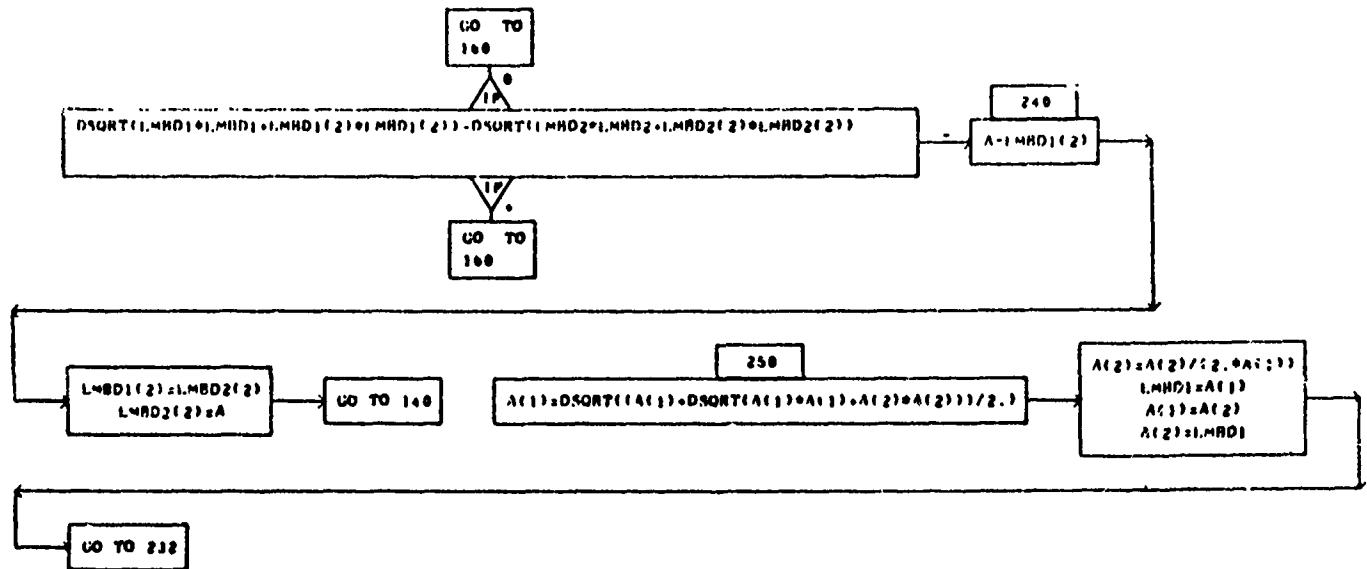
## SUBROUTINE ZOLH (PN, PNT, QK, QN1, R2, LMHD1, LMHD2, NC, IR, IUD)

PAGE 2



SUBROUTINE POLM (PN,PNT,ON,ON1,E2,LMD1,LMD2,NC,IR,IGO)

PAGE 3



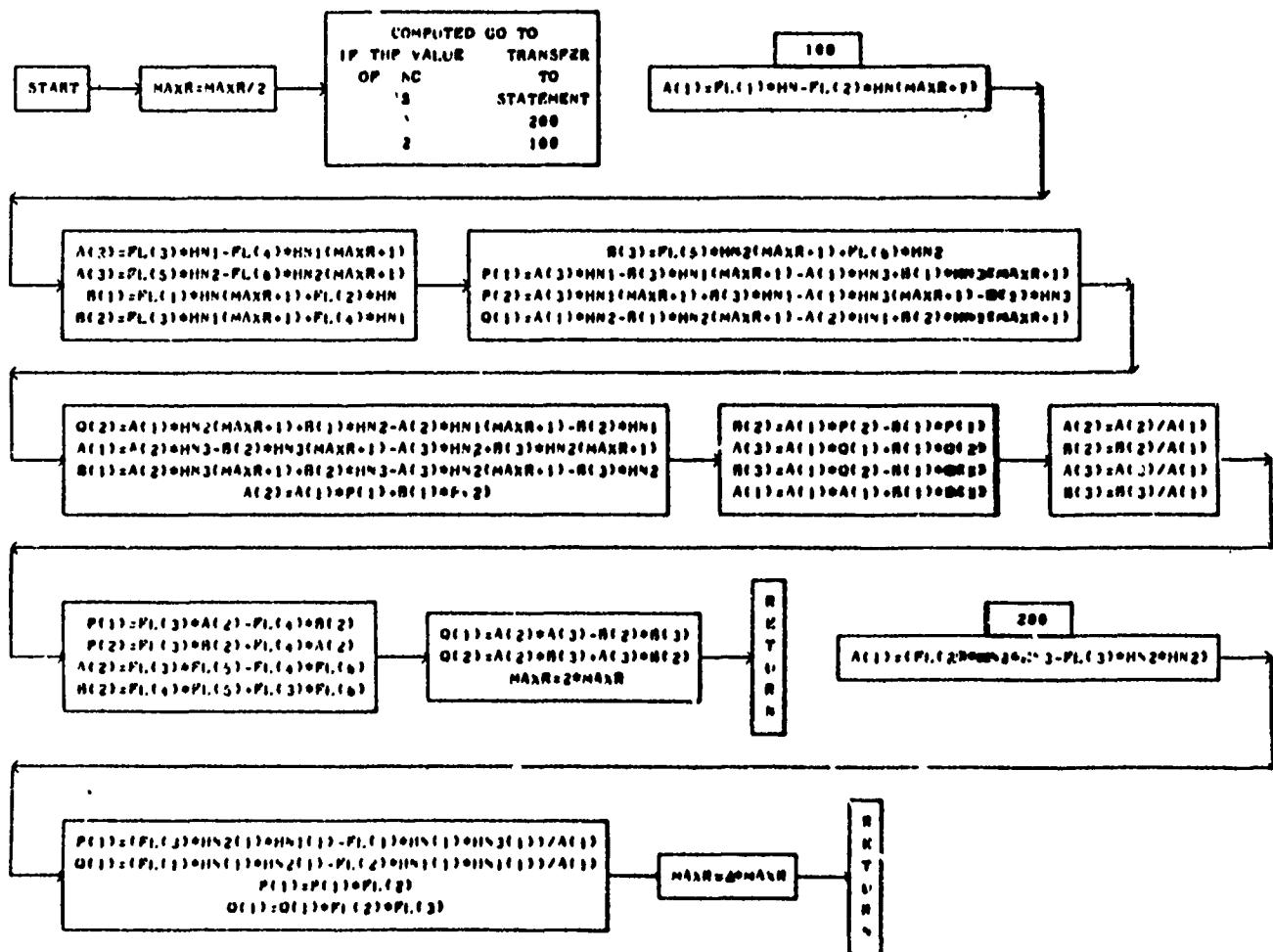
PUS

DIMENSIONED VARIABLES

S/NUMBER.	STORAGES	SYMBOL.	STORAGES	SYMBOL.	STORAGES	SYMBOL.	STORAGES	SYMBOL.	STORAGES
PL	1	MN	1	MN1	1	MN2	1	MN3	1
P	1	Q	1	A	3	R	3		

SUBROUTINE PG (PL, MN, MN1, MN2, MN3, P, Q, NC, MAXR )

PAGE 1



CLOSES  
SUBROUTINE CLOSE, COMPUTES 2 CLOSE ROOTS.

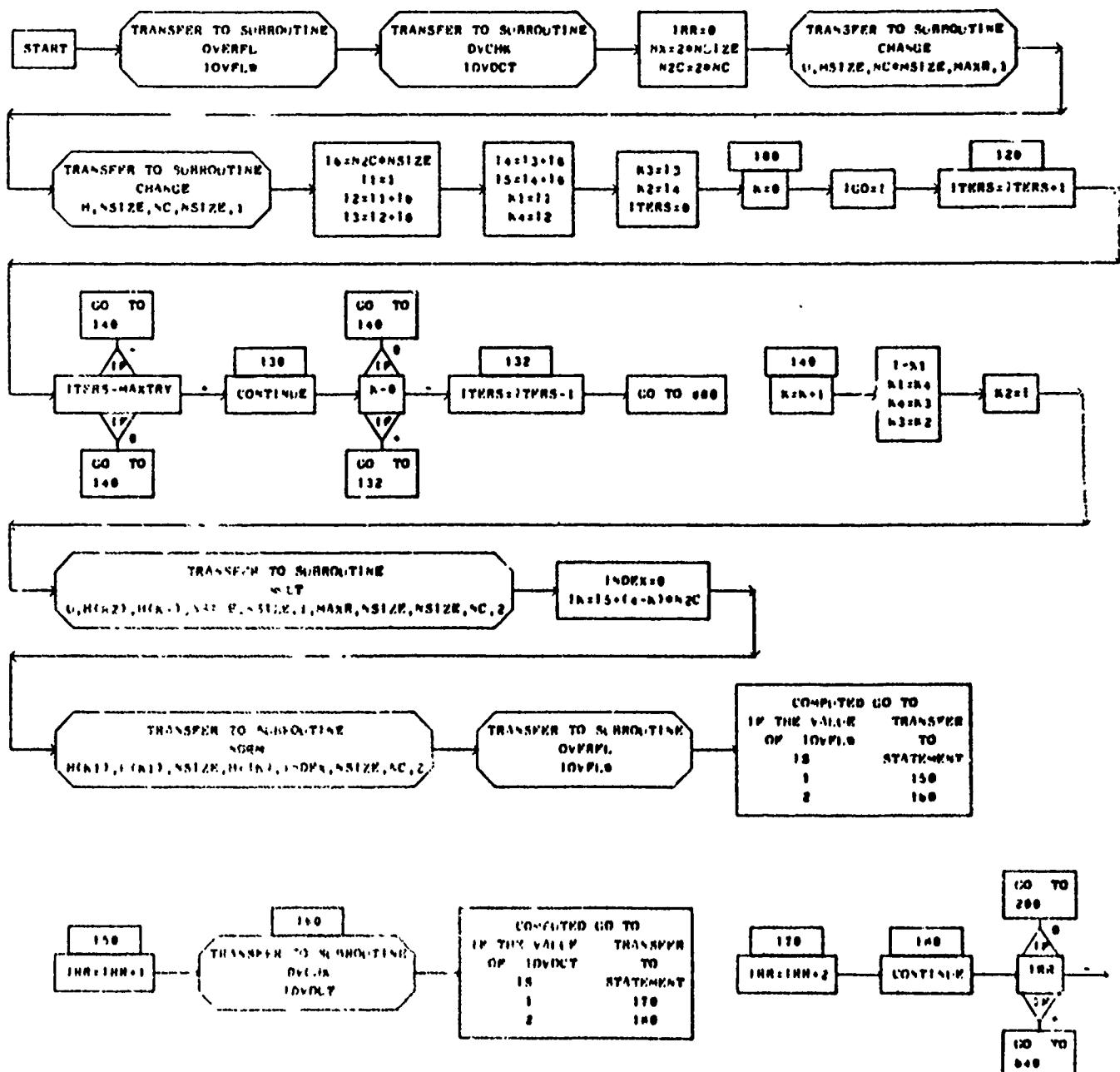
U = MATRIX, DIMENSIONED (MAXR,2NC+MAXR)  
H = STARTING GUESS, DIMENSIONED (MAXR,2NC+1+2NC+1)  
NSIZE = SIZE OF MATRIX  
MAXR = DIMENSIONED NUMBER OF ROWS OF U AND H  
MAXTRY = MAXIMUM NUMBER OF DOUBLE PRECISION ITERATIONS.  
EPS1 = SINGLE ROOT CONVERGENCE CRITERIA  
EPS2 = DOUBLE ROOT CONVERGENCE CRITERIA  
R = AITKENS CONVERGENCE CRITERIA  
IRR = ERROR RETURN INDICATOR.  
=1, OVERFLOW  
=2, DIVIDE CHECK  
=3, BOTH OVERFLOW AND DIVIDE  
CHECK.  
ITERS = NUMBER OF ITERATIONS PERFORMED.  
• FOR DOUBLE ROOT  
• FOR SINGLE ROOT  
NC = 1, REAL, 2, COMPLEX

DIMENSIONED VARIABLES

SYMBOL	STORAGES								
U	1	H	1	VALUR	1				

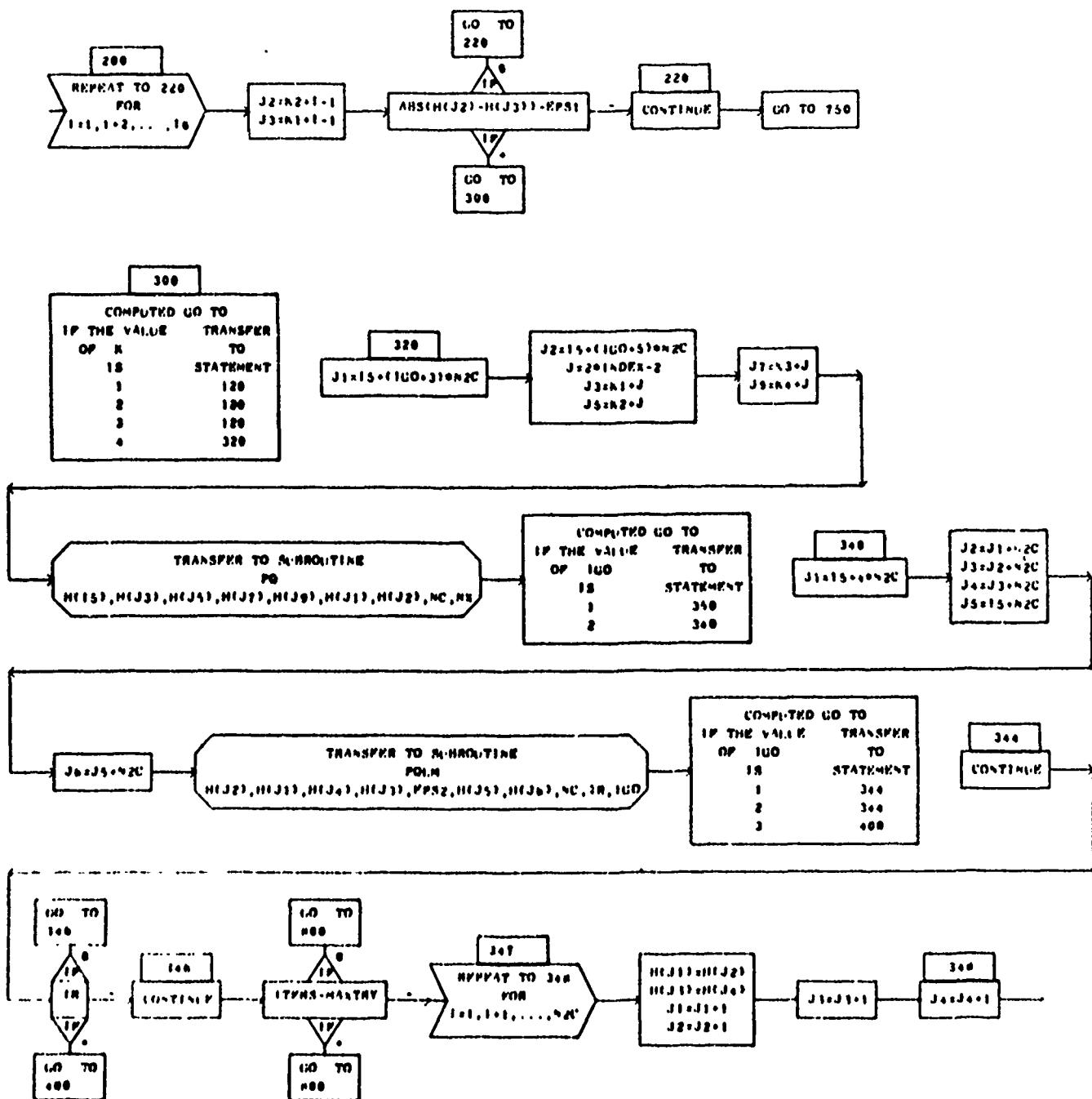
ROUTINE CLOSSES ( $U, H, NSIZE, MAXR, R, EPS1, EPS2, NC, IRR, MAXTRY, ITERS,$

PAGE 1



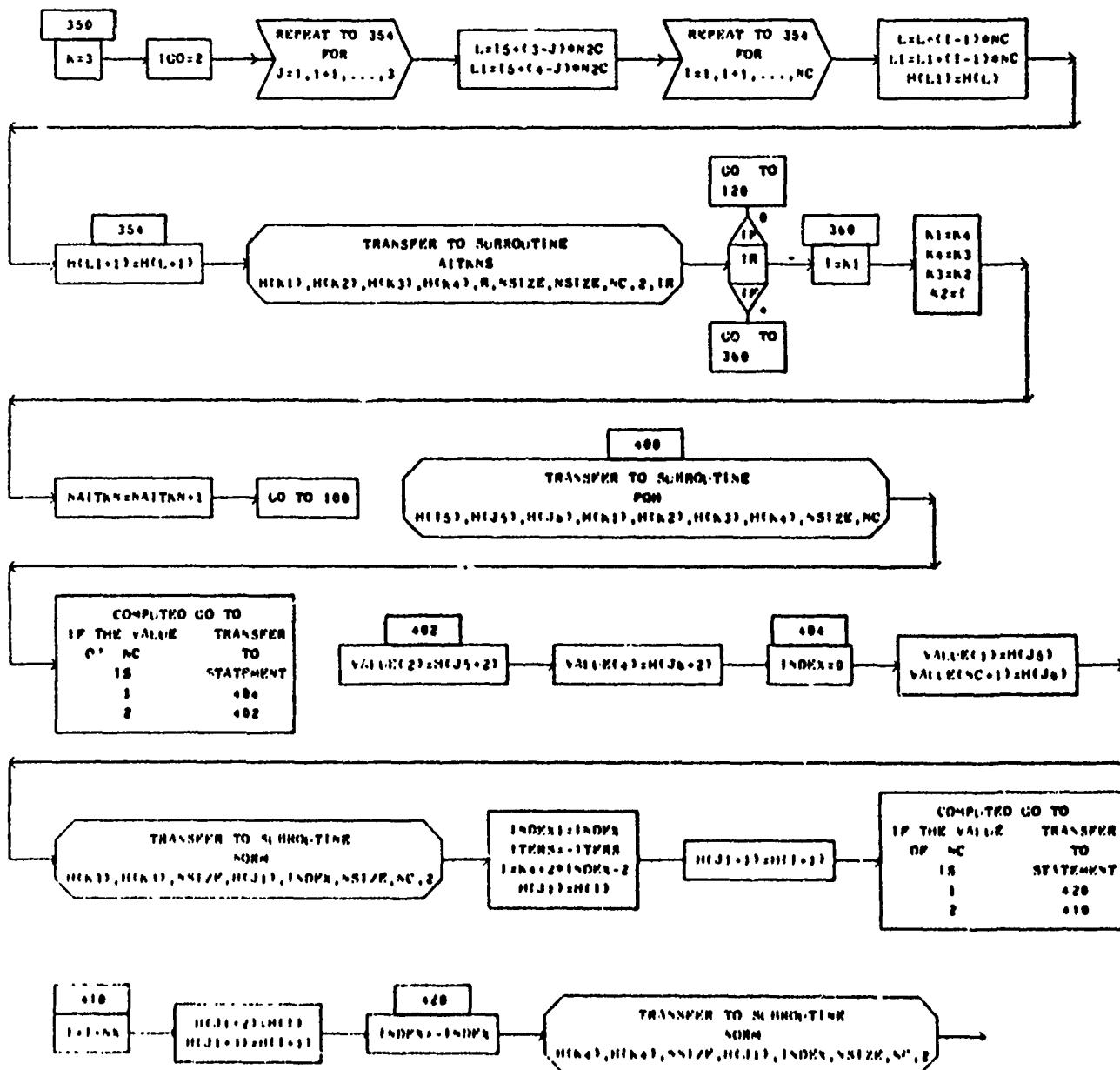
SUBROUTINE CLOSSES (U,H,N12P,MAXR,R,EPS1,EPS2,NC,IRR,MAXTRY,ITERS,

PAGE 2 1



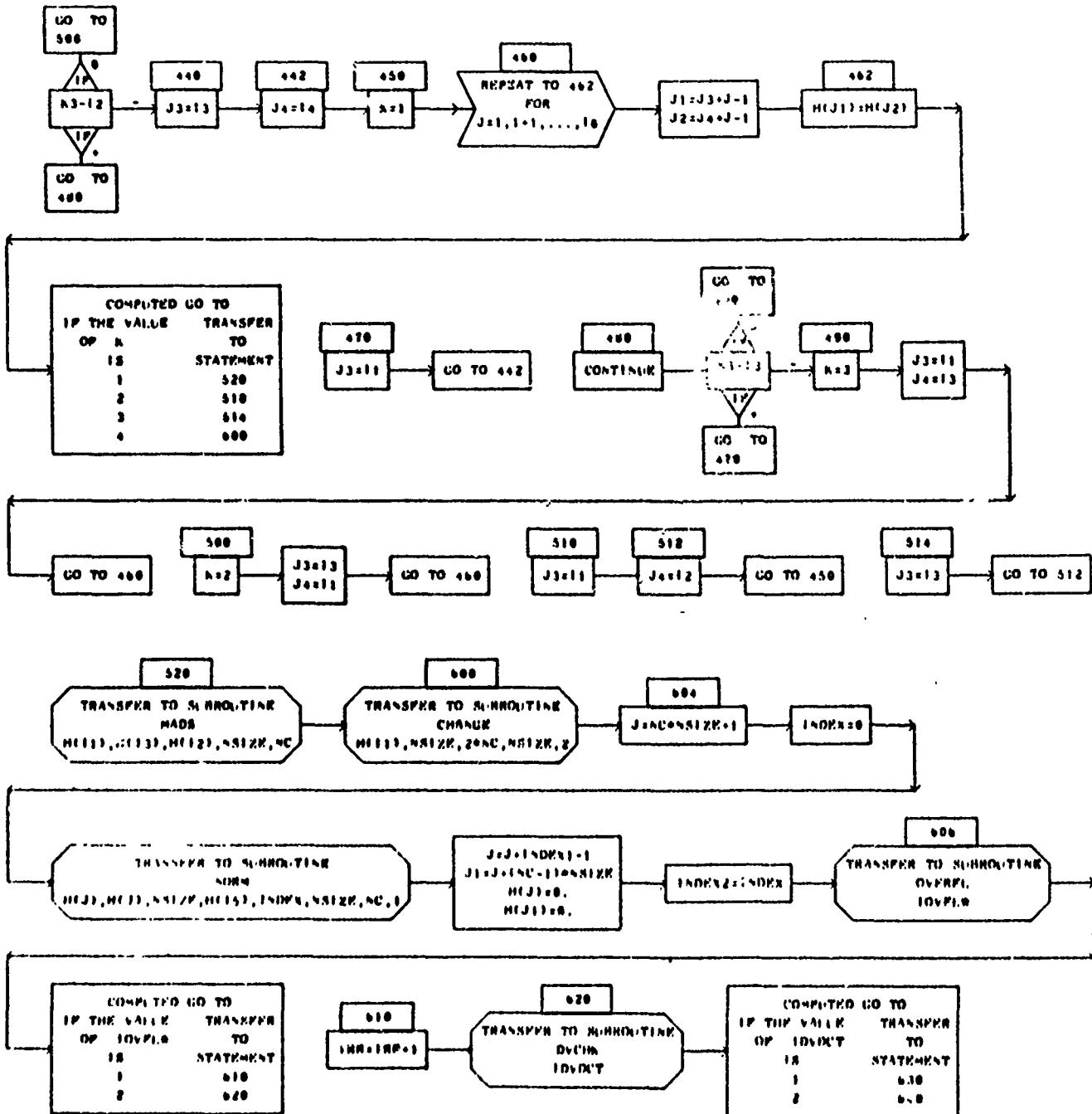
SUBROUTINE CLOSES (L,H,NSIZE,MAXR,R,KPS1,KPS2,NC,IRR,MAXTRY,ITERS,

PAGE 3



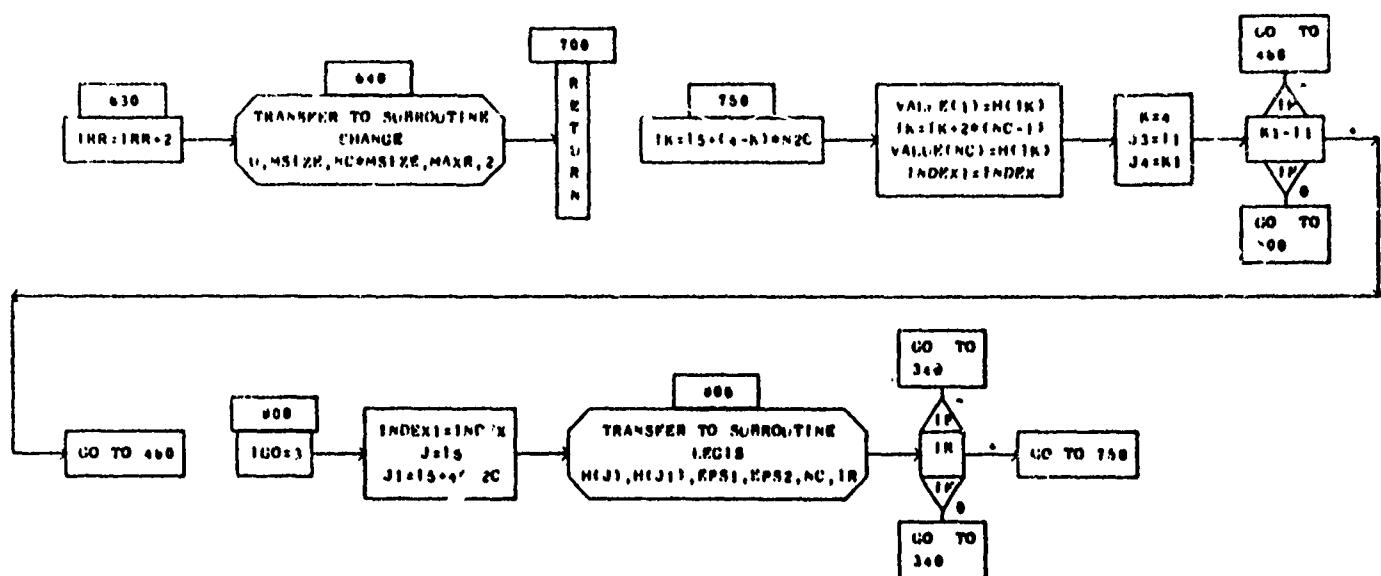
SUBROUTINE CLOSSES (U,H,NSIZE,MAXR,R,EP51,EP52,NC,IRR,MAXTRY,ITERS,

PAGE 4



SUBROUTINE CLOSES (U,H,NSIZE,MAXR,R,KPS1,EPS2,NC,IRR,MAXTRY,ITERS,

PAGE 5



NITER

A IS STORED IN CORE AT A. (MAXR X ACNPSIZE )

NTAPUT IS A UTILITY TAPE, FOR CHECK VECTORS IF DESIRED.

EPSP = EPSILON ONE = SINGLE PRECISION CONVERGENCE TEST NUMBER

EPDP = EPSILON TWO = DOUBLE PRECISION .. .. ..

NC = 1, IF REAL NP = 1, IF SINGLE PRECISION

2, IF COMPLEX .. 2, IF DOUBLE ..

NCNESS = 0, IF FIRST GUESS IS TO BE A COLUMN OF ONES.

MODOUT = NO. OF MODES TO BE COMPUTED.

NAKSR = NO. TIMES AITKENS ACCELERATION WAS USED IN SINGLE PRECISION.

NAKDR = .. .. .. .. .. .. .. .. .. .. .. .. .. .. ..

MAXSR = MAXIMUM ITERATIONS ALLOWED IN SINGLE PRECISION.

MAXDR = .. .. .. .. .. .. .. .. .. .. .. .. .. .. ..

IRN = ERROR RETURN = 1, FOR OVERFLOW

2, FOR DIVIDE CHECK

3, FOR BOTH OVERFLOW AND DIVIDE CHECK

NSIZE = NO. OF ROWS AND COLUMNS OF A

RSP = R, AITKENS ACCELERATION CONVERGENCE CONTROL, FOR SINGLE PRECIS.

RDP = R, AITKENS ACCELERATION CONVERGENCE CONTROL, FOR DOUBLE PRECIS.

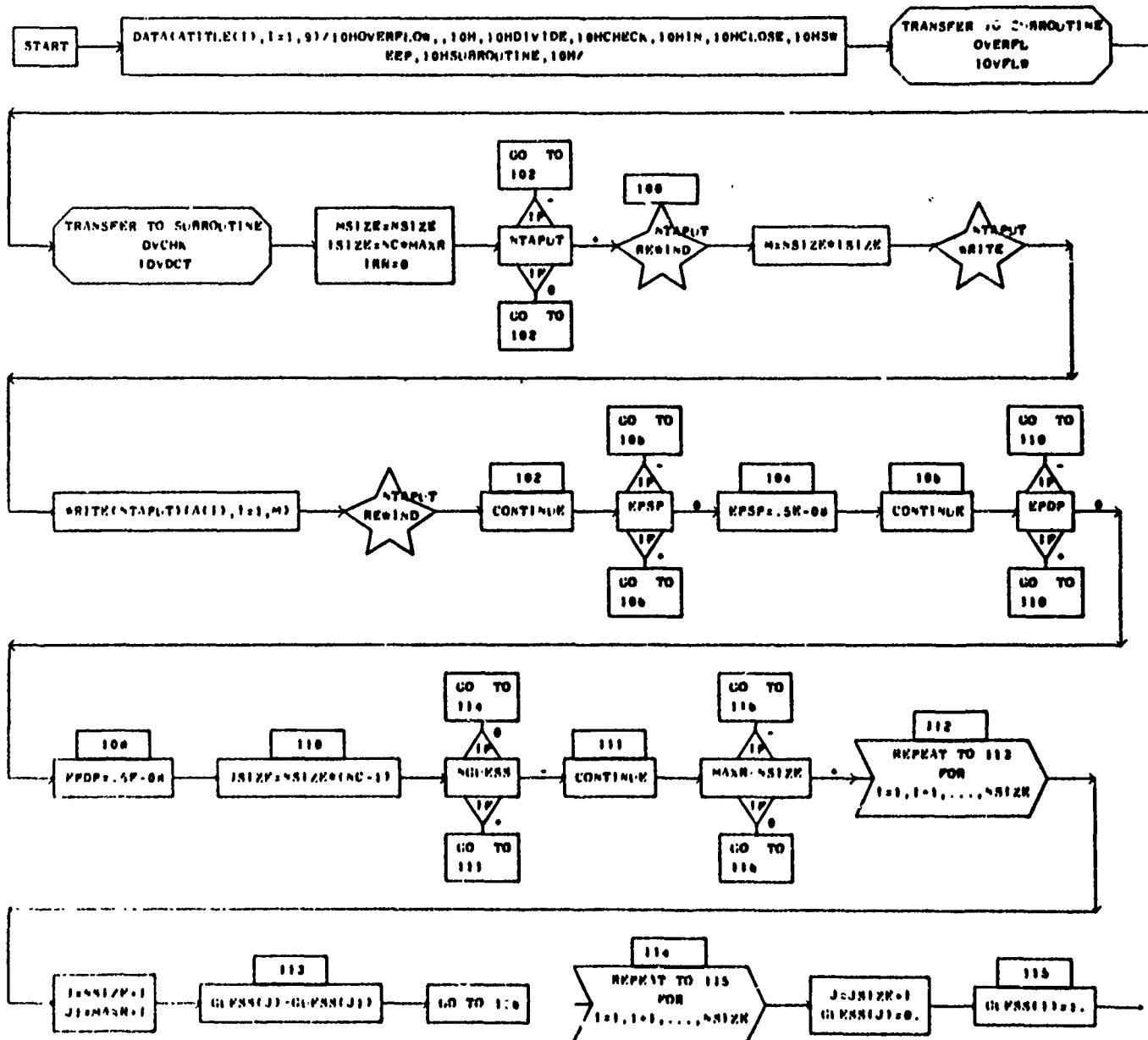
NAKA = DIMENSIONED IN MAXR OF ROWS OF A AND COLUMNS

DIMENSIONED VARIABLES

SYMBOL	STORAGES								
A	1	GUESS	1	H	1	NITER	1	NAKSR	1
NAKD	1	ATITLE	0	VECTOR	1	VALUE	1		

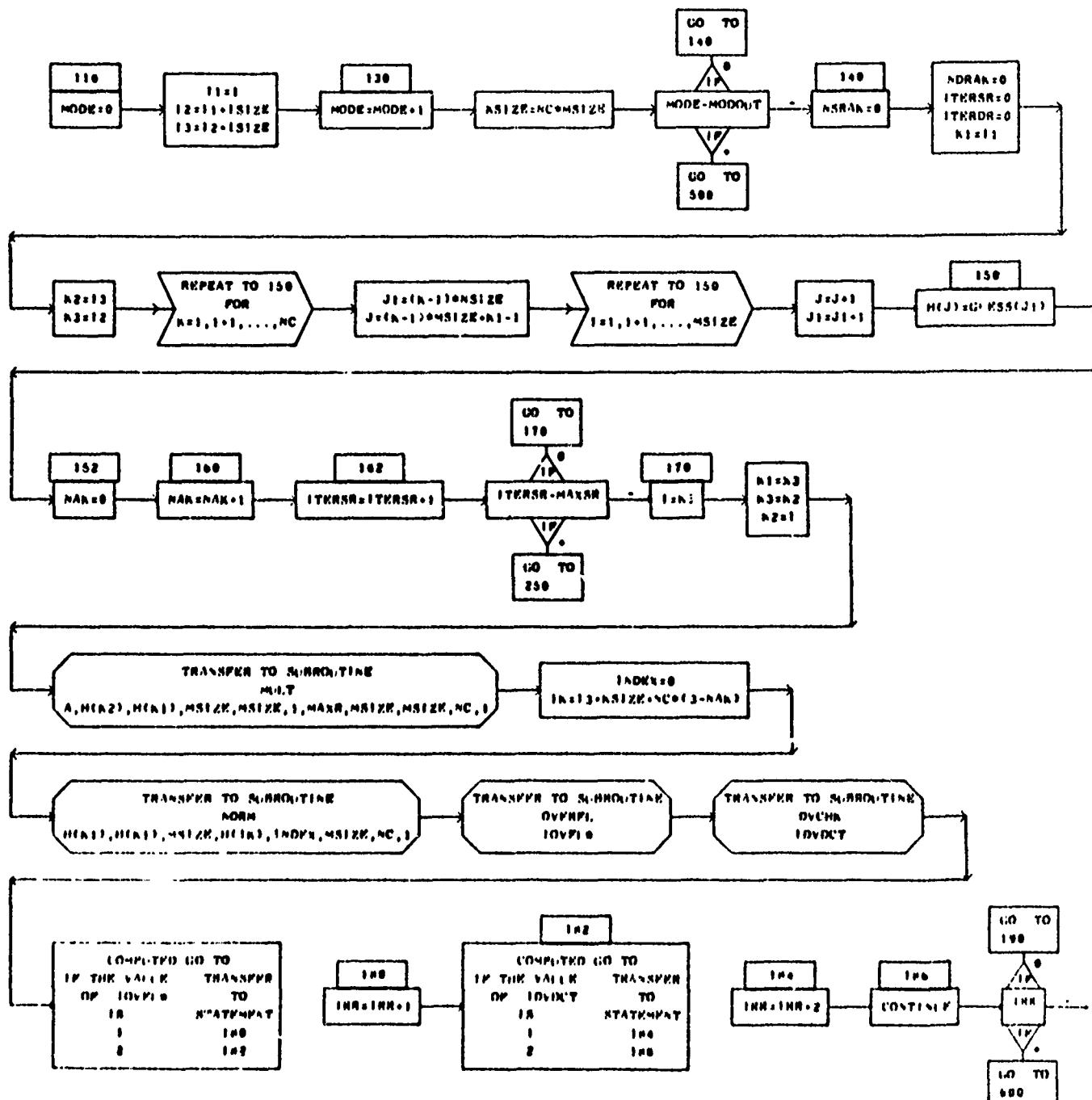
SUBROUTINE MITERSA, GUESS, NOUSS, NSIZE, MODOUT, MAXR, NC, EPSP, EPDP,

PAGE 1



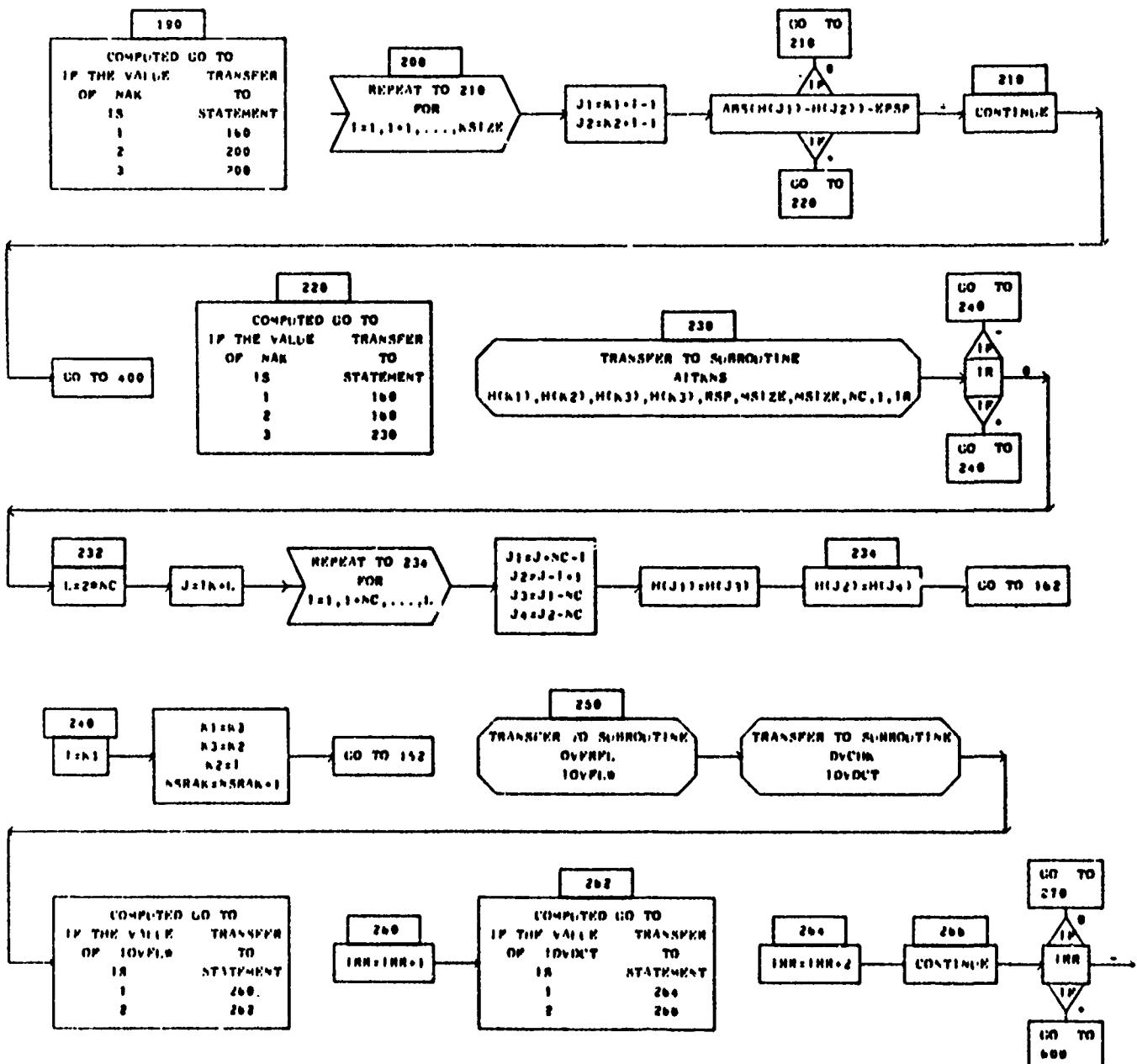
## SUBROUTINE MINTERS(A,GUESS,NGUESS,NSIZEK,MODOUT,MAXR,NC,EPSP,EPDP,

PAGE 2



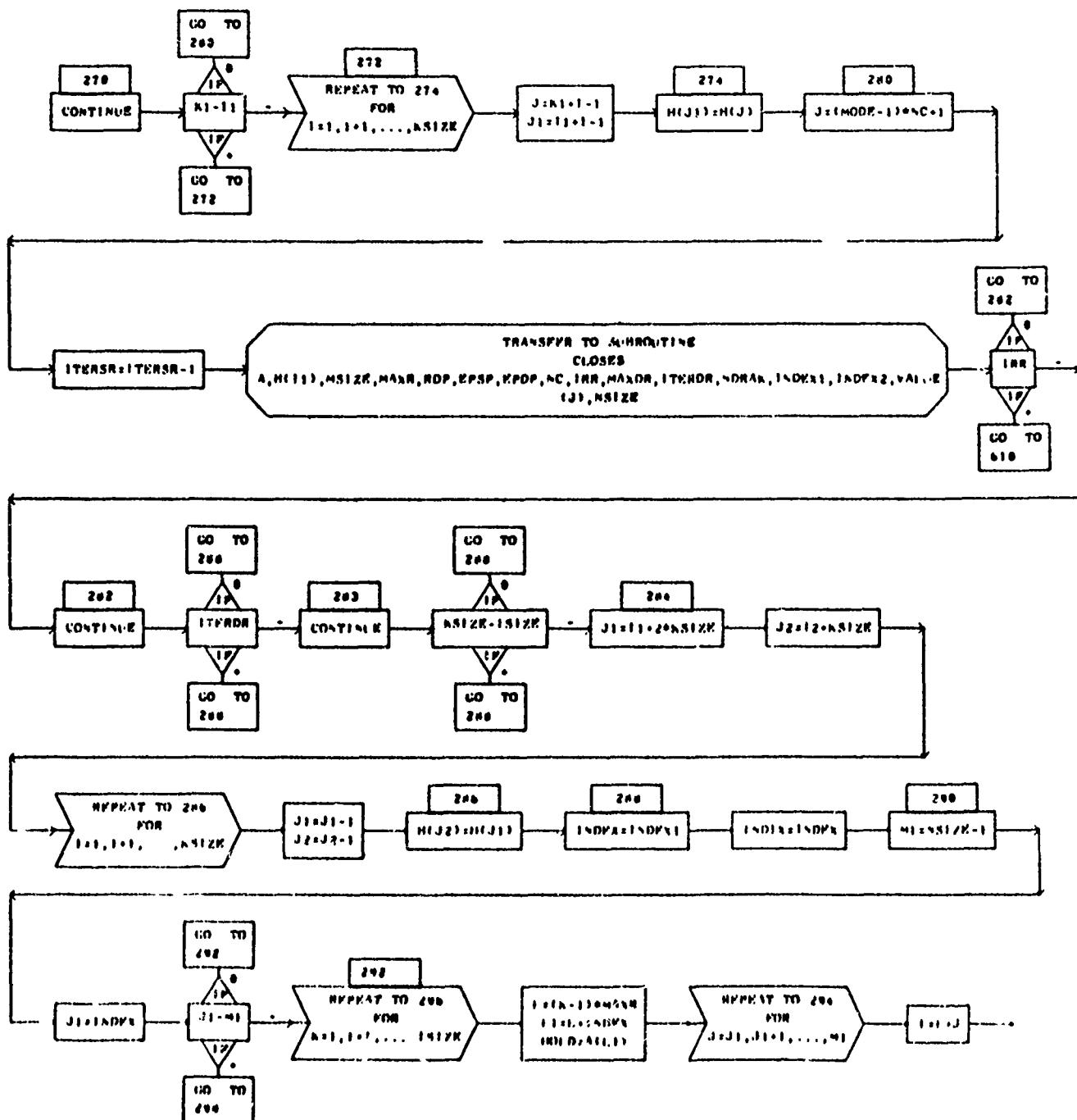
## SUBROUTINE MITERSA, GUESS, NUESS, NSIZE, MODOUT, MAXR, NC, EPSP, EPDP,

PAGE 3



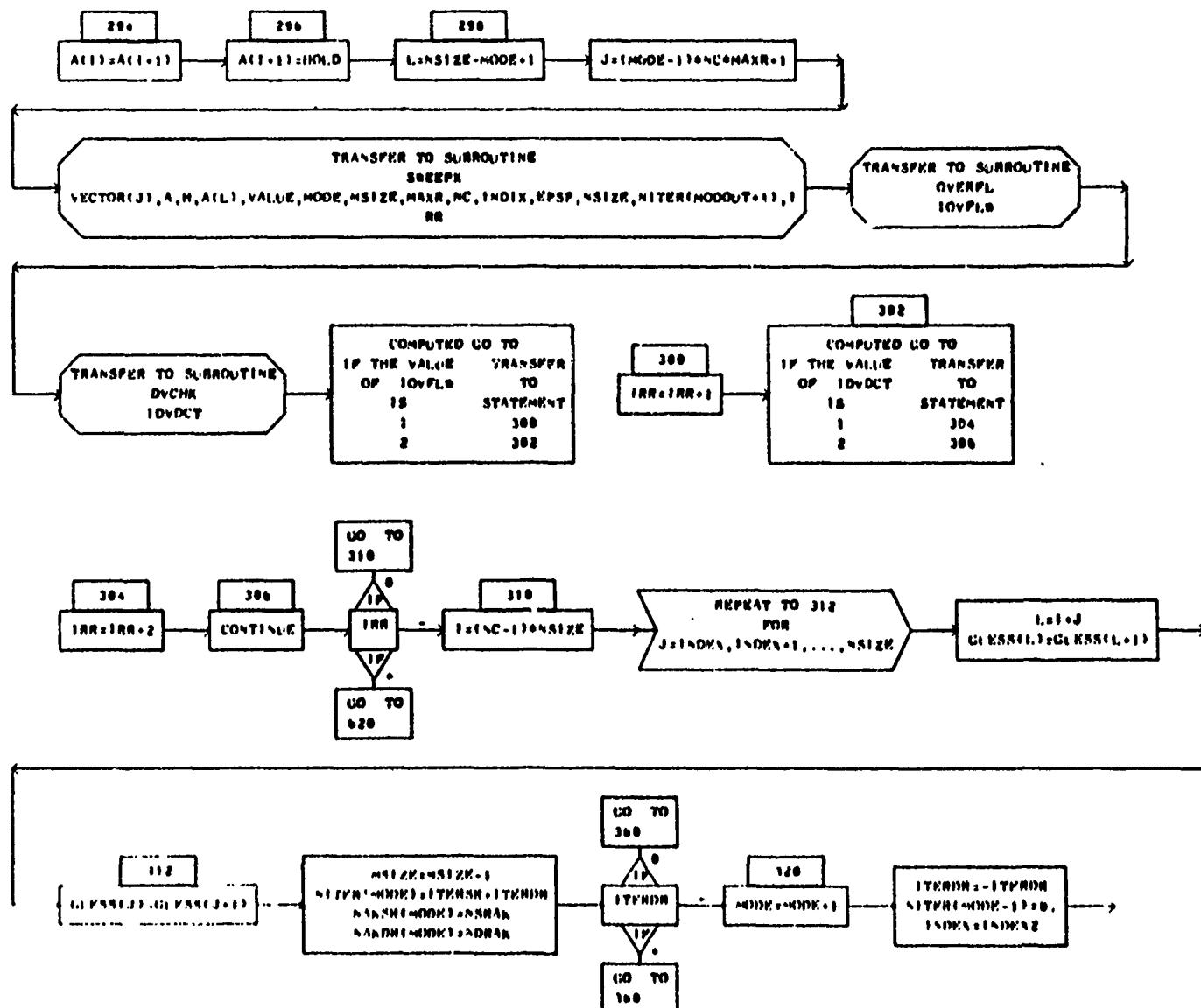
SUBROUTINE MITERSA, GLESS, NGESS, NSIZE, MODOUT, MAXR, NC, EPSP, EPDP,

PAGE 4 1



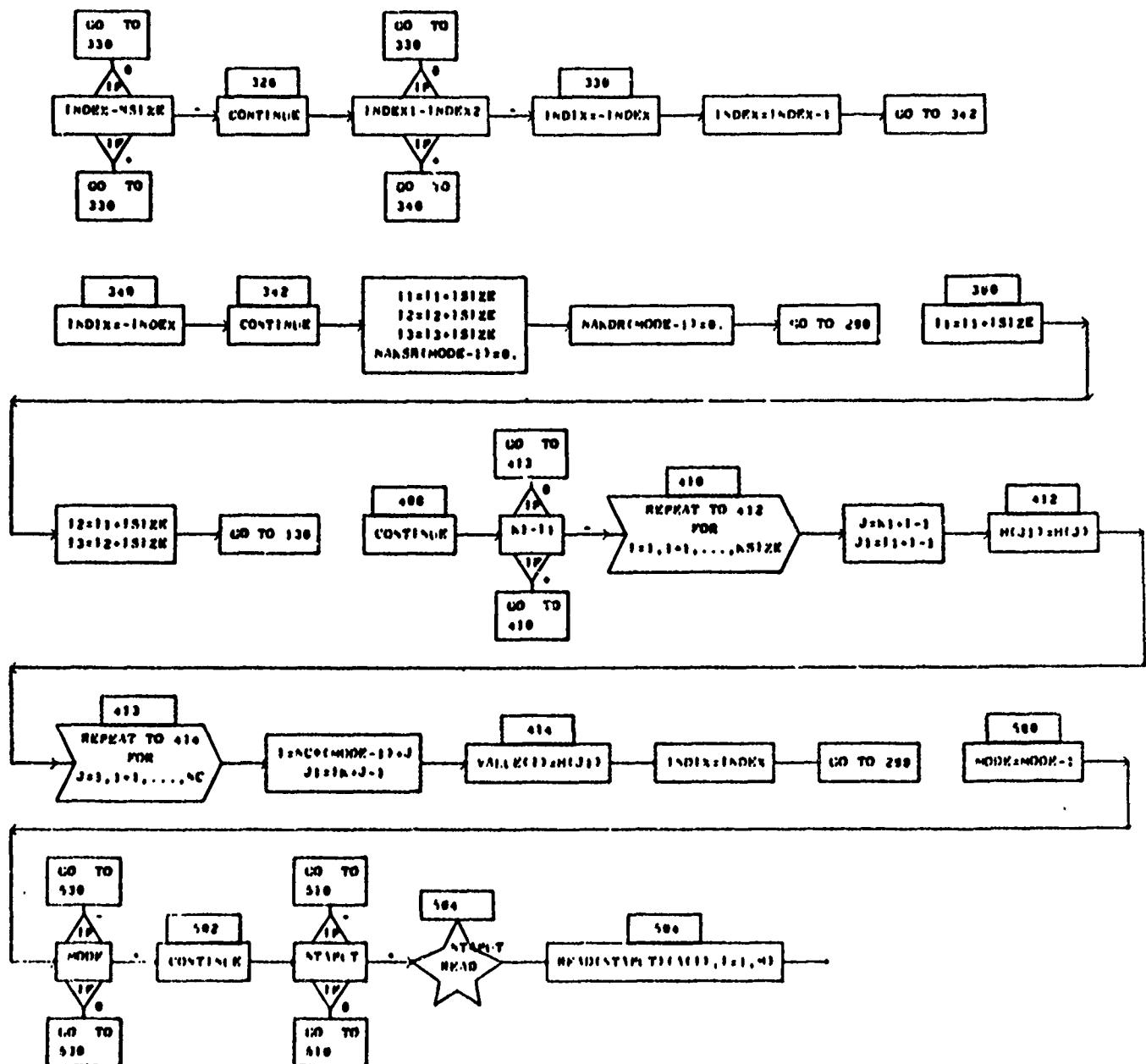
SUBROUTINE NITERSA, GUESS, NGUES, NSIZE, MODOUT, MAXR, NC, EPSP, EPDP.

PAGE 5



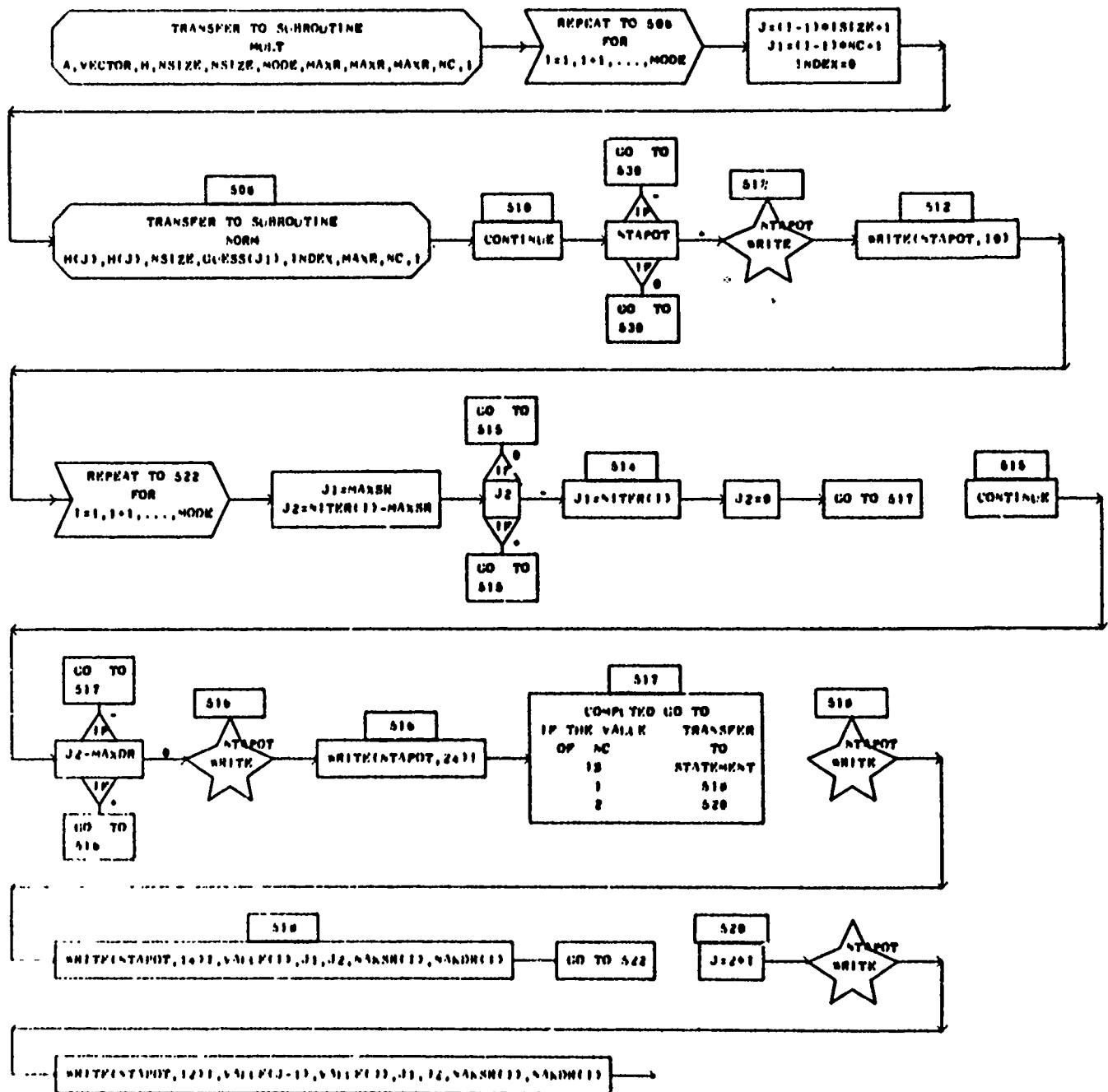
SUBROUTINE MITERSA, G1-KSS, NC1ESS, NSIZE, MODIT, MAXR, NC, KPSP, KPOP,

PAGE 6 1



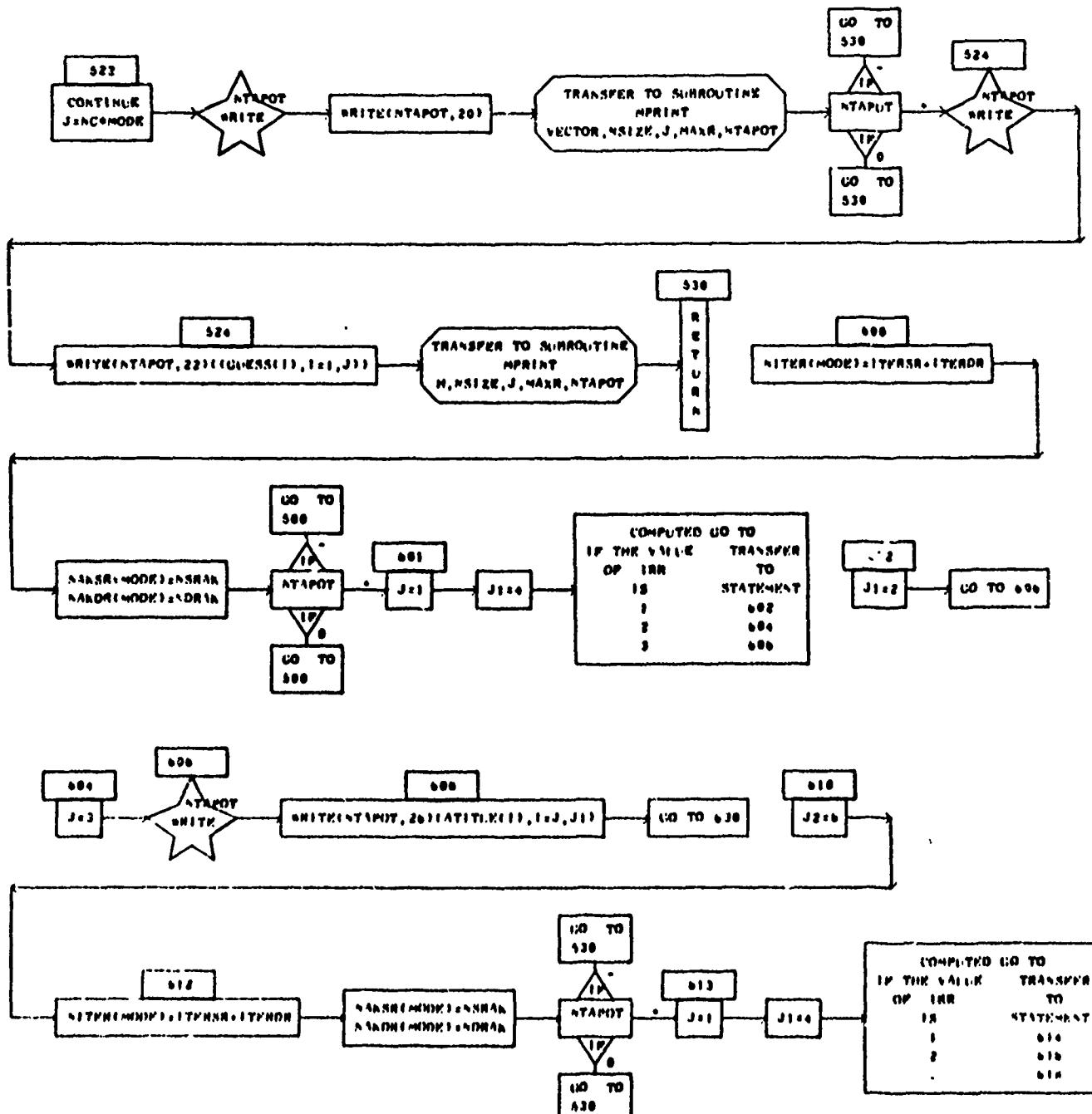
SUBROUTINE MITTERIA, GUESS, NURESS, NSIZE, MODOUT, MAXR, NC, EPSP, KPDP,

PAGE 7 1



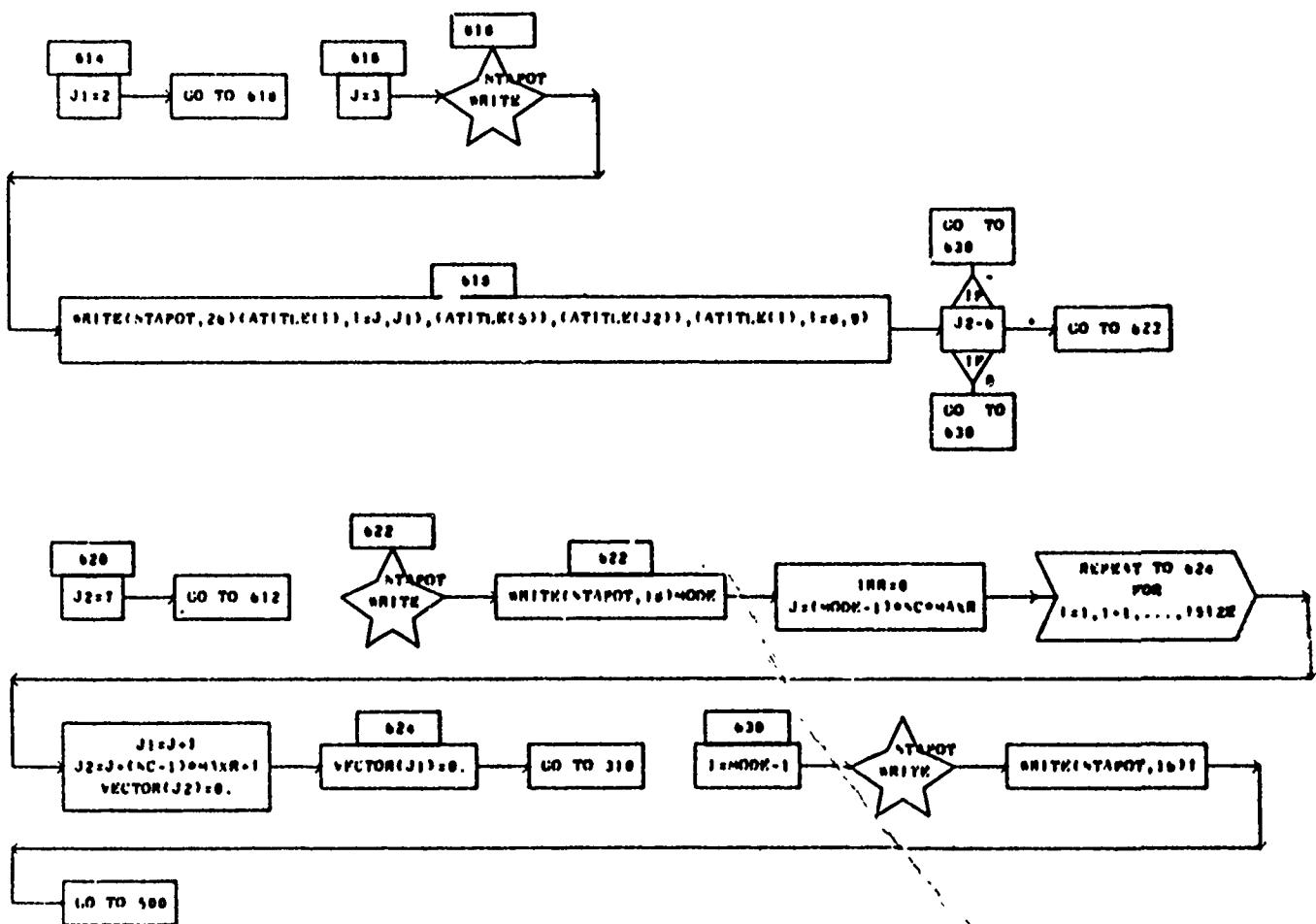
SUBROUTINE MITER(SA,GUESS,NGUESS,NSIZE,MODOUT,MAXR,NC,ZPSP,EPDP,

PAGE 6



SUBROUTINE MINTERSIA,CGUESS,NGUESS,NSIZE,MODOUT,MAXR,NC,EP1P,EPDP,

PAGE 9 1



## SKEEPS

## SUBROUTINE SKEEPS

COMPUTES TRUE MODE AND SKEEPS IT FROM THE MATRIX. (REAL OR COMPLEX)

HTRUE = TRUE MODAL COLUMNS, AS COMPUTED. U = DYNAMIC MATRIX.

H = SERIES OF MODIFIED MODAL COLUMNS. P = COLUMN OF EIGENVALUES.

US = SERIES OF MODIFIED MODAL ROWS OF U.

MODE = MODE NO. BEING COMPUTED. N = SIZE

MD = DIMENSIONED NUMBER OF ROWS OF U, L, R, H, HTRUE

MN = 1 IF PROBLEM IS REAL.

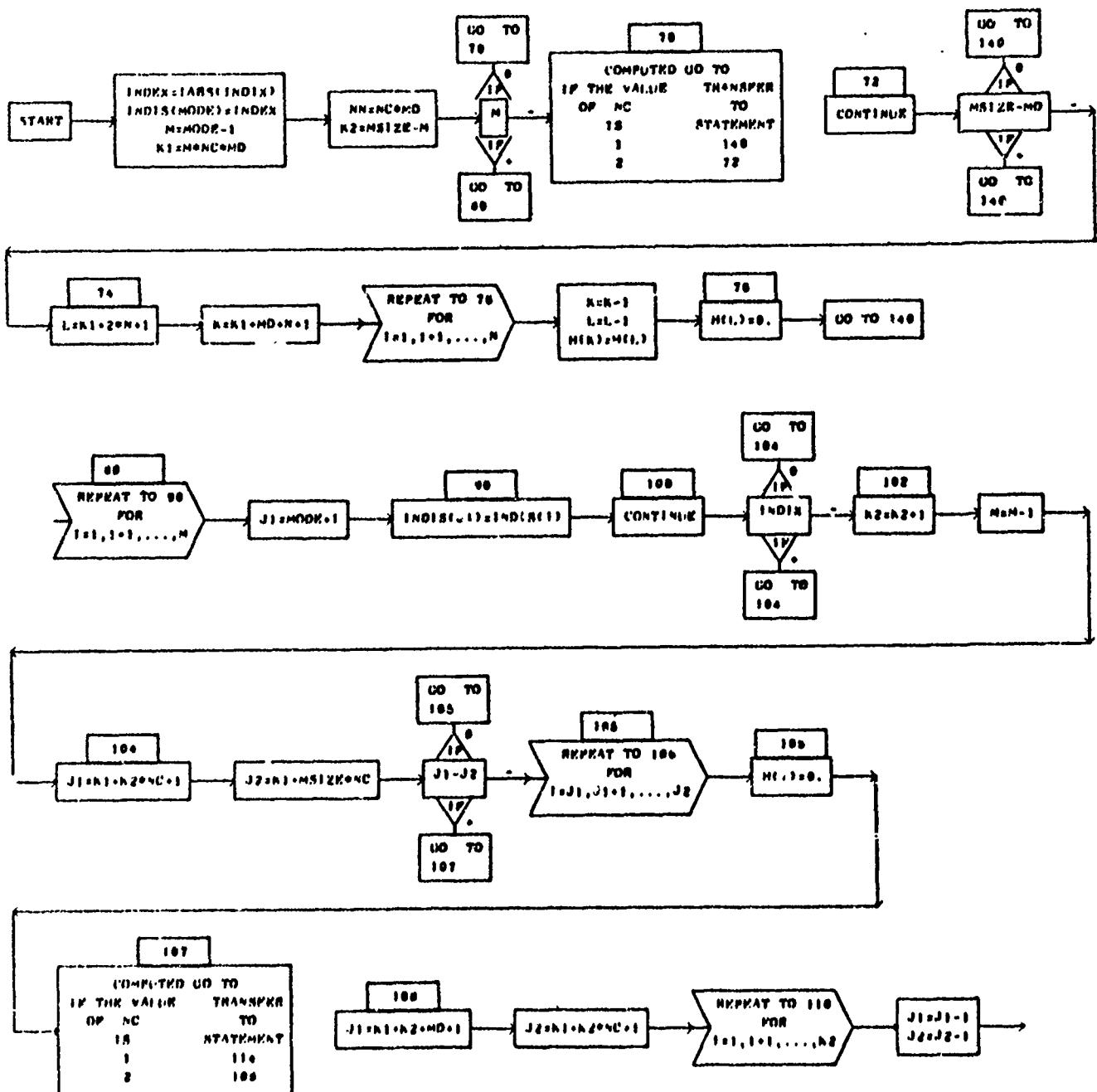
= 2 IF PROBLEM IS COMPLEX.

## DIMENSIONED VARIABLES

SYMBOL	STORAGES								
H	1	US	1	U	1	HTRUE	1	P	1
G	4	INDIS	1						

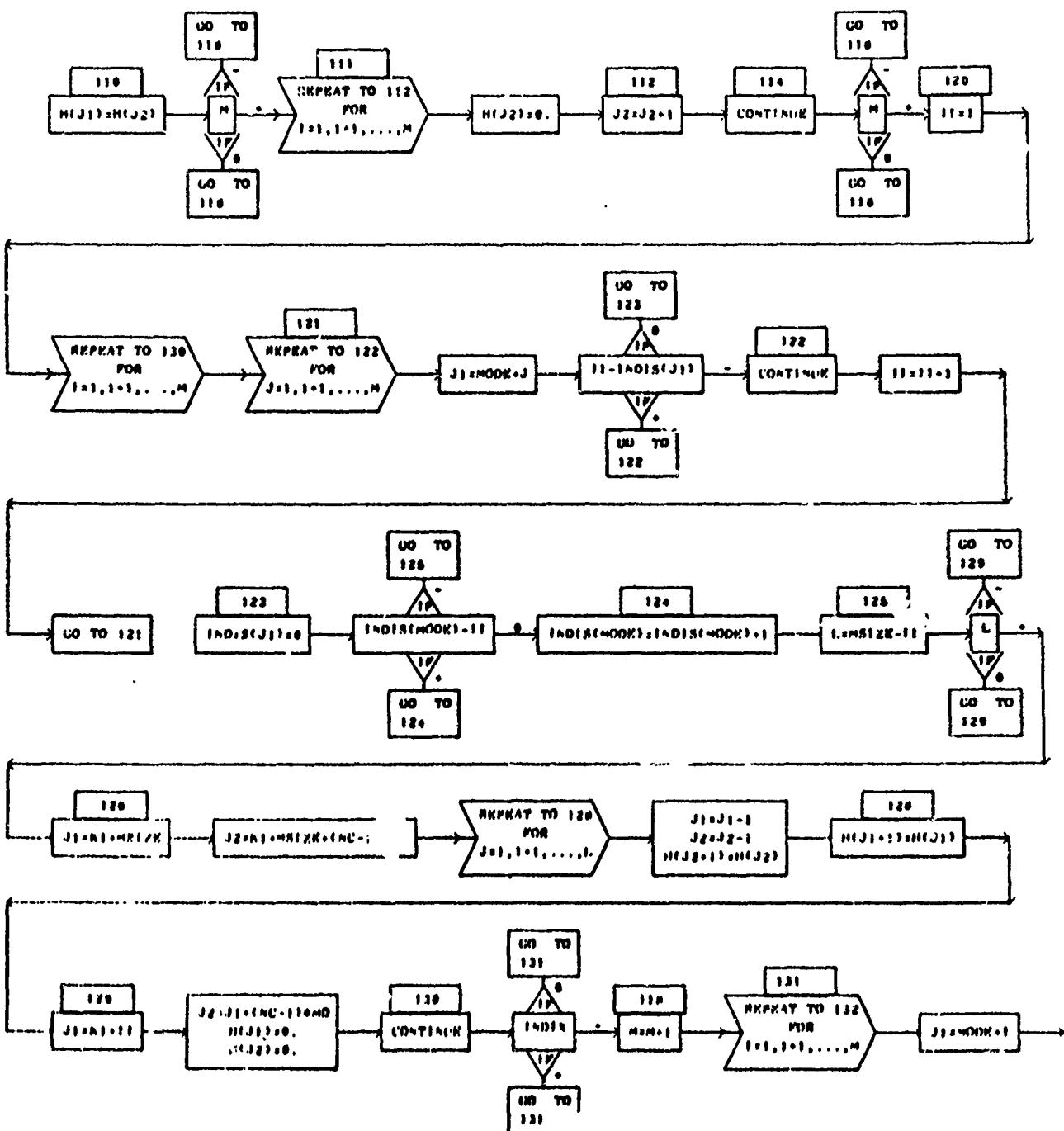
SUBROUTINE SWEEP (INTR, U, M, US, PL, MODE, N, MD, NC, INDX).

PAGE 1



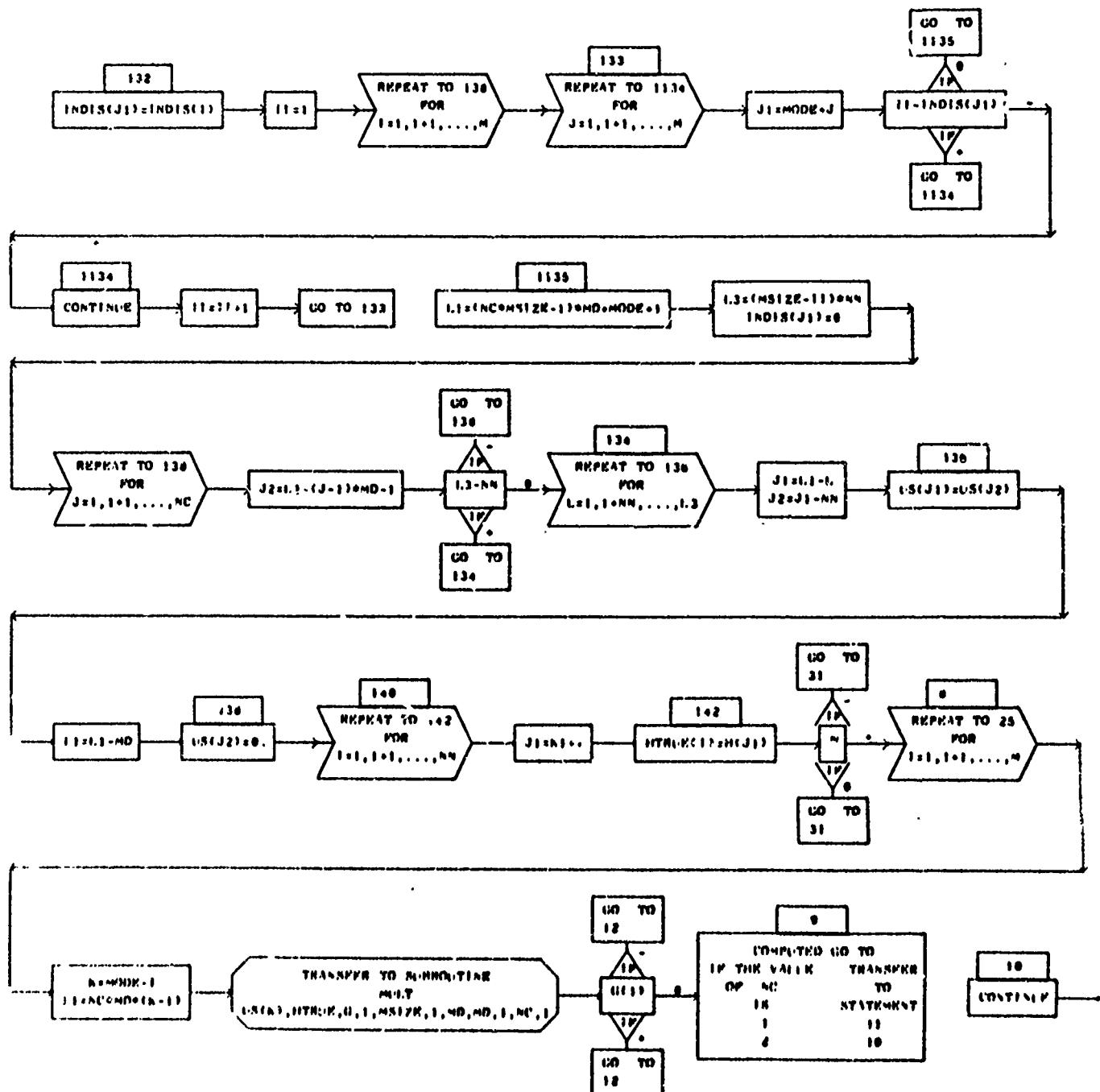
SUBROUTINE SUBRFX (INTRUE, U, H, US, PI, MODE, N, MD, NC, TH0IX).

PAGE 2



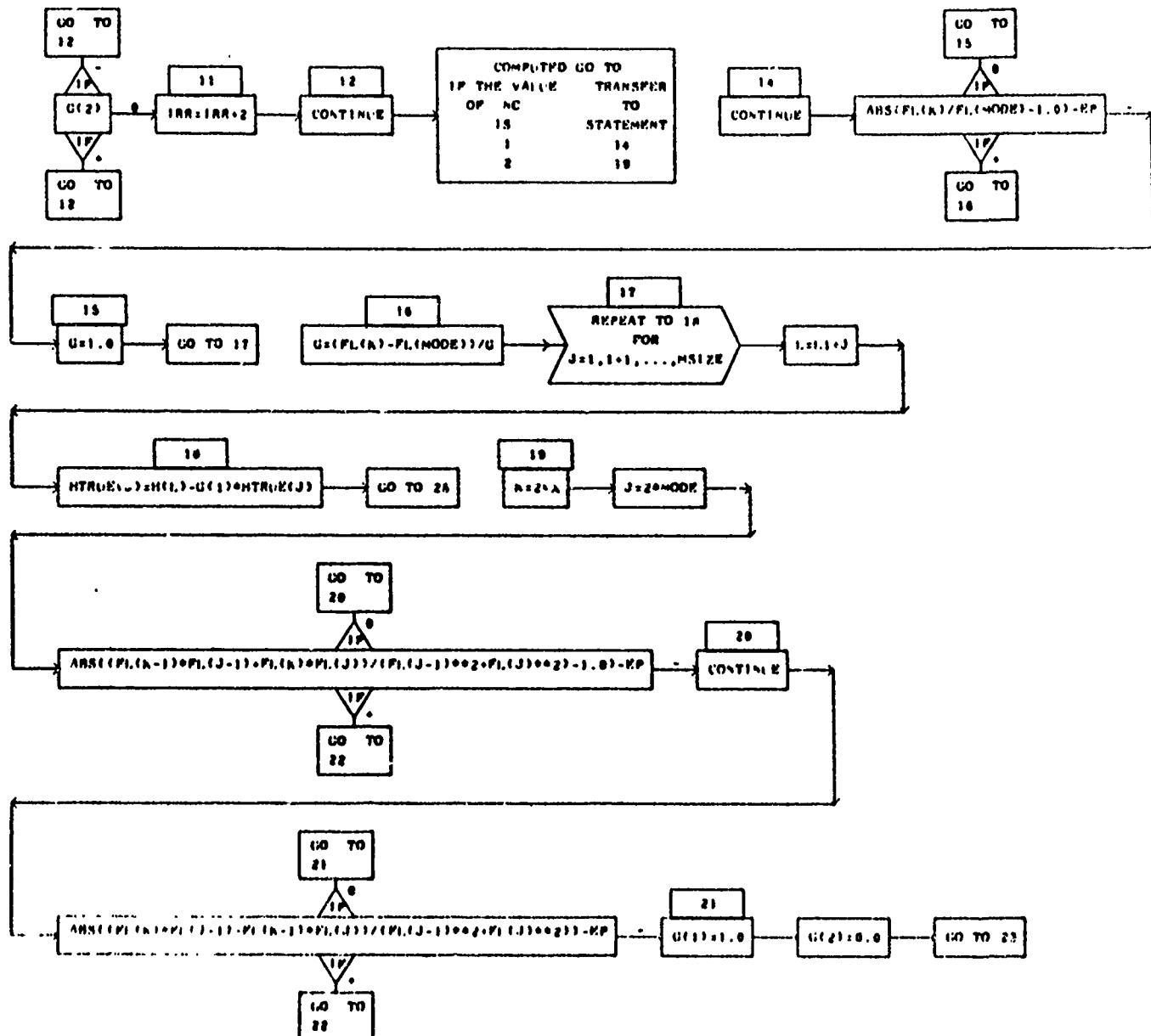
## SUBROUTINE SORPFX (INTRUE, U, N, US, PL, MODE, N, MD, NC, INDEX,

PAGE 3



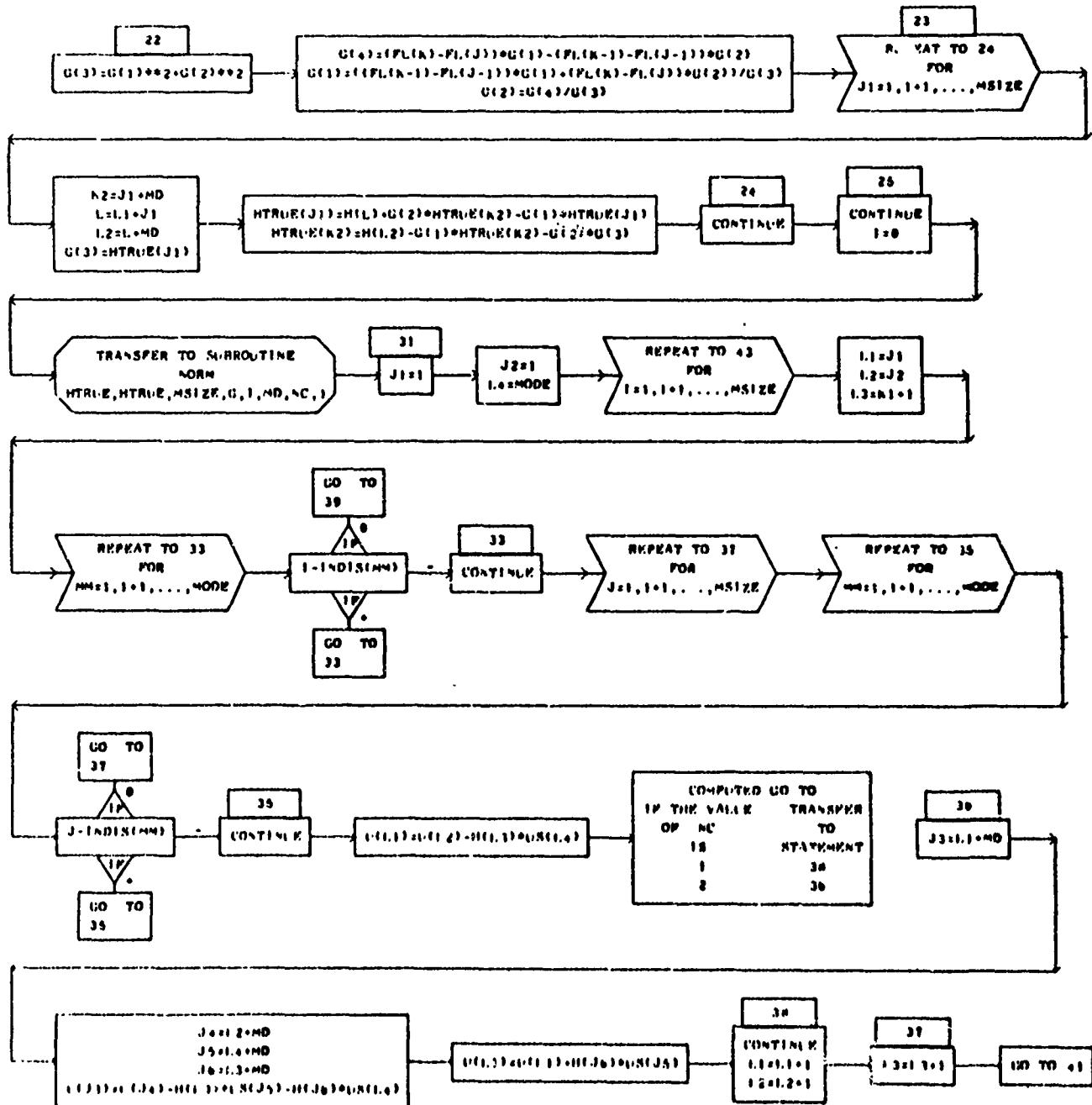
ROUTINE SKEKPx ITRUE, U, H, US, PL, MODE, N, MD, NC, INDEX,

PAGE 4 1



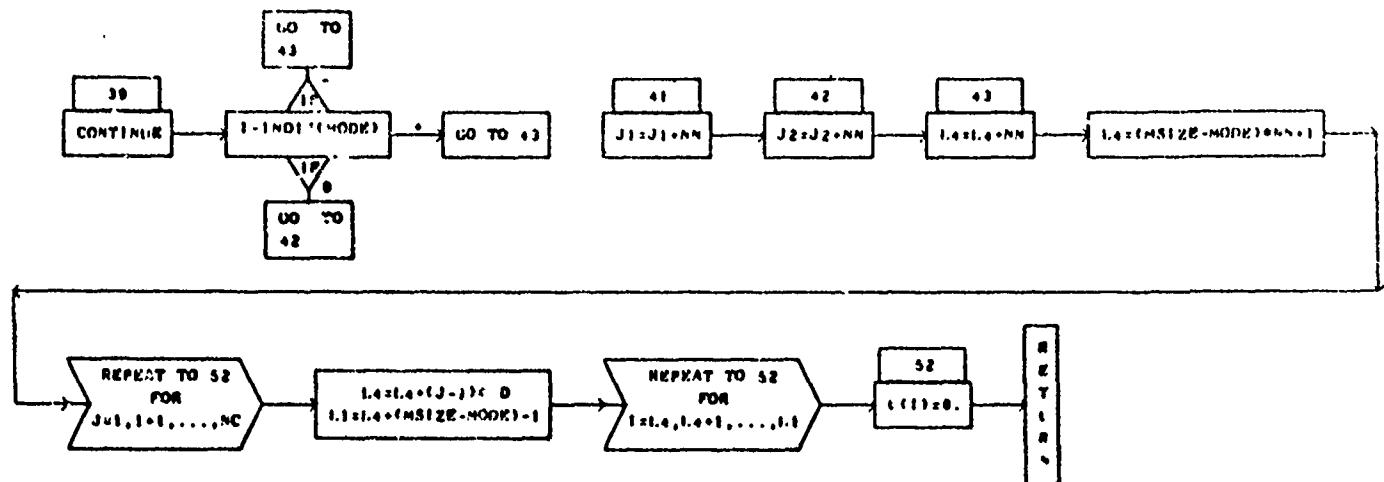
## SUBROUTINE SORPPX (HTRUE, U, H, US, PL, MODE, N, MD, NC, INDEX,

PAGE 5



SUBROUTINE SWEEPX (INTRUP, U, N, LS, PL, MODE, N, MD, NC, INDEX,

PAGE 0 1



## CHANGES

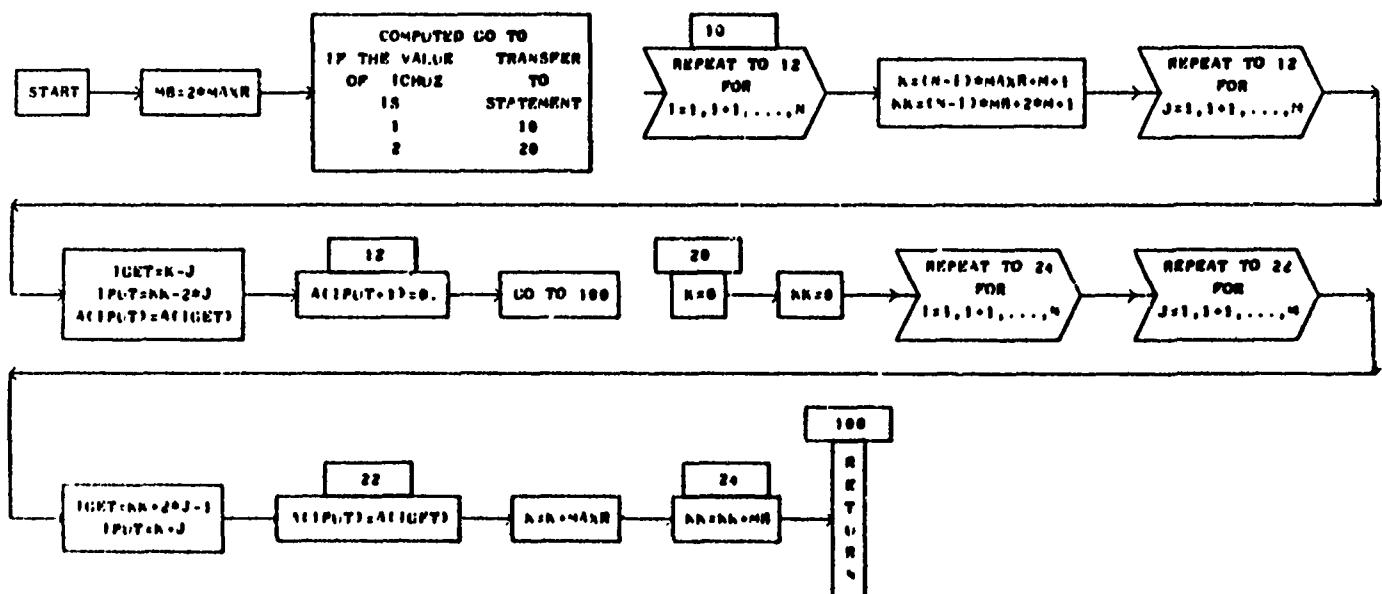
## DIMENSIONED VARIABLES

SYMBOL	STORAGES								
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A      I

## SUBROUTINE CHANGE (A,M,N,MAXR,ICHUS)

PAGE 1



S E C T I O N 10

NOMENCLATURE

## N O M E N C L A T U R E

a	Element of flexibility matrix, in./lb
$a_R$	Generalized amplitude coefficient of rigid-body modal series, in. or rad
$b_r$	Reference semichord, ft
$c_h$	Element of oscillatory aerodynamic influence coefficient matrix, dimensionless
F	Control point force, lb
z	Structural damping coefficient, dimensionless
$h_o$	Control point deflection due to rigid-body motion, in.
$h_R$	Element in rigid-body modal matrix, in. or dimensionless (see Section II)
$h_1$	Control point deflection, in.
K	Flexibility matrix normalizing constant, dimensionless
$k_r$	Reference reduced frequency, dimensionless
M	Element of mass matrix, lb.
$\bar{M}$	Element of complex mass matrix (includes aerodynamic effects), lb
m	Element of generalized mass matrix, lb., in.-lb, or $lb\cdot in^2$ .
$\bar{m}$	Element of sum of generalized mass and aerodynamic matrices, lb, in.-lb, or $lb\cdot in^2$ .
Q	Element of generalized aerodynamic force matrix, lb, in.-lb, or $lb\cdot in^2$ .
R	Number of rigid-body modes
s	Reference semispan, ft (i.e., span measured from root to tip)
U	Element of dynamic matrix, in.
V	Velocity, knots
W	Element of aerodynamic weighting matrix, dimensionless

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SYMBOLS (continued)

$\lambda$  Eigenvalue,  $\lambda = \lambda_R + i\lambda_I$ , in.

$\rho$  Atmospheric density, slugs/ft<sup>3</sup>

$f$  Frequency, cps

Matrix Notation

[ ] Square

{ } Column

[ ]<sup>T</sup> Transposed

[ I ] Unit

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13. ABSTRACT

THIS STUDY COVERS THE DEVELOPMENT OF A SET OF COMPUTER PROGRAM TO PERFORM FLUTTER ANALYSIS BY THE COLLOCATION METHOD. WHILE THIS METHOD HAS BEEN KNOWN FOR SOME TIME, ONLY RECENTLY HAVE ADVANCES IN COMPUTER TECHNOLOGY MADE THE METHOD TECHNICALLY AND FINANCIALLY FEASIBLE. THE INGREDIENTS OF A COLLOCATION FLUTTER ANALYSIS ARE 1) A FLEXIBILITY MATRIX, 2) AERODYNAMIC INFLUENCE COEFFICIENT MATRIX, AND 3) AN EIGENVALUE SOLUTION. THIS STUDY IS PRESENTED IN FOUR VOLUMES. VOLUME I CONTAINS A GENERAL PROGRAM DISCUSSION. VOLUME II CONTAINS THE PROGRAM FLUENC WHICH CALCULATES THE FLEXIBILITY MATRIX. VOLUME III CONTAINS A SET OF THREE PROGRAMS TO CALCULATE AERODYNAMIC INFLUENCE COEFFICIENTS FOR SUBSONIC, TRANSONIC, AND SUPERSONIC FLIGHT REGIMES. VOLUME IV CONTAINS THE PROGRAM COFA WHICH SETS UP AND SOLVES THE FLUTTER EIGENVALUE MATRIX.

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FLUTTER VIBRATION AERODYNAMIC INFLUENCE COEFFICIENTS						

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